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Integrated Composite Analyzer (ICAN)

Users and Programmers Manual

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Summary

This manual describes the use of and relevant equations programmed in a computer code designed to carry out a comprehensive linear analysis of multilayered fiber composites. The analysis contains the essential features required to effectively design structural components made from fiber composites. The program is an outgrowth of two in-house computer codes, MFCA (Multilayered Filamentary Composite Analysis) and INHYD (Intraply Hybrid Composite Design). The inputs to the code are constituent material properties, factors reflecting the fabrication process, and composite geometry. The code performs micromechanics, macromechanics, and laminate analysis, including the hygrothermal response of fiber composites. The code outputs are the various ply and composite properties, composite structural response, and composite stress analysis results with details on failure. The code is in Fortran IV and can be used efficiently as a package in complex structural analysis programs. The input-output format is described extensively through the use of a sample problem. The code manual consists of two parts. The mechanics for using the code are described in the first part, the pertinent equations programmed in the code are described in the second part.

Introduction

The importance of and need for a multilevel analysis used for designing structural components made of multilayered fiber composites are documented in reference 1. A multilevel analysis, which was efficient in predicting the structural response of multilayered fiber composites (with the constituent material properties, the fabrication process, and the composite geometry known), is also documented in reference 1.

The multilayered analysis presented in reference 1 consists of (1) micromechanical theories for the thermoelastic properties and the stress-level limit of the single ply as functions of constituent material properties and the particular fabrication process, (2) the combined stress-strength criterion for the single ply, and (3) multilayered composite structural response and analysis (macromechanical or laminate analyses), where the interply layer effects are taken into account. A computer code designed to carry out this multilevel analysis, supplemented as noted by references 2 to 10, has been developed at the Lewis Research Center. This code is identified as MFCA for Multilayered Filamentary Composite Analysis (ref. 11).

Intraply hybrid composites are a logical sequel to conventional and interply hybrid composites. Recently, theoretical and experimental investigations have been conducted on the mechanical behavior of intraply hybrids at the Lewis Research Center (refs. 12 to 14). The theoretical methods and equations described in these references, together with those for hygrothermal effects (ref. 15), have been integrated into a computer code for predicting hygral, thermal, and mechanical properties of intraply hybrid composites. This information can then be used in designing these composites. This code is identified as INHYD for Intraply Hybrid Composite Design (refs. 16 and 17).

The present computer code is a synergistic combination of the aforementioned computer programs MFCA and INHYD together with several significant enhancements. The code is referred to as ICAN for Integrated Composite Analyzer. It utilizes the micromechanical design of INHYD and the laminate analysis of MFCA to build a comprehensive analysis capability for structural composites. Additional features unique to ICAN are the following:

1

- (1) Ply stress-strain influence coefficients
- (2) Microstresses and microstress influence coefficients
- (3) Stress concentration factors around a circular hole
- (4) Calculation of probable delamination locations around a circular hole
- (5) Poisson's ratio mismatch details near a straight free edge
- (6) Free-edge stresses
- (7) Material cards for finite-element analysis using NASTRAN or MARC
- (8) Failure loads, summary based on the maximum stress criterion and laminate failure stresses, and summary based on first-ply failure and fiber breakage criteria
 - (9) Transverse shear stresses and normal stresses

In addition to the above, ICAN has its own data base of material properties for commonly used fibers and matrices. The user needs to specify only the coded names for the constituents. The program searches and selects the appropriate properties from its library. Furthermore, input data preparation has been simplified substantially by the introduction of a partial free-field format. The output formats have also been improved significantly to ease user interpretation of the results. These enhancements make ICAN significantly more user friendly than its predecessors. The computer code has been programmed in Fortran IV and has been tested in UNIVAC 1108, IBM 370, and CRAY 1 computers.

Since this report is to serve as a users manual, the code is divided into two parts, the users manual and the programmers manual. The Users Manual describes the mechanics of using the code with respect to program format, input and output, and sample input data sets. The descriptions are extensive enough so that even designers and analysts with little or no programming experience can easily use the code.

The programmers manual gives the various subroutine descriptions and the equations programmed therein, with details on the input and output and the global storage locations. This, along with the listing of the source program, allows the user to make his own modifications to the code as they become appropriate for further enhancements.

The Fortran variables are defined in appendix A. Included is information such as which part of the program of each global variable is generated. Table I provides a summary of details for preparing data cards, and the input data given in table II provide for immediate testing of the code. Properties for a few commonly used fibers and matrix materials are listed in appendix B. Appendix C shows sample input and output data for a specific case.

Symbols

A_{cx}	composite axial stiffness
A_{cx}^R	reduced axial stiffness
BIDE	boolean, true if interply effects are included
C_{cx}	composite coupling stiffness
C_{e1}	string with force variables
C_{e2}	string with displacement variables
COMSAT	boolean, true if laminate analysis is wanted
CSANB	boolean, true if membrane and axial symmetry exists
D_c , D_ℓ	moisture diffusivity
D_{cx}	composite flexural rigidity
D_{cx}^R	reduced bending rigidity
\mathbf{D}_v	displacement vector
d_f	filament equivalent diameter
E_f , E_{cf}	filament elastic constants
E_{f11} , etc.	fiber normal modulus
$E_{\ell}, E_{c\ell}$	ply elastic constants

 $E_{\ell 11}$, etc. ply normal modulus E_m, E_{cm} matrix elastic constants

 E_{m11} , etc. matrix normal modulus

 $\mathcal{E}_{m,etc}$ matrix failure strain allowables F combined stress-failure function

 G_{f12} , etc. fiber shear modulus G_{f12} , etc. ply shear modulus G_{m12} , etc. matrix shear modulus

 H_j interply distortion energy coefficient H_{kc} array of constituent heat conductivities

h_c composite heat capacity

i,j index, generally ply or interply

 $K_{c11,c22,c33}$ composite three-dimensional heat conductivities $K_{cxx,cyy,cxy}$ composite two-dimensional heat conductivities

 K_{f11} fiber heat conductivity K_{f11} ply heat conductivity K_{m11} matrix heat conductivity k_v apparent void volume ratio k_f actual fiber volume ratio

 $k_{f\ell}$ ply apparent fiber volume ratio k_m actual matrix volume ratio

 $k_{m\ell}$ ply apparent matrix volume ratio $k_{v\ell}$ ply apparent void volume ratio L_{sc} array of limiting conditions

 M_{ℓ} ply moisture M_{cx} applied moment $M_{cM_{\ell}x}$ hygral moment $M_{cT_{\ell}x}$ thermal moment

m load condition index N_{cx} applied membrane loads

 N_{cM_tX} hygral force N_{cT_tX} thermal force

 N_f number of fibers per end

 N_{ℓ} number of plies

 $N_{\ell c}$ number of load conditions

NONUDF boolean; true if detailed Poisson's ratio differences chart is to be suppressed

 N_{pc} string PROPC length $N_{p\ell}$ string PROP length

 P_c composite properties array

 P_{cp} string PROPC

 P_{ℓ} ply properties array

 $P_{\ell p}$ string PROP main program $Q_{f,i,p,r,s}$ indices to print out string PROP

R transformation matrix

RINDV boolean; true if displacements are known

 S_c composite failure stress $S_{\ell 11T}$, etc. ply limit failure stresses T_{ℓ} ply temperature ply thickness t_{ℓ} composite local curvature changes w_{cb} structural reference axes x, y, zcomposite coefficient of thermal expansion α_c fiber thermal coefficient of expansion α_f ply thermal coefficient of expansion α_{ℓ} matrix thermal coefficient of expansion α_m moisture expansion coefficients β_c β_e, β_ϵ correlation factors for ply thermoelastic properties correlation factor for ply heat conductivity β_h $\beta_{\ell}, \beta_{f}, \beta_{m}$ moisture expansion coefficients for ply, fiber, and matrix β_s correlation factor for ply strength β_v matrix strain magnification due to ply strain in the presence of voids δ_f interfiber spacing $\delta_{\vec{r}}$ interply layer thickness δ_s interfiber spacing angle between composite material and structural axes ϵ_{cs} ϵ_{csx} reference plane membrane strain ply strain ϵ_{ℓ} $\theta_{\ell i}, \theta_{\ell c}$ angle between ply material and composite axes ν_{f12} , etc. fiber Poisson's ratio ply Poisson's ratio $\nu_{\ell 12}$, etc. matrix Poisson's ratio ν_{m12} , etc. fiber and matrix weight density $\rho_{f,m}$ density of matrix with moisture ρ_{mw} ply stresses, fiber stresses, and matrix stresses $\sigma_{\ell}, \sigma_{f}, \sigma_{m}$ 1, 2, 3 material reference axes

Users Manual

The mechanics required to use this code for the analysis of multilayered fiber composites are described in this part of the report. The theory on which the code is based is described in the second part of the report (Programmers Manual).

The physical representations of the constituents used in the code are illustrated in figure 1. This figure shows a complete integration schematic starting with the constituent materials, fiber and matrix. The required input properties and computed properties at various levels are summarized in symbolic form as follows:

- (1) Properties required by code as input for a fiber: $E_{f11,22,33}$; $v_{f12,23,13}$; $G_{f12,22,13}$; $\alpha_{f11,22,33}$; $K_{f11,22,33}$; H_{cf} ; ρ_f ; N_f ; d_f ; and S_{ft} .
- (2) Properties required by code as input for a matrix: $E_{m11,22,33}$; $\nu_{m12,23,13}$; $G_{f12,23,13}$ $\alpha_{m11,22,33}$;
- $K_{m11,22,33}; H_{cm}; \rho_m; S_{mc}; \varepsilon_{mpc}; \varepsilon_{mpc}; \varepsilon_{mps};$ and ε_{mpTOR} .

 (3) Properties required by code as input for a single ply: fiber and matrix properties and ply characteristics β_{ρ} , β_{n} , β_{s} , and T_{f} .

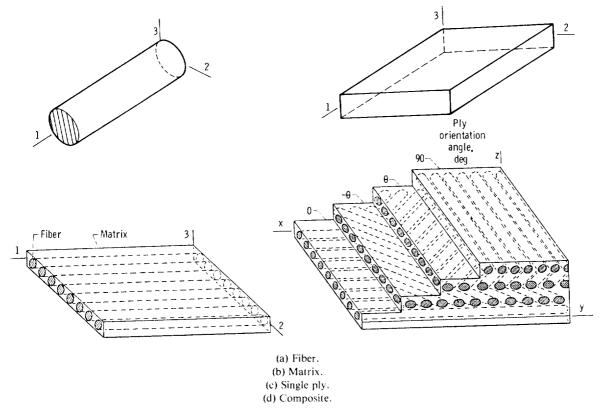


Figure 1.—Schematic of typical multilayered fiber composite and some basic components.

- (4) Properties computed by code for single ply: $E_{\ell 11,22,33}; \nu_{\ell 12,23,13}; G_{\ell 12,23,13}; \alpha_{\ell 11,22,33}; K_{\ell 11,22,33}; H_{c\ell}; \rho_{\ell}; t_{\ell}; \delta_{\ell}; S_{\ell 11T,11C,22T,22C,12S,23S}; K_{\ell 12};$ and stress analysis factors $\epsilon_{\ell 11,22,12}; \sigma_{\ell 11,22,12};$ and $1.0-F(\sigma,S,K_{\ell 12}).$
- (5) Properties required by code as input for a composite: ply properties and composite characteristics $\theta_{\ell l}$, H_j , $K'_{\ell l 2\alpha\beta}$, N_{cx} , M_{cx} or U_{cx} , and W_{cx} . (6) Output computed by code for a composite: $\{\epsilon_{cx}\} = [E_c|\{\sigma_c\} + T_{\ell}\{\alpha_c\}; |E_c|^{-1}; K_{cxx,yy,xy}; H_c;$

$$\begin{pmatrix}
N_{cx} \\
M_{cx}
\end{pmatrix} = \begin{bmatrix}
A_{cx}C_{cx} \\
C_{cx}D_{cx}
\end{bmatrix} \quad
\begin{pmatrix}
U_{cx} \\
W_{cx}
\end{pmatrix} + \begin{pmatrix}
N_{cx}T_{\ell} \\
M_{cx}T_{\ell}
\end{pmatrix}$$

and the inverse $\Delta \varphi_{\text{deli}}$.

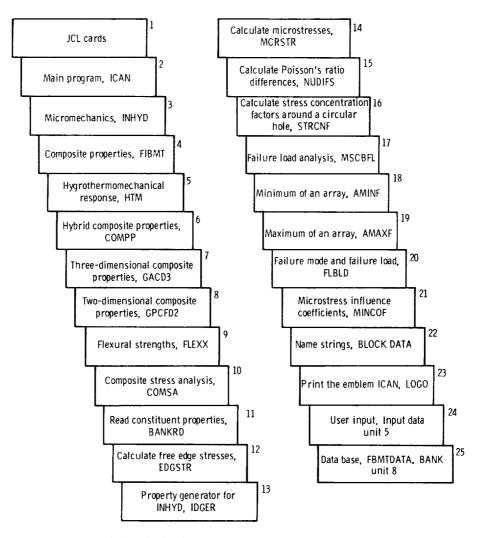
Figure 2(a) shows the subroutines and sequence in the code. The subroutines between the Main program and the input data may be arranged in any desired order. The user should refer to figure 2(b) for the logic flow of the analysis.

The following four steps are required to use the code in the user's computer facility:

- (1) Obtain the code
- (2) Make it operational in the user's computer facility
- (3) Supply the input data
- (4) Interpret the code output results

Obtain the Code

The code may be obtained in cards. If this is not convenient or possible, the cards can be punched from the compiled listing (contact COSMIC, The University of Georgia, Athens, GA 30602, concerning the availability of this program).



(a) Schematic showing subroutines and sequence of ICAN code.

Figure 2.—Subroutines, sequence, and logic flaw of ICAN code.

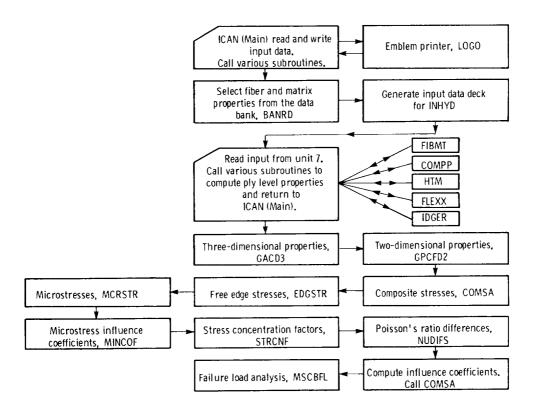
Make it Operational

A prerequisite to the program is the availability of a Fortran compiler in the user's computer facility. To run the program, certain computer-system-dependent control cards (Job Control Language (JCL) cards) may also be necessary. The computer system personnel should be consulted about these items.

Once the deck of cards has been assembled (except input data) with the proper control cards as shown in figure 2, the user is ready to compile the code in his facility. The compilation will indicate whether any additional modifications are needed. Most modifications will be minor and will usually deal with certain Fortran statements peculiar to each compiler.

Supply the Input Data

The physical arrangement of the input data cards is illustrated in figure 3. Details for preparing the input data cards are summarized in table I. A detailed description of these cards is given subsequently. A sample for preparing input data for a four-ply symmetric laminate is presented in table II. This laminate has two different material systems. The 0° plies are of AS graphite fiber/intermediate-modulus, low-strength epoxy matrix composite. The 90° plies are made of a hybrid composite. The primary composite is S glass/high-modulus, high-strength epoxy. The secondary composite is AS graphite/intermediate-modulus, high-strength epoxy.



(b) Schematic showing logic flow of ICAN code.

Figure 2.—Concluded.

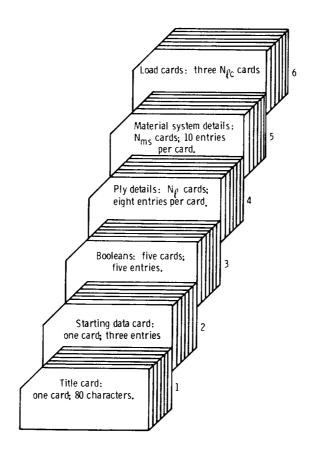


Figure 3.—Physical arrangement of input data cards.

TABLE I.—SUMMARY OF DETAILS FOR PREPARING INPUT DATA CARDS

Card group	Identification	Code symbol	Number of entries	List of entries, sequential order	Card field columns	Format	Comments and engineering units
1	Title card	TITLE	80	Alphabetic characters	1 to 80	(10a8)	
2	STDATA	NL,NLC.NMS	3	$N_{\ell}, N_{\ell c}, N_{ms}$	9 to 36	(a8,3I8)	Composite geometrics
3	Boolean for input displacement	RINDV	1		1 to 6		T (true) if displays are inputs; otherwise F (false)
	Boolean for interply layer energy contribution	BIDE	1		1 to 6		T (true) if contributions are desired; otherwise F (false)
	Boolean for mem- brane and bending symmetry	CSANB	1		1 to 6	(L6)	T (true) if symmetry exists; otherwise F (false)
	Boolean for laminate analysis	COMSAT	1		1 to 6		T (true) if laminate analysis is desired; otherwise F (false)
	Boolean for Poisson ratio chart	NONUDF	l		1 to 6		T (true) if Poisson ratio differences chart is not desired; otherwise F (false)
4	PLY (ply desired)	INPI,IPI,TU,TCU DELM,TETA,THCKNS	7	$i,j,T_u, \ T_{cu},\Delta M, \ \theta_\ell,t_\ell$	1 to 64	(a8,2I8,5F8.3)	Ply layup and temperature and moisture conditions
5	MATCRD (material system details)	CODES(1,1,J), CODES(1,2,J), VFP,VVP, CODES(2,1,J), CODES(2,2,J), VFS,VVS,VSC	9	Primary composite code names for fiber and matrix, k_f ; Secondary composite code names for fiber and matrix, k_{sc} , k_f , k_g ,	1 to 64	(a8,2a4,2E8.2)	Description of material systems to be used
6	PLOAD (loading details)	NX,NY,NXY,THCS MX,MY,MXY DMX,DMY PRSSU,PRSSL	4 3 4	$N_x, N_y, N_{xy},$ $\theta_{cs}, M_x, M_y,$ M_{xy} $dM_x/d_x,$ $dM_y/d_y,$ P_u, P_ℓ	1 to 32 1 to 32 1 to 40	(a8,7E8.4) (a8,7E8.4) (a8,7E8.4)	Loading conditions (inplane) Angle of inclination to the structural x-axis Loading conditions (bending) Loading conditions (tranverse)

Input data for additional composite systems may be easily prepared. This is done by selecting the desired fiber and matrix from the available materials listed in appendix C using the variable FBMTDATA.BANK and modifying the appropriate entries in the input data sample illustration.

After the input data have been properly assembled (as shown in fig. 3), they are placed in their physical position (fig. 2) and the code is ready to be run.

Detailed Description of Input Data

The card group numbers referred to here are given in figure 3 and table I. The sequential order of the entries in each card group is given in table I. Note that most data cards are identified by a mnemonic to indicate the card group in which it belongs in the input data deck. Also, most data cards are divided into fields of eight, with one entry per field being allowed. The mnemonic is entered in

TABLE II.—ICAN SAMPLE INPUT DATASET

1	FOUR PLY SYMMET	RIC LAMIN	ATE.	ICAN SA	MPLE INPUT	DATA.		
	STDATA	4	1		2			
	T F F F T PLY PLY PLY PLY	1 2 3 4	1 2 2	70.00 70.00 70.00 70.00	70.0 70.0 70.0 70.0	COMSAT CSANB BIDE RINDV NONUDF 0.0 .0 .0	0.0 90.0 90.0	0.010 .005 .005
	MATCRDASIMLS MATCRDSGLAHMHS PLOAD 1000. PLOAD 0.0 PLOAD .0	0.55 .55 0.0 .0	'	0.02 .01 0.0 .0	AS-IMLS AS-IMHS 0.0	0.0	0.57 .57 NX,NY MX,MY	0.03 .01 ,NXY,THCS

format A8, and the integers are entered in format I8. The real numbers may be entered anywhere in the appropriate field. The following is a brief description of each card group together with examples taken from table II:

Title card.

Any title of length up to 80 characters
FOUR PLY SYMMETRIC LAMINATE. ICAN SAMPLE INPUT DATA.

As shown, any title of length up to 80 characters including blanks may be supplied on this card. Starting data card.

1 8	.9 16	,17 24	,25 a ₃₂
Mnemonic	N_i	N_{ic}	N_{ms}
STDATA	4	ı	2

This card has a mnemonic STDATA. It contains the overall laminate and loading details. These details are the number of plies N_{ℓ} , the number of loading conditions $N_{\ell \ell}$, and the number of different material systems N_{ms} .

Booleans.

l	6,7
Boolean T or F	This space may be used for comments
Т	COMSAT
F	RINDV
F	BIDE
F	CSANB
T	NONUDF

A set of booleans, COMSAT, RINDV, BIDE, CSANB, and NONUDF is defined through these cards. These are five cards, one per each logical variable. The format is L6. The variables have the following functions:

(a) COMSAT.—The letter T in the card will direct the program to perform a complete laminate analysis. A letter F would terminate the program at this stage.

- (b) RINDV.—The letter T is entered in the card if the displacements are inputs; otherwise, the letter F is entered.
- (c) BIDE.—The letter T is entered in the card if the interply layer contributions on the composite are desired; otherwise, the letter F is entered.
- (d) CSANB.—The letter T is entered in the card if the composite has both membrane and bending symmetry; otherwise, the letter F is entered.
- (e) NONUDF.—The letter T is entered if the detailed Poisson's ratio difference chart is to be suppressed; otherwise, the letter F is entered.

Ply details card group.

1 8	,9 16	,17 24	,25 32	,33 40	,41 48	.49 56	,57 64
Mnemonic	Pły	Material MID.	T_u	T_{cu}	М	θ_{ℓ}	t_{ℓ}
PLY	1	1	70.00	70.0	.0	0.0	.015
PLY	2	2	70.00	70.0	.0	90.0	.005
PLY	3	2	70.00	70.0	.0	90.0	.005
PLY	4	1	70.00	70.0	.0	0.0	.010

All the cards in this group have the mnemonic PLY. The number of cards is N_{θ} with eight entries on each card. The first entry is PLY. The second and third entries are identification numbers for the ply and the material system, respectively. The fourth and fifth entries are the use temperature T_{u} and the cure temperature T_{cu} , respectively. The sixth entry is the percentage of moisture M. The seventh and the eighth entries are the orientation angle θ of the ply and the thickness of the ply, respectively. A default value of 0.005 is taken for the thickness if this entry is missing. The material system identification number should be different not only for different composite systems but also for varying use temperature or moisture content from ply to ply.

Material system details.

1 8	,9 16	.17 24	,25 32	,33 40	,41 48	,49 56	.57 6
Mnemonic	Fiber, matrix	k_f	k,	Fiber, matrix	V_{sc}	k_f	k,
MATCRD MATCRD	ASIMLS SGLAHMHS	.55 .55	.02 .01	ASIMLS ASIMHS	0.0 0.4	.57 .57	.03 .01

All the cards in this group have the mnemonic MATCRD. The number of cards is N_{ms} with 10 entries in each card. The first entry is MATCRD. The second and the third entries are coded words for fiber and matrix material of the primary composite. The code words are entered in format 2A4. For example, the code for AS-type fiber is AS-- and epoxy matrix is EPOX. A dictionary of codes for several fibers and matrices is provided in appendix C. The user may choose any combination of fiber and matrix for a composite system. The fourth and the fifth entries pertain to the details of the primary composite system. They are the primary fiber volume ratio and the primary void volume ratio, respectively. The next two entries refer to the secondary composite system which is applicable for the case of the hybrid composite ply. They should be the same as the second and third entries for standard composite systems. The next entry is the secondary composite system volume ratio. This is zero for the standard composite systems. The last two entries are the fiber volume ratio and the void volume ratio for the secondary composite system. These values are entered when applicable.

Load cards.

1 8	<u>,9</u> 16,	17 24	,25 32,	33 40
Mnemonic	N_x	N_{xy}	N_{xy}	T_{hes}
PLOAD	1000.	0.0	0.0	0.0
PLOAD	0.0	0.0	0.0	
PLOAD	0.0	0.0	0.0	0.0

All the cards in this group start with the mnemonic PLOAD. There are three cards for each loading condition. Thus, the total number of cards is $3N_{\ell c}$. The first card under each loading condition contains entries N_x , N_y , and N_{xy} for the membrane loads and T_{hcs} for the orientation of the loads with respect to the structural axes. Similarly the second card contains the bending resultants M_x , M_y , and M_{xy} . The last card contains the transverse shear resultants DM_x and DM_y and the transverse pressures P_u and P_ℓ .

The user input data are read from I/O unit 5. Apart from this, ICAN uses two more units, 7 and 8, for its I/O operations. Unit 8 is used to store the material properties data base. Unit 7 is used as a scratch file by ICAN. These I/O units must be appropriately defined by using the operating system JCL.

Output

The following items are printed out by the program:

- (1) ICAN logo
- (2) ICAN coordinate systems
- (3) ICAN input data echo
- (4) Input data summary
- (5) Fiber, matrix, and ply level properties of primary and secondary composites
- (6) Composite three-dimensional strain-stress and stress-strain relations about the structural axes; MAT9 card for MSC/NASTRAN solid elements
 - (7) Composite properties generated in array PC
 - (8) Composite constitutive equations about the structural axes
 - (9) Reduced bending and axial stiffnesses
 - (10) Data for finite-element analysis
 - (11) Displacement-force relations for the current load condition
 - (12) Ply hygrothermomechanical properties/response
 - (13) Details of Poisson's ratio mismatch among the plies
 - (14) Free edge stresses
- (15) Microstresses and microstress influence coefficients for each different composite material
 - (16) Stress concentration factors around a circular hole
 - (17) Locations of probable delamination around circular holes
 - (18) Ply stress and strain influence coefficients
 - (19) Laminate failure load analysis based on the first-ply failure/maximum stress criteria
- (20) Summary of the laminate failure stress analysis based on two alternatives, first-ply failure and fiber breakage

The printout of the input data summary (app. B item 4) shows details regarding composite geometry, constituent specifications, temperature and moisture conditions, and the loading conditions.

The next few pages of the output are generated by the INHYD program package. They show the fiber-matrix properties for the different composite systems and the ply level properties of the composites (app. B, item 5).

The output of the composite three-dimensional strain-stress temperature and moisture relations and composite stress-strain relations about the structural axes are printed under the following headings:

(a) 3-D COMPOSITE STRAIN STRESS TEMPERATURE MOISTURE RELATIONS-STRUCTURAL AXES

The matrices $[E_c]_s^{-1}$, $[\alpha_c]_s$, and $[\beta_c]_s$ in the equation

$$\{\epsilon_c\}_s = [E_c]_s^{-1} \{\sigma_c\}_s - \Delta T_\ell \{\alpha_c\}_s - M_\ell \{\beta_c\}_s$$

where
$$\Delta T_{\ell} = T_{\ell} - T_{cu}$$

are printed by the subroutine GACD3.

(b) 3-D COMPOSITE STRESS STRAIN RELATIONS-STRUCTURAL AXES

The matrix $|E_c|_s$ in the equation

$$|\sigma_c|_S = |E_c|_S |\epsilon_c|_S$$

is printed out by the subroutine GACD3.

The subscripts in the preceding equations indicate that the relations are written about the structural axes. It is noted that these properties are only local to subroutine GACD3. They can be made global if needed. The properties needed to prepare the MAT9 card of MSC/NASTRAN are printed out next under the heading MAT9 CARD FOR MSC/NASTRAN SOLID ELEMENTS (app. B, item 6).

The output of the composite properties, generated in array PC, are printed under the following heading (app. B, item 7):

COMPOSITE PROPERTIES—VALID ONLY FOR CONSTANT TEMPERATURE THROUGH THICKNESS LINES 1 to 31: 3-D COMPOSITE PROPERTIES ABOUT MATERIAL AXES LINES 33 to 62: 2-D COMPOSITE PROPERTIES ABOUT STRUCTURAL AXES Sixty-two entries are printed under this heading as shown in the following list:

Code name	Notation	Explanation
PC(1)	$ ho_{_{ m C}}$	weight density
PC(2)	t_c	thickness
PC(3) to PC(11)	$ E_c $	three-dimensional stress-strain relations about material axes
PC(12) to PC(14)	$ \alpha_c $	three-dimensional coefficients of expansion about material axes
PC(15) to PC(18)	$\{K_c\},H_c$	three-dimensional heat conductivity and heat capacity along material axes
PC(19) to PC(30)	$E_{c11}, G_{c12}, \nu_{c12}$	three-dimensional constants about material axes
PC(31)	z_c	distance to reference plane from bottom of composite
PC(32)		blank
PC(33) to PC(38)	$ E_c ^{-1}$	two-dimensional stress-strain relations about structural axes
PC(39) to PC(47)	$E_{c11}, G_{c12}, \nu_{c12}$	two-dimensional elastic constants along structural axes
PC(48) to PC(54)	α_c , K_c , H_c	two-dimensional coefficients of thermal expansion, heat conductivity, and heat capacity along structural axes
PC(55) to PC(58)	D_{c}	moisture diffusivities
PC(59) to PC(62)	eta_c	moisture expansion coefficients

Array PC and its corresponding string and headings are controlled by the formats in subroutine GPCFD2. For nonuniform temperature/moisture, the bending equivalent and the membrane equivalent elastic constants may be obtained by utilizing the reduced bending rigidity matrix and the reduced stiffness matrix which are also regular output of ICAN.

The output for the composite constitutive equations are printed in the following manner (app. B, item 8):

FORCES FORCE DISPLACEMENT DISPL T-FORCES H-FORCES RELATIONS
$$\begin{cases}
[N_{cx}] \\ [M_{cx}]
\end{cases} =
\begin{bmatrix}
[A_{cx}||C_{cx}|] \\ [C_{cx}||D_{cx}]
\end{bmatrix}
\begin{bmatrix}
[E_{csx}] \\ [W_{cb}]
\end{bmatrix} -
\begin{bmatrix}
[N_{CT_iX}] \\ [M_{CT_iX}]
\end{bmatrix} -
\begin{bmatrix}
[N_{CM_iX}] \\ [M_{CM_iX}]
\end{bmatrix}$$

The elements of matrices A_{cx} , C_{ex} , D_{cx} , $N_{cT_{\ell}x}$, $N_{cM_{\ell}x}$, $M_{cT_{\ell}x}$, and $M_{cM_{\ell}x}$ are printed out by the subroutine GPCFD2.

The output for the reduced bending rigidities is printed under the heading (app. B, item 9): REDUCED BENDING RIGIDITIES. The elements of $[D_{cx}^R]$ are printed out as a matrix.

Similarly, the output for the reduced axial stiffness $[A_{cx}^R]$ is printed out under the heading REDUCED STIFFNESS MATRIX. The corresponding formats for the above two outputs are in subroutine GPCFD2 (app. B, item 10).

The next printout comes from the main program under the heading: SOME USEFUL DATA FOR F.E. ANALYSIS. This information is useful for preparing material data cards for finite element codes NASTRAN and MARC.

The inverse of the constitutive equations is printed out in the following manner (app. B, item 11):

DISP DISPLACEMENT FORCE FORCES RELATIONS
$$\begin{cases}
[\epsilon_{cax}] \\ [w_{cb}]
\end{cases} = \begin{bmatrix}
|A_{cx}||C_{cx}| \\ |C_{cx}||D_{cx}|
\end{bmatrix}^{-1} \begin{cases}
[N_{cx}] + [N_{cT_{i}X}] + [N_{cM_{i}X}] \\ [M_{cx}] - [M_{cT_{i}X}] - [M_{cM_{i}X}]
\end{cases}$$

The elements of this inverse are printed out in the subroutine COMSA.

The current values for the loads and corresponding set of ply properties generated in array PL are printed out next (app. B, item 12). The explanations of the 75 entries in the PL property array are given in the following list:

Code пате	Notation	Explanation	
PL(1,I)	k_v	ply void volume ratio	
PL(2,I)	$k_{f\ell}$	ply apparent fiber volume ratio	
PL(3,I)	k_f	ply actual fiber volume ratio	
PL(4,I)	$k_{m\ell}$	ply apparent matrix volume ratio	
PL(5,I)	k_m	ply actual matrix volume ratio	
PL(6,I)	$ ho_\ell^{\prime\prime\prime}$	ply weight density	
PL(7,I)	t_{ℓ}	ply layer thickness	
PL(8,I)	δ_ℓ	ply and interply layer thickness	
PL(9,I)	\dot{H}_{i}	interply layer distortion energy coefficient	
PL(10,1)	z_e	distance from bottom of composite to ply centroid	
PL(11,I)	z_{cg}	distance from reference plane to ply centroid	
PL(12,I)	θ_{cs}^{rs}	angle from structural axes to composite material axes (same for all plies) (fig. 2)	
PL(13,I)	$ heta_\ell$	angle from ply material axes to composite material axes (fig. 2)	
PL(14,I)	$ heta_{\ell s}$	angle from ply material axes to composite structural axes (fig. 2)	
PL(15,I) to PL(23,I)	$[E_{\ell}]^{-1}$	ply stress-strain relations	
PL(24,I) to PL(26,I)	$\{\alpha_{\ell}\}$	ply thermal coefficients of expansion	
PL(27,I) to PL(29,I)	$\{oldsymbol{K}_\ell\}$	ply heat conductivities	
PL(30,I)	$H_{c\ell}$	ply heat capacity	
PL(34,I) to PL(42,I)	$E_{\ell11}$, $ u_{\ell12}$, $G_{\ell12}$	ply elastic constants	
PL(43,I) to PL(48,I)	D_ℓ and eta_ℓ	moisture diffusivities and expansion coefficients	
PL(49,I)	$ ho_{\mu m del}$	interply delamination factor	
PL(50,1)	T_ℓ	ply temperature	
PL(51,I) to PL(60,I)	$S_{\ell 11T}$, etc.	ply limiting stresses	
PL(61,I)	$K_{\ell'12lphaeta}$	coefficient in combined stress-strength criterion	
PL(62,I)		combined stress-strength criterion	
PL(63,I)		interply delamination criterion	
PL(64,I) to PL(69,I)	$\{\epsilon_\ell\}, \{\sigma_\ell\}$	ply applied strains and stresses	
PL(70,I)	Δho_j	adjacent ply relative rotation	
PL(71,I)	λ.	Hoffman's failure criterion	
PL(72,I)	M_{ℓ}	ply moisture	
PL(73,I)	$\sigma_{\ell 13}$	transverse shear stress	
PL(74,1) PL(75,1)	$\sigma_{\ell 23}$	transverse shear stress thickness stretch stress	
1 11 (12,1)	$\sigma_{l'33}$	emerico offeten offeso	

The next printout shows Poisson's ratio differences between the plies and the composite (app. B, item 13). They are printed out by the subroutine FESTRE under the heading DETAILS OF POISSON'S RATIO MISMATCH.

The stress peaks near the free edge region are printed out next by the subroutine EDGSTR under the heading (app. C, item 14) FREE EDGE STRESSES.

Item 14 of appendix B shows ply stresses in the structural coordinate system and the through-thethickness stresses σ_{zz} , σ_{xz} , and σ_{yz} . The boundary layer decay length is also shown in the table under the heading YDCAY LENGTH. Care must be exercised in interpreting the results. They are based on approximate engineering theories and give good qualitative information regarding the relative magnitudes of the peaks in the individual plies. This printout is suppressed in the case of combined loading.

The microstresses in each ply are printed out next by the subroutine MCRSTR (app. B, item 15(a)). Two regions of interest are considered for the computations, the region between the fibers composed entirely of matrix (A) and the region consisting of fibers as well as matrix (B). The stresses are given a descriptive notation. Thus, SM2AL means stress in matrix along the transverse (2) direction in region A due to a ply stress along the longitudinal direction of the material. Figure 4 shows the definitions for regions A and B. The printout also shows microstresses resulting from moisture and temperature differences if nontrivial M_{ℓ} and T_{ℓ} are present.

The microstress influence coefficients, stresses due to unit applied stresses in direction 11, 22, 12, 13, and 23 (app. B, item 15(b)); unit temperature difference T_{ℓ} ; and unit moisture content M_{ℓ} are output from the subroutine MINCOF. These variables are printed out following the microstresses.

Under the heading STRESS CONCENTRATION FACTORS (app. B, item 16) are printed out the factors K_{1xx} , K_{1yy} , and K_{1xy} which are due to inplane loading around a circular hole at 5° intervals by the subroutine STRCNF. Cumulative stress concentration due to combined loading may be estimated by simple addition of the respective stress concentration factors.

The next output (app. B, item 17) is under the heading POISSON RATIO DIFFERENCES and results from the subroutine NUDIFS. For each ply, the Poisson's ratio differences, $(\nu_l^i - \nu_c^{i-1})$ and $(\nu_l^i - \nu_c)$, and the products K_{1xx} ($\nu_l^i - \nu_c$), K_{1yy} ($\nu_l^i - \nu_c$), and K_{1xy} ($\nu_l^i - \nu_c$) are printed out at θ intervals of 5° around a circular hole. This is suppressed if the boolean NONUDF is set to TRUE. This item shows the locations of probable delamination for each ply. These are the locations where products such as K_{1xx} ($\nu_l^i - \nu_l$), for example, are maximum.

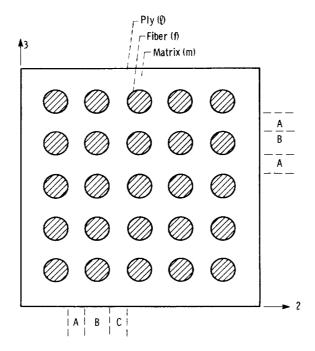


Figure 4.—Definitions of regions for ply microstress calculations.

The next item in appendix B shows the ply stress and strain influence coefficient arrays and ply stress influence coefficient arrays (app. B, item 18). These are computed in the subroutine COMSA and are printed by the main program ICAN. The first table gives the influence coefficients based on unit loads or moments/inch. The second table gives the influence coefficients in terms of unit applied stresses. Explanations of usage of these tables are provided at the end of each table.

The output from the subroutine MSCBFL is printed out next under the heading LAMINATE FAILURE STRESS ANALYSIS (app. B, item 19). The analysis is based on first-ply failure criteria. Results are printed in a tabular form for each ply, and a summary of the analysis is shown in the end (app. B, item 20). The summary shows the critical ply, the failure mode, and the load for each of the applied load types, σ_{cxxT} , σ_{cxxC} , σ_{cyyT} , σ_{cyyC} , and σ_{cxyS} , respectively. The first table shows results based on first-ply failure, and the second table shows results based on fiber failure by breakage.

A Typical IBM Terminal Session

To run ICAN, the user must first install and compile the program on his/her computer according to the system to be used. The procedure used on the Lewis Research Center IBM 370 is described in detail here starting from log on. The computer prompt signals are identified with uppercase letters. User entries are in lowercase letters. The following are prerequisites for the user to be able to run ICAN:

- (1) A knowledge of how to compile and store the object module in the public storage space.
- (2) A knowledge of redit or tedit processors so as to be able to create vs datasets of the input data deck. The details of the input data format have already been described in earlier paragraphs.
- (3) A knowledge of commands like rmds, mds, ddef, libdef, print, and erase. These are a few of the commands commonly used in running a program on the IBM 370.

The user is advised to migrate the object deck, the input dataset, and the material property data base so as to conserve his/her permanent storage. The object deck, which is a binary version of the compiled source program, is referred to here as OBJ.ICAN. The data base of material properties is referred to as FBMTDATA.BANK.

The session is started by logging on at the terminal. This is achieved by typing logon, userid, and password. The system replies

```
TSS/370 RELEASE 3.0 PRPZ3 FTF18

SOME MESSAGE TASKID = OBD7 POOLID = LRCFM -
LOGON AT 11:30 ON 01/15/84
```

The user is now ready for the session. The first phase of the session consists of restoring the necessary data sets to temporary storage. This is achieved by the following commands:

```
rmds obj. ican, aaa
SUCCESSFUL (TEMP) RESTORE OBJ.ICAN AS (AAA)
rmds fbmtdata.bank, ccc
SUCCESSFUL (TEMP) RESTORE FBMTDATA.BANK AS (CCC)
rmds ican.sample.input, bbb
SUCCESSFUL (TEMP) RESTORE ICAN.SAMPLE.INPUT AS (BBB)
```

At this point, the user has all the necessary data sets to run ICAN in his/her temporary storage.

The input/output fortran units that are utilized by ICAN for its various input/output operations need to be defined next. This forms the second phase of the session and is achieved by

```
ddef ft05f001, vs, bbb
ddef ft06f001, vs, icanout.bbb, ret = t
ddef ft08f001, vs, ccc, ret = t
ddef ft07f001, vs, T7, ret = t
```

During these operations, the system usually responds by the minimum prompt, the underscore (_). The third phase consists of loading and executing the object deck and printing out the results. This is done by the following commands:

```
libdef lds, aaa
load gpcom$$$
ican
TERMINATED: STOP
print icanout,bbb, prtsp = edit
PRINT BSN = 8835, 1200 LINES
```

The last phase involves cleaning up the user's storage place and is achieved by issuing the commands

release lds release ft erase aaa erase bbb erase ccc erase t7

The user may either logoff or proceed to execute another run for a different set of input data after the preceding set of commands.

Programmers Manual

A brief description of the main program (or control program) and theoretical equations programmed in the code are presented in this portion of the report. The subroutine descriptions follow the order of execution as shown in the flowchart (fig. 2(b)) rather than the physical sequential order (fig. 2(a)). It is assumed in the following discussion that the user has a working knowledge of computer programming and that he/she is familiar with the terminology appropriate to multilayered composite mechanics.

The assumptions and details leading to the derivation of the equations programmed in the code are not included here. However, they are described in the references cited. It is suggested that the interested user have these references available to him/her.

The information provided in this portion of the code together with the source program listing enables the user to modify, implement, and extend the code according to need.

Main Program

The main program contains the global variables, the various subroutines, the input data and format, the various program control statements, and the output. These are discussed subsequently. The flowchart of the program is shown in figure 5.

The global variables are given in the following list:

```
boolean CSANB, BIDE, RINDV, COMSAT, NONUDF integers N_{\ell}, N_{p\ell}, N_{pc}, N_{f}, N_{\ell c}, M, Q_{i}, Q_{s}, Q_{p}, Q_{p}, Q_{f} real \theta_{cs}, \rho_{f}, \rho_{m}, d_{f}, E, \nu, G, f, m, \pi real arrays K_{\nu\ell}, K_{f\ell}, \theta_{\ell c}, t_{\ell}(1,1000), P_{\ell}(75,1000), P_{c}(1,62) maximum dimensions E_{c\ell}, E_{cm}, A_{cx}, C_{cx}, D_{cx}, D_{cx}^{R}, A_{cx}^{R}(3,3), \alpha_{f}, \alpha_{m}, \alpha_{e}, N_{cT_{\ell}X}, M_{dT_{\ell}X}, N_{cM_{\ell}X}, M_{cM_{\ell}X}, \epsilon_{csz}, \epsilon_{cbx}(1,3), L_{sc}(1,6), M_{cx}, N_{cx}, (3,N_{\ell c}), D_{\nu}(10,6), AINF (6,1000,8), (\lambda_{\nu})_{P,S}, (\lambda_{x})_{P,S}, (\ell_{\nu})_{P,S}, (\ell_{\nu})_
```

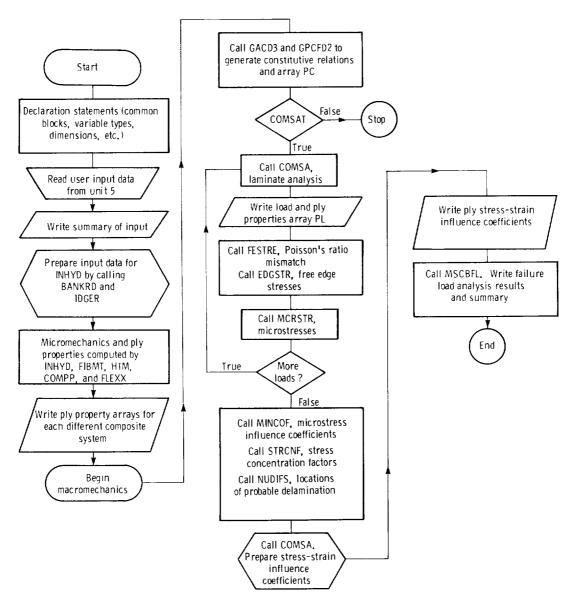


Figure 5.—ICAN program flowchart.

string arrays title (80 characters) read in.

> P_{ℓ} (eight spaces per field, $N_{p\ell}$ fields) C_{e1} (six spaces per field, six fields) C_{e2} (six spaces per field, six fields) P_{cp} (six spaces per field, N_{pc} fields) codes C

 N_{ℓ} , $N_{p\ell}$, N_{pc} , N_f , N_{ms} current dimensions

 $K_{\nu\ell}, K_{f\ell}, \theta_{\ell c}, t_{\ell}(1, N_{\ell}), P_{\ell}(75, N_{\ell})$ real arrays

current dimensions

 $P_c(1, N_{pc}),$ AINF (6, N_ℓ, 8), $\lambda_{y,x,P,S}(1, N_{\ell}),$

 $\ell_{x,y,P,S,}(1,N_{\ell})$

The subroutines are as follows:

INVA inverse of an array

generates composite three-dimensional elastic and thermal properties and GACD3

the two-dimensional thermal properties

BLOCK DATA DISP (String) and RESF (String)

GPCFD2 generates composite two-dimensional elastic constants and constitutive

equations

COMSA generates the ply strain and stress states due to applied loads, checks for

ply failure and interply delamination, and generates the ply stress and

strain influence coefficients

INHYB generates ply level properties with the aid of subroutines FIBMT, HTM,

COMPP, and FLEXX

BANKRD/IDGER generates constituent properties by using the data base

FBMTDATA.BANK and arranges them in a proper format so as to input

to INHYD

FESTRE computes Poisson's ratio mismatch between the plies and the composite

EDGSTR computes interlaminar free edge stresses

MCRSTR/MINCOF generates the microstresses and the corresponding influence coefficients

STRCNF generates the stress concentration factors around a circular hole

NUDIFS generates the Poisson's ratio differences within the plies and the probable

locations of delamination around the free edge of a circular hole

MSCBFL performs failure load analysis based on first ply failure/maximum-stress

criteria and prints the summary

AMINF minimum value of an array AMAXF maximum value of an array

FLRLD determines the failure load, failure mode, and the ply location

These subroutines are described in detail in the next section.

INPUT title, N_{ℓ} , $N_{\ell c}$, N_{ms} , CSANB, BIDE, RINDV,

COMSAT, NONUDF, t_{θ} θ_{θ} T_{θ} M_{θ} fiber name, matrix name, $k_{\nu\theta}$ $k_{f\theta}$ k_{sc} , N_{cx} , M_{cx} ,

 DM_{cx} , P_u , P_ℓ

(For substitution and definition, see appendix A.)

Subroutine Description

Subroutine INVA (N,A,C).—This subroutine computes the inverse of a square matrix A by Gauss elimination and stores it in array C. The check

 $|A| \neq 0$

is made and, if satisfied, the program continues; otherwise, the message SINGULAR MATRIX is displayed. The subroutine inputs are N, the matrix order, and the matrix A. The output is

 $A^{-1} \rightarrow C$

Subroutine GACD3(C).—This subroutine generates the three-dimensional hygrothermoelastic properties of the composite about its structural (x,y,z) and material (1,2,3) axes. The angle θ is measured from x of the structural axes system. (See fig. 6.) In figure 6, replace xy etc. by 11 etc. and

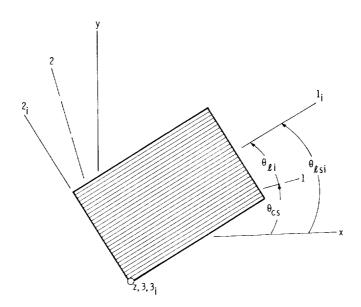


Figure 6.—Ply orientation geometry. Composite structural axes, x,y,z; composite material axes, 1,2,3; ply material axes (coincides with fiber direction), $1_i,2_i,3_i$.

measure θ from the material axes to obtain properties about the material axes. These composite properties are generated from the following equations:

$$\begin{split} [E_c] &= \frac{1}{t_c} \left[\sum_{i=1}^{N_\ell} (z_{\ell i+1} - z_{\ell i}) [R_{\ell i}]^T [E_{\ell i}] [R_{\ell i}] + \sum_{j=1}^{N_{\ell-1}} H_j [S_j] \right] \\ [\alpha_c] &= \frac{1}{t_c} [E_c] \sum_{i=1}^{N_\ell} (z_{\ell i+1} - z_{\ell i}) [R_{\ell i}]^T [E_{\ell i}] [\alpha_{\ell i}] \\ [\beta_c] &= \frac{1}{t_c} [E_c] \sum_{i=1}^{N_\ell} (z_{\ell i+1} - z_{\ell i}) [R_{\ell i}]^T [E_{\ell i}] [\beta_{\ell i}] \end{split}$$

The arrays $\{\alpha_c\}$, $\{\beta_c\}$, $\{\alpha_{\ell\ell}\}$, and $\{\beta_{\ell\ell}\}$ in the preceding equations are given by

$$\{\alpha_c\} = [\alpha_{cxx}\alpha_{cyy}\alpha_{czz}\alpha_{cyz}\alpha_{czx}\alpha_{cxy}]^T$$

$$\{\beta_c\} = [\beta_{cxx}\beta_{cyy}\beta_{czz}\beta_{cyz}\beta_{czx}\beta_{cxy}]^T$$

and

$$\{\alpha_{\ell}\} = [\alpha_{\ell 11}\alpha_{\ell 22}\alpha_{\ell 33} \ 0 \ 0 \ 0]^T$$

$$[\beta_{\ell}] = [\beta_{\ell 11} \beta_{\ell 22} \beta_{\ell 33} \ 0 \ 0 \ 0]^T$$

For all practical purposes, the two-dimensional thermal coefficients of expansion about the composite structural axes are the same as α_{cxx} , α_{cyy} , and α_{cxy} in the array $\{\alpha_c\}$ for the three-dimensional case.

The matrix $[E_c]^{-1}$ is given by

$$[E_c]^{-1} = \begin{bmatrix} \frac{1}{E_{c11}} & -\frac{\nu_{c21}}{E_{c22}} & \frac{\nu_{c31}}{E_{c33}} & 0 & 0 & 0 \\ -\frac{\nu_{c12}}{E_{c11}} & \frac{1}{E_{c22}} & -\frac{\nu_{c32}}{E_{c33}} & 0 & 0 & 0 \\ -\frac{\nu_{c13}}{E_{c11}} & -\frac{\nu_{c23}}{E_{c22}} & -\frac{1}{E_{c33}} & 0 & 0 & 0 \\ 0 & 0 & 0 & \frac{1}{E_{c23}} & 0 & 0 \\ 0 & 0 & 0 & \frac{1}{E_{c31}} & 0 \\ 0 & 0 & 0 & 0 & \frac{1}{E_{c31}} & 0 \end{bmatrix}$$

Note that for the case of an anisotropic material, the elements (1,6), (2,6), (3,6), and (4,5) and their symmetric parts will not be zero.

The matrices $[E_{ii}]^{-1}$ and $[R_{ii}]^{-1}$ are given by

$$[E_{\ell i}]^{-1} = \begin{bmatrix} \frac{1}{E_{\ell 11}} & -\frac{\nu_{\ell 21}}{E_{\ell 22}} & -\frac{\nu_{\ell 31}}{E_{\ell 33}} & 0 & 0 & 0 \\ -\frac{\nu_{\ell 12}}{E_{\ell 11}} & \frac{1}{E_{\ell 22}} & -\frac{\nu_{\ell 32}}{E_{\ell 33}} & 0 & 0 & 0 \\ -\frac{\nu_{\ell 13}}{E_{\ell 11}} & -\frac{\nu_{\ell 23}}{E_{\ell 22}} & \frac{1}{E_{\ell 33}} & 0 & 0 & 0 \\ 0 & 0 & 0 & \frac{1}{E_{\ell 23}} & 0 & 0 \\ 0 & 0 & 0 & \frac{1}{E_{\ell 31}} & 0 \\ 0 & 0 & 0 & 0 & \frac{1}{E_{\ell 31}} & 0 \\ 0 & 0 & 0 & 0 & 0 & \frac{1}{E_{\ell 31}} \end{bmatrix}_{i}$$

$$[R_{ij}] = \begin{bmatrix} \cos^2 \theta & \sin^2 \theta & 0 & 0 & 0 & \frac{1}{2} \sin 2\theta \\ \sin^2 \theta & \cos^2 \theta & 0 & 0 & 0 & -\frac{1}{2} \sin 2\theta \\ 0 & 0 & 1 & 0 & 0 & 0 \\ 0 & 0 & 0 & \cos \theta & \sin \theta & 0 \\ 0 & 0 & 0 & -\sin \theta & \cos \theta & 0 \\ -\sin 2\theta & \sin 2\theta & 0 & 0 & 0 & \cos 2\theta \end{bmatrix}_{i}$$

where $\theta = \theta_{ij}$ for properties about the composite material and $\theta = \theta_{ij} + \theta_{cs}$ for properties about the composite structural axes. (See fig. 6.)

The matrix $[S_{ij}]$ is given by

Here $A = \sin 2\theta_i - \sin 2\theta_{i-1}$ and $B = \cos 2\theta_i - \cos 2\theta_{i-1}$ where i > 1 and denotes the ply index.

The angles θ_i and θ_{i-1} (fig. 6) are given by

$$\theta_i = \theta_{\ell i} + \theta_{cs}$$

$$\theta_{i-1} = \theta_{\ell i-1} + \theta_{cs}$$

The composite heat capacity is the same for both the two- and the three-dimensional cases. It is given by

$$h_c = \frac{1}{t_c} \sum_{i=1}^{N_i} h_{ii} t_{ii}$$

and t_c is given by

$$t_c = \sum_{i=1}^{N_\ell} t_{\ell i}$$

The composite three-dimensional heat conductivities along the composite material axes, assuming an orthotropic composite, are given by

$$K_{c11} = \frac{1}{t_c} \sum_{i=1}^{N_\ell} t_{\ell i} (K_{\ell 11} \cos^2 \theta_{\ell} + K_{\ell 22} \sin^2 \theta_{\ell})_i$$

$$K_{c22} = \frac{1}{t_c} \sum_{i=1}^{N_\ell} t_{\ell i} (K_{\ell 11} \sin^2 \theta_{\ell} + K_{\ell 22} \cos^2 \theta_{\ell})_i$$

$$\frac{1}{K_{c33}} = \frac{1}{t_c} \sum_{i=1}^{N_\ell} \left(\frac{t_{\ell}}{K_{\ell 33}}\right)_i$$

The angle θ_{ℓ} is measured from the material axes (fig. 6)

The composite two-dimensional heat conductivities along the composite structural axes are given by (see ref. 9 for the transformation equations)

$$K_{cxx} = \frac{1}{t_c} \sum_{i=1}^{N_f} t_{ii} (K_{\ell 11} \cos^2 \theta + K_{\ell 22} \sin^2 \theta)_i$$

$$K_{cyy} = \frac{1}{t_c} \sum_{i=1}^{N_f} t_{ii} (K_{\ell 11} \sin^2 \theta + K_{\ell 22} \cos^2 \theta)_i$$

$$K_{cyx} = K_{cxy} = \frac{1}{t_c} \sum_{i=1}^{N_f} t_{ii} (K_{\ell 22} - K_{\ell 11})_i \sin 2\theta_i$$

$$K_{cyz} = K_{c33}$$

The angle θ in the last set of equations is measured from the composite structural axes and is equal to $\theta_{cs} + \theta_{\ell}$. The inputs to the subroutine are N_{ℓ} , $z_{\ell l+1}$, $z_{\ell l}$, θ_{cs} , $\theta_{\ell l}$, $[E_i]$, H_j , $[\alpha_{\ell l}]$, $h_{\ell l}$, and $[K_{\ell l}]$, which are all global. The variable N_{ℓ} is input data. The remaining quantities are either generated or are transferred from information stored in PL(11,1), PL(13,1), PL(15,1-23,1), PL(8,1), PL(24,1) to PL(26,1), PL(30,1), PL(27,1), and PL(29,1). The outputs are t_c and the arrays are $[E_c]^{-1}$, $[\alpha_c]$, $[E_c]$, h_c , and $[E_c]$. The composite thickness t_c is stored in PC(2). The arrays $[E_c]^{-1}$, $[\alpha_c]$, and $[E_c]$ for both composite material and structural axes are printed out under the headings 3-D COMPOSITE STRAIN STRESS TEMPERATURE MOISTURE RELATIONS-STRUCTURAL AXES and 3-D COMPOSITE STRESS STRAIN RELATIONS-STRUCTURAL AXES.

The composite material axes properties $[E_c]$ and $\{\alpha_c\}$ are stored in PC(3) to PC(14) as global variables. The corresponding moduli are stored in PC(19) to PC(30). The three-dimensional heat conductivities and heat capacity along the material axes are stored in PC(15) to PC(18). The two-dimensional thermal coefficients of expansion along the structural axes are stored in PC(48) to PC(50). The two-dimensional heat conductivities and heat capacity along the structural axes are stored in PC(51) to PC(54). Note that the heat capacity is a scalar quantity and is independent of the reference axes. Therefore, PC(54) equals PC(18). The moisture diffusivities and expansion coefficients are stored in entries PC(55) to PC(62).

Subroutine BLOCK DATA.—In this block, the strings C_{e1} and C_{e2} , which are printed out with the composite constitutive equations, are defined. The string C_{e1} contains the resultant force notation N_{cx} , N_{cy} , N_{cxy} , M_{cx} , M_{cy} , and M_{cxy} . The string C_{e2} contains the notation for the corresponding displacements.

Subroutine GPCFD2 (RESF, DISP, PROPC).—This subroutine generates the required section properties and the force-deformation temperature-moisture relations for a two-dimensional

multilayered composite. It also generates the plane-stress elastic constants for the composite. The force-deformation temperature-moisture relations generated in this procedure are defined in the following equation:

The generic equations for the elements in the arrays $[A_{cx}]$, $[C_{cx}]$, $[D_{cx}]$, $[N_{cT_{\ell}x}]$, $[N_{cT_{\ell}x}]$, $[N_{cM_{\ell}x}]$, and $[M_{cM_{\ell}x}]$ are

$$\begin{split} [A_{cx}] &= \sum_{i=1}^{N_{\ell}} (z_{\tilde{u}+1} - z_{\tilde{u}}) [R_{\tilde{u}}]^T [E_{\tilde{u}}]^{-1} [R_{\tilde{u}}] + \sum_{j=1}^{N_{\ell-1}} H_j [S_j] \\ [C_{cx}] &= \frac{1}{2} \sum_{i=1}^{N_{\ell}} (z_{\tilde{u}+1}^2 - z_{\tilde{u}}^2) [R_{\tilde{u}}]^T [E_{\tilde{u}}]^{-1} [R_{\tilde{u}}] + \sum_{j=1}^{N_{\ell-1}} z_{rpj} H_j [S_j] \\ [D_{cx}] &= \frac{1}{3} \sum_{i=1}^{N_{\ell}} (z_{\tilde{u}+1}^3 - z_{\tilde{u}}^3) [R_{\tilde{u}}]^T [E_{\tilde{u}}]^{-1} [R_{\tilde{u}}] + \frac{1}{2} \sum_{j=1}^{N_{\ell-1}} z_{rpj}^2 H_j [S_j] \\ [N_{cT_{\ell}x}] &= \sum_{i=1}^{N_{\ell}} \Delta T_{\tilde{u}} (z_{\tilde{u}+1} - z_{\tilde{u}}) [R_{\tilde{u}}] [E_{\tilde{u}}]^{-1} [\alpha_{\tilde{u}}] \\ [N_{cM_{\ell}x}] &= \sum_{i=1}^{N_{\ell}} M_{\tilde{u}} (z_{\tilde{u}+1} - z_{\tilde{u}}) [R_{\tilde{u}}] [E_{\tilde{u}}]^{-1} [\beta_{\tilde{u}}] \\ [M_{cT_{\ell}x}] &= \frac{1}{2} \sum_{i=1}^{N_{\ell}} \Delta T_{\tilde{u}} (z_{\tilde{u}+1}^2 - z_{\tilde{u}}^2) [R_{\tilde{u}}]^T [E_{\tilde{u}}]^{-1} [\alpha_{\tilde{u}}] \\ [M_{cM_{\ell}x}] &= \frac{1}{2} \sum_{i=1}^{N_{\ell}} M_{\tilde{u}} (z_{\tilde{u}+1}^2 - z_{\tilde{u}}^2) [R_{\tilde{u}}]^T [E_{\tilde{u}}]^{-1} [\beta_{\tilde{u}}] \end{split}$$

where $\Delta T_{\ell i} = T_{\ell i} - T_{cui}$

The arrays $\{\alpha_{\ell i}\}$, $\{\beta_{\ell i}\}$, $[R_{\ell i}]$, $[E_{\ell i}]$, and $[S_j]$ are

$$\{\alpha_{ij}\} = [\alpha_{11} \quad \alpha_{22} \quad 0]_i^T$$

$$\{\beta_{ij}\} = [\beta_{11} \quad \beta_{22} \quad 0]_{i}^{T}$$

$$[R_{\theta}] = \begin{bmatrix} \cos^2 \theta & \sin^2 \theta & \frac{1}{2} \sin 2\theta \\ \\ \sin^2 \theta & \cos^2 \theta & -\frac{1}{2} \sin 2\theta \\ \\ -\sin 2\theta & \sin 2\theta & \cos 2\theta \end{bmatrix}_{i}$$

$$[E_{ij}] = \begin{bmatrix} \frac{1}{E_{\ell 11}} & -\frac{\nu_{\ell 21}}{E_{\ell 22}} & 0\\ -\frac{\nu_{\ell 12}}{E_{\ell 11}} & \frac{1}{E_{\ell 22}} & 0\\ 0 & 0 & \frac{1}{G_{\ell 12}} \end{bmatrix}_i$$

$$S_{j22} = S_{j11} = \frac{1}{4} (\sin 2\theta_i - \sin 2\theta_{i-1})^2$$

$$S_{j21} = S_{j12} = -S_{j11}$$

$$S_{j32} = S_{j23} = \frac{1}{4} (\sin 2\theta_i - \sin 2\theta_{i-1}) (\cos 2\theta_i - \cos 2\theta_{i-1})$$

$$S_{i31} = S_{i13} = -S_{i23}$$

$$S_{j33} = \frac{1}{4} (\cos 2\theta_i - \cos 2\theta_{i-1})^2$$

Here θ_i equals the $\theta_{cs} + \theta_l$ (fig. 6). The reduced bending rigidities (ref. 6) are generated in this procedure according to the equation

$$D_{cx}^{R} = [D_{cx} - C_{cx}A_{cx}^{-1}C_{cx}]$$

The reduced axial stiffnesses are generated in the procedure according to the equation

$$A_{cx}^{R} = [A_{cx} - C_{cx}D_{cx}^{-1}C_{cx}]$$

The two-dimensional composite elastic constants are generated from the following equation (assuming $T_{ii} = T_{\ell}$ for i = 1 to N_{ℓ} and $M_{ii} = M_{\ell}$ for i = 1 to N_{ℓ}):

$$[E_{CX}]^{-1} = \frac{1}{t_c} \left\langle \sum_{i=1}^{N_\ell} (z_{\ell i+1} - z_{\ell i}) [R_{\ell i}]^T [E_{\ell i}]^{-1} [R_{\ell i}] + \sum_{j=1}^{N_\ell} H_j[S_j] \right\rangle$$

where

$$t_c = \sum_{i=1}^{N_\ell} t_{\ell i}$$

The inputs to this subroutine are $t_{\ell i}$, $T_{\ell i}$, $M_{\ell i}$, θ_i (relative to composite structural axes), H_j , and the ply elastic constants. These quantities are global and are located, respectively, in PL(7,1), PL(50,1), PL(72,1), PL(14,1), PL(9,1), and PL(31,1) to PL(42,1). The arrays $[R_{\ell i}]^T$, $[E_{\ell i}]^{-1}$, $[R_{\ell i}]$, and $[S_j]$ and the dimensions $z_{\ell i}$ are generated within this subroutine.

The outputs are the force-deformation temperature-moisture relations, which are stored in the global arrays $ACX = A_{cx}$, $RAC = A_{cx}^R$, $CPC = C_{cx}$, $FLX = D_{cx}$, $RDC = D_{cx}^R$, $NSDT = N_{cT_{cx}}$, $MSDT = M_{cT_{cx}}$, $NSDH = N_{cM_{cx}}$, and $MSDH = M_{cM_{cx}}$. These are printed out under the heading

FORCES FORCE DISPLACEMENT RELATIONS DISPL T-FORCES H-FORCES. The reduced bending rigidities are printed out under the heading REDUCED BENDING RIGIDITIES. The reduced axial stiffnesses are printed out under the heading REDUCED STIFFNESS MATRIX. The inverse of the constitutive equations

$$\begin{bmatrix} A_{cx} & [C_{cx}] \\ [C_{cx}] & [D_{cx}] \end{bmatrix}^{-1}$$

are printed out under the heading DISP DISPLACEMENT FORCE RELATIONS FORCES. The distances z_c , z_{\emptyset} , and z_{\emptyset} are stored in PC(31,1), PL(10,1), and PL(11,1), respectively. The two-dimensional composite stress-strain relations are stored in PC(33) to PC(38), and the two-dimensional composite moduli and Poisson's ratios are stored in PC(39) to PC(47). The two-dimensional thermal properties are stored in PC(48) to PC(54), as is described in the section subroutine GACD3.

Subroutine COMSA (M).—In this subroutine the stress and strain states of each ply are computed given the edge membrane forces, the ply temperature, and the changes in curvature. In addition, two-ply, combined stress-strength criteria and the interply delamination criterion are generated. Also generated are the ply stress-strain influence coefficients. The equations programmed for the *i*th strain and stress states are

$$\begin{split} \{\epsilon_{\emptyset}\} &= [R_{\emptyset}][A_{cx}]^{-1} \Big\langle \{N_{cx}\} + \{N_{cT_{\ell}x}\} + \{N_{cM_{\ell}x}\} + [C_{cx}]\{w_{cbx}\} \Big\rangle - z[R_{\emptyset}]\{w_{cbx}\} \\ \{\sigma_{\emptyset}\} &= [E_{\emptyset}]^{-1} [R_{\emptyset}][A_{cx}]^{-1} \Big\langle \{N_{cx}\} + \{N_{cT_{\ell}x}\} + \{N_{cM_{\ell}x}\} + [C_{cx}]\{w_{cbx}\} \Big\rangle \\ &\qquad \qquad - [E_{\emptyset}]^{-1} \Big\langle T_{\emptyset}[\alpha_{\emptyset}] + M_{\emptyset}[\beta_{\emptyset}] + z[R_{\emptyset}]\{w_{cbx}\} \Big\rangle \end{split}$$

The reference plane strains ϵ_{csx} and the curvature changes are computed from

$$\begin{cases} \{\epsilon_{csx}\} \\ \{w_{cbx}\} \end{cases} = \begin{bmatrix} [A_{cx}] & [C_{cx}]^{-1} \\ [C_{cx}] & [D_{cx}] \end{bmatrix}$$

$$\begin{cases} \{N_{cx}\} \\ \{M_{cx}\} \end{pmatrix} + \begin{cases} \{N_{cT_{\ell}x}\} \\ \{M_{cT_{\ell}x}\} \end{pmatrix} + \begin{cases} \{N_{cM_{\ell}x}\} \\ \{M_{cM_{\ell}x}\} \end{pmatrix}$$

when either the membrane force or the moments or both are given.

The strains are generated locally in EPSL and SIGL, respectively, and are stored in PL(64,1) to PL(69,1). The matrices $[R_{ij}]$ and $[E_{ij}]$ are generated locally from information transferred from PL(14,1) and PL(31,1) to PL(42,1). The distance z_{ij} , the ply temperature T_{ij} , and the ply moisture M_{ij} are transferred from PL(11,1), PL(50,1), and PL(72,1), respectively. The remaining matrices are

$$\begin{array}{lll} A_{cx} & \rightarrow & \mathrm{ACX} \\ C_{cx} & \rightarrow & \mathrm{CPC} \\ N_{cT_{l}X} & \rightarrow & \mathrm{NSDT} \\ N_{cM_{l}X} & \rightarrow & \mathrm{NSDH} \\ N_{cx} & \rightarrow & \mathrm{NSB}_{m} \\ M_{cT_{l}X} & \rightarrow & \mathrm{MSDT} \\ M_{cm_{l}X} & \rightarrow & \mathrm{MSDH} \\ M_{cx} & \rightarrow & \mathrm{MSB}_{m} \end{array}$$

and $w_{cbx} \rightarrow WXX_m$ (local curvature from bending analysis), where m denotes the load condition.

It is important to note that the stress analysis in the coded form also handles the case where both the reference plane membrane strains and the local curvatures are given. In this case the ply strains are given by

$$\{\epsilon_{CXi}\} = \{\epsilon_{CXX}\} - z[w_{ChY}]$$

where $\{\epsilon_{cxi}\}\$ is the *i*th ply strain along the structural axis, $\{\epsilon_{cxx}\}\$ is the reference plane membrane strain, z is the distance from the reference plane to the centroid of the *i*th ply, and $\{w_{cbx}\}\$ is the local curvature. These variables are read in the array D_{vm} , where m denotes the load condition.

The corresponding *i*th ply stresses are given by

$$\{\sigma_i\} = [E_{ij}]^{-1} \left\langle [R_{ij}] | \epsilon_{cxi} - \Delta T_{ij} | \alpha_{ij} \rangle - M_{ij} | \beta_{ij} \rangle \right\rangle$$

$$\Delta T_{ij} = T_{ij} - T_{cui}$$

where $[\sigma_{ii}]$ is the *i*th ply stress along the material axes, $[E_{ii}]$ is the *i*th ply elastic constant about the material axes, $[R_{ii}]$ is the transformation matrix of the *i*th ply, $\{\epsilon_{cxi}\}$ is the *i*th ply strain along the structural axes as given by a previous equation, T_{ii} is the temperature of the *i*th ply, T_{cui} is the cure temperature of the *i*th ply, $\{\alpha_{ii}\}$ is the thermal coefficient of expansion of the *i*th ply along the material axes, M_{ii} is the moisture content of the *i*th ply, and $\{\beta_{ii}\}$ is the moisture expansion coefficient of the *i*th ply along the material axes.

The displacement force relations are printed out in the following format:

DISPLACEMENT DISPLACEMENT FORCE RELATIONS FORCES

$$\begin{cases}
\{U_{cx}\} \\
\{W_{cx}\}
\end{cases} = \begin{bmatrix}
[A_{cx}] & [C_{cx}] \\
[C_{cx}] & [D_{cx}]
\end{bmatrix}^{-1} \qquad \begin{cases}
[N_{cx}] \\
[M_{cx}]
\end{cases}$$

Two similar sets are printed out. In the first set, the displacement and force vectors are in symbolic form. In the second set, the displacement and force vectors have their numerical values. (See outputs of trial cases, app. B.)

The failure criterion may be determined by either of the following methods:

(1) Modified distortion energy

$$F = 1 - \left[\left(\frac{\sigma_{\ell 11\alpha}}{S_{\ell 11\alpha}} \right)^2 + \left(\frac{\sigma_{\ell 22\beta}}{S_{\ell 11\beta}} \right)^2 - K_{\ell 12\beta} \frac{\sigma_{\ell 11\alpha}}{S_{\ell 11\alpha}} \frac{\sigma_{\ell 22}}{S_{\ell 22}} + \left(\frac{\sigma_{\ell 12S}}{S_{\ell 12S}} \right)^2 \right]_i \to PL(62, I)$$

The parameters α and β are specified as follows:

$$\alpha = \begin{cases} T & \sigma_{\ell 1 1} \ge 0 \\ C & \sigma_{\ell 1 1} < 0 \end{cases}$$

$$\beta = \begin{cases} T & \sigma_{\ell 2 2} \ge 0 \\ C & \sigma_{\ell 2 3} < 0 \end{cases}$$

$$S_{\ell 11\alpha} = \begin{cases} S_{\ell 11T} & \alpha = T \\ \min(S_{\ell 11C}, S_{\ell 11CD}) & \alpha = C \end{cases}$$

$$S_{\ell 22\alpha} = \begin{cases} S_{\ell 22T} & \beta = T \\ S_{\ell 22C} & \beta = C \end{cases}$$

$$K_{\ell 12\alpha\beta} = K_{\ell 12\alpha\beta}' \frac{(1 + 4\nu_{\ell 12} - \nu_{\ell 13}) E_{\ell 22} + (1 - \nu_{\ell 23}) E_{\ell 11}}{\left[E_{\ell 11} E_{\ell 22} (2 + \nu_{\ell 12} + \nu_{\ell 13}) (2 + \nu_{\ell 21} + \nu_{\ell 23}) \right]^{1/2}}$$

$$K'_{\ell 12\alpha\beta} = \begin{cases} \text{BET}(1, 7) & \alpha, \beta = T \\ \text{BET}(2, 7) & \alpha = C, \beta = T \\ \text{BET}(1, 8) & \alpha = T, \beta = C \\ \text{BET}(2, 8) & \alpha, \beta = C \end{cases}$$

The multiplier of $K'_{\ell 12\alpha\beta}$ was generated in the main program and is stored in PL(61,1). The constant $K'_{12\alpha\beta}$ constitute theory-experiment correlation factors. These are set as unity in COMSA. However, the user can modify the correlation factors if he/she wishes, by redefining the matrix BET in the subroutine COMSA.

(2) Hoffman's criterion (ref. 9)

 $S_{\ell 11C} = \min(S_{\ell 11C}, S_{\ell 11CD})$

$$F = 1 - \left[\frac{\sigma_{\ell 11}^2 - \sigma_{\ell 11}\sigma_{P22}}{S_{\ell 11c}S_{\ell 11T}} + \frac{\sigma_{\ell 22}^2}{S_{\ell 22C}S_{\ell 22T}} + \frac{S_{\ell 11C} - S_{\ell 11T}}{S_{\ell 11C}S_{\ell 11T}}\sigma_{\ell 11} + \frac{S_{\ell 22C} - S_{\ell 22T}}{S_{\ell 22C}S_{\ell 22T}}\sigma_{\ell 22} + \frac{\sigma_{\ell 12}^2}{S_{\ell 12S}^2} \right]_i - PL(71,1)$$

F>0 no failure

F = 0 incipient failure

F<0 failure

The interply delamination criterion for the jth interply layer at the mth load condition is governed by

$$\left[1 - \left(\frac{|\Delta\varphi|}{\Delta\varphi_{\text{del}}}\right)\right]_{j} \rightarrow \text{PL}(63,I) \quad \text{when } i > 1$$

$$\Delta\varphi_{j} = \frac{1}{2} \left(\epsilon_{cyy} - \epsilon_{cxx}\right) \left(\sin 2\theta_{i} - \sin 2\theta_{i-1}\right) + \frac{1}{2} \epsilon_{cxy} \left(\cos 2\theta_{i} - \cos 2\theta_{i-1}\right) \left(\epsilon_{cx}\right) = \left[A_{cx}\right]^{-1} \left(\left[N_{cx}\right] + \left[N_{cT_{i}x}\right] + \left[N_{cM_{i}x}\right] + \left[C_{cx}\right] \left[w_{cbx}\right]\right)$$

or by the displacement force equation described previously.

The inputs to the subroutine are the ply angle measured from the structural axes (θ_i , from PL(14,1)); the distance from the reference plane to the centroid of the ply (z_{ij} , from PL(11,1)); the ply temperature (T_{ij} , from PL(50,1)); the interply delamination limit ($\Delta\varphi_{\text{del}j}$, from PL(60,1)); the ply thermoelastic properties stored in PL(24 to 26,I) and PL(31 to 42,I); the ply extensional and coupling rigidities, $A_{cx} = ACX$ and $C_{cx} = CPC$; the local curvatures $w_{cbx} = WXX$; the adjustment constants $K'_{\ell 12TT} = BET(1, 7)$, $K'_{\ell 12CT} = BET(2, 7)$, $K'_{\ell 12TC} = BET(1, 8)$, and $K'_{\ell 12CC} = BET(2, 8)$; and the load conditions $N_{cx} = NBS(m)$.

The subroutine outputs are the modified distortion energy PL(62,I), Hoffman's criterion PL(71,I), the interply delamination criterion PL(63,I), and the adjacent ply relative rotation ($\Delta \varphi j$, from PL(70,I)).

Subroutine EDGSTR.—This subroutine computes the interlaminar stresses σ_{zz} , σ_{zy} , and σ_{zx} near a straight free edge region of a finite width, infinitely long plate under uniform extension. The equations used are based on an approximate formulation analogous to that in reference 18. The calculations are performed in two parts. The first part consists of computations of decay lengths for

the interlaminar stresses. The decay length is a measure of a free edge region in which the interlaminar stresses may be significant. This is achieved in the main program. The second part uses this information to compute the interlaminar stresses in the subroutine EDGSTR. The pertinent equations are discussed in the following paragraphs. Note that in the case of hybrid composite plies, the calculations are repeated not only for the primary composite but also for the secondary composite by using the appropriate ply constituent properties. The primary and the secondary composites are distinguished by using the letters P and S, respectively, in the Fortran variables. In the case of biaxial loading, this subroutine is bypassed as there are no free edges.

Part 1.—Decay length or boundary layer width computations. The interlaminar stresses near the free edge are assumed to decay exponentially. The decay length is calculated with the aid of the following equations:

$$\{\ell_b\} = \frac{-\alpha_{t\ell}}{\lambda} \left(\frac{t_\ell}{t_c}\right)$$

where

$$\alpha = \ell_n^{-1} (0.001)$$

and

$$\{\lambda\} = \left\{ \frac{G_m}{E_{\ell \nu \nu}} \left[\sqrt{\frac{\pi}{4(1 - \mathbf{k}_{\nu})k_f}} - 1 \right] \right\}^{1/2}$$

The calculations are repeated for each layer. Quantities ℓ_b and λ_i are stored in arrays YPL and PLMDAY. These quantities pertain to the free edge parallel to the load axis X. The corresponding quantities for the load axis parallel to Y are stored in arrays XPL and PLMDAX. These are computed by replacing $E_{\ell yy}$ with $E_{\ell xx}$ in the preceding equations. For the intraply hybrid composite, the respective arrays for the secondary composite are denoted by YSL, SLMDAY, XSL, and SLMDAX. Note that the letter P is replaced by S. This notation is followed consistently throughout the text. The labeled common block ILAB6 is used to store and pass these data to subroutine EDGSTR.

Part 2.—Interlaminar stress computations. In the EDGSTR subroutine, the ply stresses PL(67,1) to PL(69,1) are transformed to the structural coordinate system x, y, and z. These stresses are stored in the matrix SIGMA (3,1) for each layer. The interlaminar stresses $\{\sigma_{zz}\}$ are computed with the aid of the following relations:

$$\sigma_{\ell zz}^{i} = \alpha^{2} \left(\frac{t_{\ell}^{i}}{\ell_{0}^{i}} \right)^{2} \left[\frac{\sigma_{\ell yy}^{i}}{2} + \frac{1}{t_{\ell}^{i}} \sum_{j=N_{\ell}}^{j+1} \sigma_{\ell yy}^{j} t_{\ell}^{j} \right]$$

for
$$i = N_{\ell-1}$$
 to $N_{\ell}/2 + 1$

$$\sigma_{\ell zz}^{N_{\ell}} = \alpha^2 \left(\frac{t_{\ell}^{N_{\ell}}}{L_{b}^{N_{\ell}}} \right)^2 \frac{\sigma_{\ell yy}^{N_{\ell}}}{2}$$

The interlaminar shear stresses $\{\sigma_{\ell zy}\}$ and $\{\sigma_{\ell zx}\}$ are calculated by

$$\sigma_{\mathcal{Z}y}^{i} = \frac{\alpha}{(e^{\alpha} - 1)} \frac{\sum_{j=N_{\ell}}^{j+1} \sigma_{\mathcal{L}y}^{j} t_{\ell}^{j}}{\ell_{b}^{j}} \qquad for \ i = N_{\ell} \text{to } \frac{N_{\ell}}{2} + 1$$

and

$$\sigma_{\ell x x}^{i} = \frac{3 \sum_{j=N_{\ell}}^{j+1} \sigma_{\ell n y}^{j}}{\ell h} \qquad \text{for } i = N_{\ell} \text{to } \frac{N_{\ell}}{2} + 1$$

In these equations, the computations are started from the top layer $(i = N_{\ell})$. After the midplane is approached $(i = N_{\ell}/2 + 1)$, the calculations are repeated starting from the bottom layer (i = 1) and continued until i becomes $(N_{\ell}/-1)$.

The interlaminar stresses are stored in the arrays YSZZP, SZYP, and SZXP for the primary composite and in the arrays YSZZS, SZYS, and SZXS for the secondary composite. They are, however, made dimensionless by dividing by the applied normal stress $\sigma_{\ell xx}$.

Subroutine STRCNF.—This subroutine calculates the stress concentration factors around a circular hole due to membrane loading. The equations used are taken from reference 19 and are strictly applicable for infinite plates. Three factors are computed in the subroutine and are defined by the following equations:

$$K_{1xx} = \frac{\sigma_{\theta\theta}}{\sigma_{xx\infty}}$$

$$K_{1yy} = \frac{\sigma_{\theta\theta}}{\sigma_{yy\infty}}$$

$$K_{1xy} = \frac{\sigma_{\theta\theta}}{\sigma_{x:\infty}}$$

Quantities $\sigma_{\chi\chi\infty}$, $\sigma_{yy\infty}$, and $\sigma_{\chi y\infty}$ are the applied stresses, and $\sigma_{\theta\theta}$ is the hoop stress at any angle θ from the load axis. The stress concentration factors are stored in the local arrays XK1, XK3, and TEMP. The expressions for $K_{1\chi\chi}$, $K_{1\chi y}$, and $K_{1\chi y}$ are the following:

$$K_{1xx} = \frac{E_{ctt}}{E_{cxx}} \left\{ -\sqrt{\frac{E_{cxy}}{E_{cyy}}} \cos^2 \theta + \left[1 + \sqrt{2\left(\frac{E_{cxx}}{E_{cyy}} - \nu_{cxy}\right)} + \frac{E_{cxx}}{G_{cxy}} \right] \sin^2 \theta \right\}$$

$$K_{1yy} = \frac{E_{crr}}{E_{cxx}} \left\{ -\sqrt{\frac{E_{cyy}}{E_{cxx}}} \cos^2 \theta + \left[1 + \sqrt{2\left(\frac{E_{cyy}}{E_{cxx}} - \nu_{cxy}\right)} + \frac{E_{cyy}}{G_{cxy}} \right] \sin^2 \theta \right\}$$

$$K_{1xy} = \frac{E_{ctt}}{E_{cxx}} \left\{ 1 + \sqrt{\frac{E_{cxx}}{E_{cyy}}} + \left[\sqrt{2\left(\frac{E_{cxx}}{E_{cyy}} - \nu_{cxy}\right) + \frac{E_{cxx}}{G_{cxy}}} \right] - \left[\sqrt{2\left(\frac{E_{cxx}}{E_{cyy}} - \nu_{cxy}\right) + \frac{E_{cxx}}{G_{cxy}}} \sin 2\theta \right] \right\}$$

In the preceding expressions, E_{ctt} and E_{crr} are the composite moduli in the tangential and radial directions at angle θ . Angle θ is measured from the x-axis for K_{1xx} and K_{1xy} and from the y-axis for K_{1yy} . The program rearranges the computed K_{1yy} values so that they correspond to the same location as those of K_{1xx} and K_{1xy} .

Subroutine NUDIFS.—In this subroutine, the Poisson's ratio differences between the adjacent plies and the composite are computed around a circular hole at 5° intervals. The products of the differences and the corresponding stress concentration factors are computed next. These products are expected to provide insight into the probable delamination locations. It is assumed that onset of

delamination is likely to occur at the locations for which the product of Poisson's ratio mismatch with the corresponding stress concentration factor is a maximum. Accordingly, these products are computed at 5° intervals and the maxima are calculated. Two sets of tables are the output from this subroutine. The first table comes out optionally if the boolean NONUDF is set to FALSE. It contains all the details of the computations. The second table consists of the summary of results, with notes on the maxima and the locations. The following are the programmed equations:

At any angle θ the Poisson's ratio is computed by

$$v_{crt} = E_{crr} \left[\frac{v_{cxy}}{E_{cxy}} - \left(\frac{1 + 2v_{cxy}}{E_{cxy}} + \frac{1}{E_{cyy}} - \frac{1}{G_{cxy}} \right) \cos^2 \theta \sin^2 \theta \right]$$

The ply Poisson's ratio is given by

$$\{\nu_{\ell r t}\} = E_{\ell r r} \left[\frac{\nu_{\ell 12}}{E_{\ell 11}} - \left(\frac{1 + 2\nu_{\ell 12}}{E_{\ell 11}} + \frac{1}{E_{\ell 22}} - \frac{1}{G_{\ell 12}} \right) \cos^2 \theta \sin^2 \theta \right]$$

The difference in Poisson's ratio between the *i*th and (i+1)th plies is given by $(\nu_{trt}^{i+1} - \nu_{trt}^{i})$, and the difference with respect to the composite is given by $(\nu_{trt}^{i} - \nu_{crt})$. These are stored in the arrays A2 and A3, respectively. The products of K_{1xx} , K_{1yy} , and K_{1xy} with A3 are computed next and are stored in the arrays A5, A6, and A7, respectively. The maxima and their location in each of the four quadrants (0-90, 90-180, 180-270, and 270-0) are computed by calling the subroutine AMAXF for the three arrays A5, A6, and A7. The values of stress concentration factors are passed through the labeled common block ILAB8 from the subroutine STRCNF.

Subroutine MSCBFL (AINF).—A complete laminate failure stress analysis, based on first-ply failure and the maximum strength criteria, is performed in this subroutine. The inputs to this routine are the ply allowables $S_{\ell 11C}$, $S_{\ell 11T}$, $S_{\ell 22C}$, $S_{\ell 22T}$, and $S_{\ell 12S}$ and the ply influence coefficient matrix AINF. The ply stress allowables are generated by the INHYD routines and are stored in the ply properties array PL. These are accessed through the labeled common block ILAB2. The ply stress influence coefficients are generated by COMSA and the main program and are passed to the present routine by the subroutine argument.

The failure stress for a particular ply due to a specific loading is given by the ratio of the allowable strength to the ply stress influence coefficient. For example, the failure stress due to a tensile load is given by

$$S_c^i = \frac{S_{\ell 11T}^i}{\text{Fact } 1^i}$$

where Fact1ⁱ is the stress influence coefficient for ith ply due to unit tensile loading, $S_{\Pi 1T}^i$ is the strength allowable for ith ply in longitudinal tension, and S_c^i is the failure stress for the ith ply due to a tensile loading. The failure stresses are stored in the matrix FAILD. In the case of temperature/moisture presence, the allowable strengths are updated to take into account temperature or moisture stresses; the failure stresses are computed with and without the effects of temperature-and moisture-induced stresses for comparison. The program considers primarily five different loadings, longitudinal compression and tension, transverse compression, and tension and inplane shear.

After the failure load computations for each ply are determined, the active failure mode and the corresponding failure strength for each type of loading are determined by calling the subroutine AMINF. This subroutine returns the value of the minimum failure load, the ply number, and the failure mode as output. The output from this subroutine is printed under the heading LAMINATE FAILURE STRESS ANALYSIS.

Subroutine MCRSTR.—This subroutine generates the microstresses in the ply constituents due to the inplane loading. These are stored in the ply microproperty arrays PLMP and PLMS for the

primary and the secondary composites. The ply constituent properties and the applied loads are inputs to this subroutine. They are accessed with the aid of the common blocks PBANK, MFBANK, ILAB2, ILAB5, and ILAB9. The PLMP and PLMS each contain 41 entries which are explained in the following list:

Code name	Algebraic notation	Fortran variable
<i>PLM(1,I)</i>	σ_{m11L}	SM1L
PLM(2,I)	σ_{m11T}	SMIT
PLM(3,I)	σ_{f11L}	SF1L
PLM(4,I)	σ_{f11T}	SF1T
PLM(5,I)	$\sigma_{m22L}^{(\mathrm{A})}$	SM2AL
PLM(6,I)	$\sigma^{(\mathrm{A})}_{m22T}$	SM2AT
PLM(7,I)	$\sigma_{m22L}^{ m (B)}$	SM2BL
PLM(8,I)	$\sigma^{\mathrm{(B)}}_{m22T}$	SM2BT
PLM(9, i)	$\sigma_{f22L}^{(B)}$	SF2BL
PLM(10,I)	$\sigma_{f22T}^{ ext{(B)}}$	SF2BT
PLM(11,I)	$\sigma_{m33L}^{(A)}$	SM3AL
PLM(12,I)	$\sigma_{m33T}^{(A)}$	SM3AT
PLM(13,I)	$\sigma_{m33L}^{(\mathrm{B})}$	SM3BL
PLM(14,I)	$\sigma_{m33T}^{\mathrm{(B)}}$	SM3BT
PLM(15,I)	$\sigma_{f33L}^{ m (B)}$	SF3BL
PLM(16,I)	$\sigma_{f33T}^{ m (B)}$	SF3BT
PLM(17,I)	$\sigma_{m12}^{(\mathrm{A})}$	SM12A
PLM(18,I)	$\sigma_{m12}^{(\mathrm{B})}$	SM12B
PLM(19,I)	$\sigma_{f12}^{ m (B)}$	SF12B
PLM(20,I)	$\sigma_{m13}^{(A)}$	SM13A
PLM(21,I)	$\sigma_{m13}^{(\mathrm{B})}$	SM13B
PLM(22,I)	$\sigma_{f13}^{(\mathrm{B})}$	SF13B
PLM(23,I)	$\sigma_{m23}^{(\mathrm{A})}$	SM23A
PLM(24,I)	$\sigma_{m23}^{(\mathrm{B})}$	SM23B

PLM(25,I)	$\sigma_{f23}^{(\mathrm{B})}$		SF23B
PLM(26,I)	σ_{m11}		SMIIDT
PLM(27,I)	σ_{f11}		SF11DT
PLM(28,I)	$\sigma_{m22}^{(\mathrm{A})}$	Microstresses due to temperature gradient $\Delta T \ell$	SM2ADT
PLM(29,I)	$\sigma_{m22}^{(\mathrm{B})}$		SM2BDT
PLM(30,I)	$\sigma_{f22}^{(\mathrm{B})}$		SF2BDT
PLM(31,1)	$\sigma^{({ m A})}_{m33}$		SM3ADT
PLM(32,1)	$\sigma^{(\mathrm{B})}_{m33}$		SM3BDT
PLM(33,1)	$\sigma_{f33}^{(\mathrm{B})}$		SF3BDT
PLM(34,I)	σ_{m11}		SM11DM
PLM(35,1)	σ_{f11}		SF11DM
PLM(36,1)	$\sigma_{m22}^{(\mathrm{A})}$	Microstresses due to moisture \mathbf{M}_ℓ	SM2ADM
PLM(37,I)	$\sigma^{ m (B)}_{m22}$		SM2BDM
PLM(38,I)	$\sigma_{f22}^{(\mathrm{B})}$		SF2BDM
PLM(39,I)	$\sigma_{m33}^{(\mathrm{A})}$		SM3ADM
PLM(40,1)	$\sigma_{m33}^{(\mathrm{B})}$		SM3BDM
PLM(41,1)	$\sigma_{f33}^{(\mathrm{B})}$		SF3BDM

In this list, entries 26 to 41 are suppressed automatically if the temperature gradients and moisture contents are not present. The superscripts A and B refer to two regions as described in figure 4.

The microstresses are calculated with the aid of the following equations: (For notation and sign conventions, see figs. 4 and 6.)

Ply microstresses due to a longitudinal stress $\sigma_{\ell 11}$ are given by

$$\sigma_{m11} = (E_m/E_{\ell 11})\sigma_{\ell 11}$$

$$\sigma_{f11} = (E_{f11}/E_{\ell11})\sigma_{\ell11}$$

$$\sigma_{m22}^{(A)} = (\nu_m - \nu_{\ell 12})(E_m/E_{11})\sigma_{\ell 11}$$

$$\sigma_{m22}^{(\mathrm{B})} = \sigma_{f22}^{(\mathrm{B})} = - \frac{1 - \sqrt{k_{\mathrm{f}}}}{\sqrt{k_{\mathrm{f}}}} \, \sigma_{\mathrm{fl} \, 1}$$

$$\sigma_{m33}^{(A)} = \sigma_{m22}^{(A)}$$

$$\sigma_{m33}^{(B)} = \sigma_{m22}^{(B)}$$

$$\sigma_{f33}^{(B)} = \sigma_{f22}^{(B)}$$

Ply microstresses due to a transverse stress $\sigma_{\ell 22}$ are given by

$$\sigma_{m11} = \left(\nu_m - \frac{\nu_{\ell 12} E_m}{E_{\ell 11}}\right) \sigma_{\ell 22}$$

$$\sigma_{f11} = \left(\nu_{f12} - \nu_{\ell12} \frac{E_{f11}}{E_{\ell11}}\right) \sigma_{\ell22}$$

$$\sigma_{m22}^{(A)} = (E_m/E_2)\sigma_{\ell 22}$$

$$\sigma_{m22}^{(B)} = (E_{\ell22}/E_2)\sigma_{\ell22}$$

$$\sigma_{f22}^{(B)} = (E_{\ell 22}/E_2)\sigma_{\ell 22}$$

where E_2 is given by

$$E_{2} = (1 - \sqrt{k_{f}}) E_{m} + \frac{\sqrt{k_{f}} E_{m}}{1 - \sqrt{k_{f}} \left(1 - \frac{E_{m}}{E_{f22}}\right)}$$

$$\sigma_{m33}^{(A)} = (\nu_m/\nu_{\ell 23})(E_m/E_{\ell 22})\sigma_{\ell 22}$$

$$\sigma_{m33}^{\text{(B)}} = \frac{1 - \sqrt{k_f}}{\sqrt{k_f}} \, \sigma_{\ell 22}$$

$$\sigma_{f33}^{(B)} = \sigma_{m33}^{(B)}$$

Ply microstresses due to inplane shear stress ($\sigma_{f|2}$) are given by

$$\sigma_{m12}^{(A)} = (G_m/G_{12})\sigma_{\ell 12}$$

$$\sigma_{m12}^{(B)} = (G_{\ell 12}/G_{12})\sigma_{\ell 12}$$

$$\sigma_{f12}^{(B)} = (G_{\ell12}/G_{12})\sigma_{\ell12}$$

where G_{12} is given by

$$G_{12} = \left(1 - \sqrt{k_f}\right)G_m + \frac{\sqrt{k_f}G_m}{1 - \sqrt{k_f}\left(1 - \frac{G_m}{G_{f23}}\right)}$$

$$\sigma_{m13}^{(A)} = \sigma_{m12}^{(A)}$$

$$\sigma_{m13}^{(B)} = \sigma_{m12}^{(B)}$$

$$\sigma_{f13}^{(B)} = \sigma_{f12}^{(B)}$$

Ply microstresses due to through-the-thickness shear stress $\sigma_{\ell 23}$ are given by

$$\sigma_{m23}^{(A)} = (G_m/G_{\ell 23})\sigma_{\ell 23}$$

$$\sigma_{m23}^{(\mathrm{B})} = (G_{23}/G_{\ell 23})\sigma_{\ell 23}$$

where G_{23} is given by

$$G_{23} = \frac{G_m}{1 - \sqrt{k_f} \left(1 - \frac{G_m}{G_{f23}} \right)}$$

$$\sigma_{f23}^{(\mathrm{B})} = \sigma_{m23}^{(\mathrm{B})}$$

Ply microstresses due to temperature gradient ΔT_ℓ are given by

$$\sigma_{m11} = (\alpha_{\ell 11} - \alpha_m) \Delta T_{\ell} E_m$$

$$\sigma_{f|1} = (\alpha_{\ell|1} - \alpha_{f|1}) \Delta T_{\ell} E_{f|1}$$

$$\sigma_{m22}^{(A)} = (\alpha_{\ell 22} - \alpha_m) \Delta T_{\ell} E_m$$

$$\sigma_{m22}^{(\mathrm{B})} = \sigma_{f22}^{(\mathrm{B})} = -\frac{1 - \sqrt{k_f}}{\sqrt{k_f}} \quad \sigma_{m22}^{(\mathrm{A})}$$

$$\sigma_{m33}^{(A)} = \sigma_{m22}^{(A)}$$

$$\sigma_{m33}^{(B)} = \sigma_{m22}^{(B)}$$

$$\sigma_{f33}^{(\mathrm{B})} = \sigma_{f22}^{(\mathrm{B})}$$

$$\Delta T_{\ell} = T_{\ell} - T_{cu}$$

Ply microstresses due to moisture M_{ℓ} are given by

$$\sigma_{m11} = (\beta_{\ell 11} - \beta_m) M_{\ell} E_m$$

$$\sigma_{f11} = \beta_{\ell 11} M_{\ell} E_{f11}$$

$$\sigma_{m22}^{(A)} = (\beta_{\ell 22} - \beta_m) M_{\ell} E_m$$

$$\sigma_{m22}^{(B)} = -\frac{1 - \sqrt{k_f}}{\sqrt{k_f}} \sigma_{m22}^{(A)}$$

$$\sigma_{m33}^{(A)} = \sigma_{m22}^{(A)}$$

$$\sigma_{m33}^{(\mathrm{B})} = \sigma_{m22}^{(\mathrm{B})}$$

$$\sigma_{f33}^{(A)} = \sigma_{f33}^{(A)}$$

Subroutine MINCOF.—This subroutine generates the microstress influence coefficients for each different material system used in the layup. The equations used are similar to those programmed for MCRSTR. However, the influence coefficients are based on the application of unit load in a specific direction or unit temperature difference or unit moisture content. The influence coefficients are stored in the matrix PINF. This matrix has 17 entries. They are described in the following list:

Entry	Algebraic notation	Fortran variable
PINF(1,K,NLD)	σ_{m11}	SM11
PINF(2,K,NLD)	$\sigma_{m22}^{({ m A})}$	SM22A
PINF(3,K,NLD)	$\sigma_{m22}^{(\mathrm{B})}$	SM22B
PINF(4,K,NLD)	$\sigma_{m12}^{(\mathrm{A})}$	SM12A
PINF(5,K,NLD)	$\sigma_{m12}^{(\mathrm{B})}$	SM12B
PINF(6,K,NLD)	$\sigma_{m13}^{(\mathrm{A})}$	SM13A
PINF(7,K,NLD)	$\sigma_{m13}^{(\mathrm{B})}$	SM13B
PINF(8,K,NLD)	$\sigma_{m23}^{(\mathrm{A})}$	SM23A
PINF(9,K,NLD)	$\sigma^{ m (B)}_{m23}$	SM23B

PINF(10,K,NLD)	$\sigma_{m33}^{(A)}$	SM33A
PINF(11,K,NLD)	$\sigma_{m33}^{(\mathrm{B})}$	SM33B
PINF(12,K,NLD)	σ_{f11}	SF11
PINF(13,K,NLD)	$\sigma_{f22}^{(\mathrm{B})}$	SF22B
PINF(14,K,NLD)	$\sigma_{f33}^{(\mathrm{B})}$	SF33B
PINF(15,K,NLD)	σ_{f12}	SF12
PINF(16,K,NLD)	σ_{f13}	SF13
PINF(17,K,NLD)	$\sigma_{f23}^{(\mathrm{B})}$	SF23B

The dimension K varies from 1 to NMS, where NMS is the number of material systems. NLD varies from 1 to 7. The expression NLD = 1 to 5 refers to unit applied stresses in 11, 22, 12, 13, and 23, respectively. The expression NLD = 6 corresponds to unit temperature loading, and the expression NLD = 7 corresponds to unit moisture loading.

The microstress influence coefficients are computed for secondary composites and optionally computed for intraply hybrid composites. These are stored in the matrix SINF.

Subroutines AMAXF, AMINF, LOGO, and LOGO2.—These subroutines perform several auxiliary duties. AMAXF finds the maximum value of a one-dimensional array and its location. AMINF finds the minimum value of a one-dimensional array and its location. These two subroutines are utilized by MSCBFL and NUDIFS in conjunction with searching for failure loads and the probable locations of delamination. LOGO is a subroutine to generate the ICAN emblem for the output. The description of the material and the structural coordinate system by appropriate figures is generated by the subroutine LOGO2.

Subroutine INHYD.—This subroutine generates the composite ply properties, necessary for the laminate response analysis. The inputs to this routine are the constituent properties which are supplied in the appropriate format by the subroutines IDGED and BANKRD. INHYD calls the subroutines FIBMT, COMPP, and HTM to perform the micromechanics analysis, including the analysis of hygrothermal effects. The ply properties are stored in the array PROPS, which is accessed by the main program through the labeled common block PBANK. INHYD is called once for each different material system by the main program. The outputs of INHYD show the properties of the fiber, matrix, and composite.

The fiber and matrix properties for the primary composite are read in from the input provided by IDGER. These are stored in arrays PF and PM. Similarly, the arrays SF and SM are used to store the properties of secondary composite constituents if the composite is of the hybrid type. The program then checks for temperature and moisture. The properties of the matrix are updated for the presence of temperature and moisture. The following are the equations programmed to account for the hygrothermal property degradation:

The wet glass transition temperature is computed from

$$T_{gwr} = (0.005M_{\ell}^2 - .1M_{\ell} + 1)T_{gdr}$$

where T_{gwr} is the wet glass transition temperature, T_{gdr} is the dry glass transition temperature for the resin matrix, and M_{ℓ} is the percentage of moisture by weight.

The reduction factors X_{mp} and X_{tp} are computed from

$$X_{mp} = \sqrt{(T_{gwr} - T_u)/(T_{gdr} - T_o)}$$

$$X_{tp} = 1/X_{mp}$$

where T_o is the reference temperature (70 °F), and T_u is the use temperature.

The moduli and strengths of the matrix are multiplied by X_{mp} to obtain the new properties for the matrix. The density is given by

$$\rho_{mw} = \rho_m + 3\rho_m k_m M_1 / 100$$

The thermal properties, such as heat capacity, thermal expansion coefficient, and thermal conductivity are multiplied by the second factor X_{tp} to account for the hygrothermal conditioning.

After the property arrays PF, PM, SF, and SM are properly filled, the program chooses either FIBMT or HTM subroutines to perform micromechanics. The subroutine HTM is chosen if temperature/moisture effects are to be taken into consideration. Otherwise, FIBMT is chosen for dry room temperature property computations. The outputs from these routines are primary and secondary composite ply properties. They are stored in the arrays P and S, respectively. These properties are made common to subroutine COMPP through the common blocks ILAB1 and ILAB3. The subroutine COMPP is called by INHYD for hybrid composites to compute the hybrid composite ply properties. These properties are stored in the array H. One of the arrays P, S, or H are passed to ICAN via common block PBANK and the array PROPS. For example, if the ply is made of 100 percent primary composite only, the array PROPS is assigned to have the same entries as P, etc.

The subroutine INHYD also calls FLEXX, which performs a flexural strength analysis. However, these are only for additional information and are not used by ICAN at the present time.

Subroutine FIBMT (C, F, M, VF, VM, VP, KV, IFLAG).—This subroutine generates properties of a ply by using the constituent properties which are supplied from the subroutine INHYD. The constituent properties are stored in the arrays F and M; F contains the fiber properties, and M contains the matrix properties. The composite properties are stored in the array C, which is returned to INHYD. The theory behind the programmed equations is discussed in reference 13. The following is a description of each entry in the arrays C, F, and M, with the corresponding algebraic notation:

Composite Properties Array C(1)

Entry	Description	Notation
C(1)	elastic moduli	$E_{\ell 1 1}$
C(2)	elastic moduli	$E_{\ell 22}$
C(3)	elastic moduli	$E_{\ell 33}$
C(4)	shear moduli	$G_{\ell 12}$
C(5)	shear moduli	G_{l23}
C(6)	shear moduli	$G_{\ell 13}$
C(7)	Poisson's ratio	$\nu_{\ell 12}$
C(8)	Poisson's Ratio	$\nu_{\ell 23}$
C(9)	Poisson's Ratio	$\nu_{\ell 13}$
C(10)	thermal expansion coefficient	$\alpha_{\ell 1 1}$
C(11)	thermal expansion coefficient	$lpha_{\ell 22}$
C(12)	thermal expansion coefficient	α_{l33}
C(13)	density	$ ho_\ell$
C(14)	heat capacity	C_{ℓ}
C(15)	heat conductivity	$K_{\ell 1 1}$
C(16)	heat conductivity	$K_{\ell 22}$
C(17)	heat conductivity	$K_{\ell 33}$
C(18)	strength	$S_{\ell 1 1 T}$
C(19)	strength	$S_{\ell 11C}$
C(20)	strength	$S_{\ell 22T}$
C(21)	strength	$S_{\ell 22C}$
C(22)	strength	$S_{\ell 12}$
C(23)	moisture diffusivity	$D_{\ell 1 1}$
C(24)	moisture diffusivity	$D_{\ell 22}$
C(25)	moisture diffusivity	$D_{\ell 33}$
C(26)	moisture expansion coefficient	$eta_{\ell 1 1}$
C(27)	moisture expansion coefficient	β_{i22}

C(28)	moisture expansion coefficient	β_{l33}
C(29)	flexural moduli	$E_{\ell 11}$
C(30)	flexural moduli	$E_{\ell 22}$
C(31)	strengths (flexural)	S_{123}
C(32)	strengths (flexural)	S_{l11F}
C(33)	strengths (flexural)	$S_{\ell 22F}$
C(34)	strengths (flexural)	$S_{\ell 12}$
C(35)	ply thickness	t_{ℓ}
C(36)	interply thickness	δ_ℓ
C(37)	interfiber spacing	δ_s
	Fiber Properties Array	
Entry	Description	Notation
F(1)	elastic moduli	E_{f11}
F(2)	elastic moduli	E_{f22}
F(3)	shear moduli	G_{f12}
F(4)	shear moduli	$G_{\mathfrak{S}^2}$
E(5)	Poisson's ratio	-122

thermal expansion coefficient

thermal expansion coefficient

number of fibers per end

Poisson's ratio

Poisson's ratio

fiber diameter

heat conductivity

heat conductivity

heat conductivity

heat capacity

density

strength

strength

F(5)

F(6)

F(7)

F(8)

F(9)

F(10)

F(11)

F(12)

F(13)

F(14)

F(15)

F(16)

F(17)

Matrix Properties Array

 v_{f12}

 ν_{f23}

 α_{f11}

 α_{f22}

 ho_f N_f d_f C_f K_{f11} K_{f22} K_{f33} S_{fT}

Entry	Description	Notation
M(1)	elastic modulus	E_m
M(2)	shear modulus	$G_m^{'''}$
M(3)	Poisson's ratio	ν_m
M(4)	thermal expansion coefficient	α_m
M(5)	density	$\rho_m^{\prime\prime\prime}$
M(6)	heat capacity	C_m
M(7)	heat conductivity	$K_m^{'''}$
M(8)	strength	$S_{mT}^{'''}$
M(9)	strength	S_{mC}^{m1}
M(10)	strength	S_{mS}
M(11)	moisture coefficient	β_m
M(12)	diffusivity	D_m

The following are the programmed equations for the entries in array C:

Normal moduli:

$$E_{\ell 1 1} = k_f E_{f 1 1} + k_m E_m$$

$$E_{\ell 22} = \frac{E_m}{1 - \sqrt{k_f} (1 - E_m / E_{f22})}$$

$$E_{\ell 33} = E_{\ell 22}$$

Shear moduli:

$$G_{\ell 12} = \frac{G_m}{1 - \sqrt{k_f} \left(1 - \frac{G_m}{G_{f12}} \right)}$$

$$G_{\ell 13} = G_{\ell 12}$$

$$G_{\ell 23} = \frac{G_m}{1 - k_f \left(1 - \frac{G_m}{G_{f23}}\right)}$$

Poisson's Ratio:

$$v_{\ell 12} = v_m + k_f (v_{f12} - v_m)$$

$$\nu_{\ell 13} = \nu_{\ell 12}$$

$$v_{\ell 23} = k_f v_{f23} + k_m \left(2v_m - \frac{v_{\ell 12}}{E_{\ell 11}} E_{\ell 22} \right)$$

Coefficients of thermal expansion:

$$\alpha_{f|1} = \frac{\alpha_{f|1} + k_m [(\alpha_m E_m / E_{f|1}) - \alpha_{f|1}]}{1 + k_m \left(\frac{E_m}{E_{f|1}} - 1\right)}$$

$$\alpha_{f22} = \alpha_m (1 - \sqrt{k_f}) \left[\frac{1 + k_f \nu_m E_{f11}}{E_{f11} + k_m (E_m - E_{f11})} \right] + \alpha_{f22} k_f$$

$$\alpha_{33} = \alpha_{f22}$$

Density:

$$\rho_{\ell} = \rho_f k_f + \rho_m k_m$$

Heat capacity:

$$C_{\ell} = \frac{(k_f C_f \rho_f + k_m C_m \rho_m)}{\rho_{\ell}}$$

Heat conductivities:

$$K_{\ell 1 1} = k_f K_{f 1 1} + k_m K_m$$

$$K_{\ell 22} = (1 - \sqrt{k_f}) K_m + \frac{\sqrt{k_f}}{1 - \sqrt{k_f} \left(1 - \frac{K_m}{K_{\ell 22}}\right)} K_m$$

$$K_{\ell 33} = K_{\ell 22}$$

In the preceding equations, K_m should be replaced by

$$K_m \rightarrow (1 - \sqrt{k_\nu})K_m + \frac{K_m \sqrt{k_\nu}}{1 - \sqrt{k_\nu} \left(1 - \frac{K_m}{K_\nu}\right)}$$

if there are voids. The quantity K_{ν} is the void conductivity.

Strengths:

$$S_{\ell 11T} = S_{fT}(k_f + k_m E_m / E_{f11})$$

The longitudinal compressive strength is computed based on three different criteria, rule of mixtures, fiber microbuckling, and delamination. The minimum of the three estimates is returned as $S_{\ell 11C}$. The equations for the three cases are

$$S_{\text{SLLC}}$$
 (rule of mixtures) = $S_{fc}(k_f + k_m E_m / E_{f11})$

$$S_{11C}$$
 (delamination) = $(13S_{\ell 12} + S_{mc})$

$$S_{i11C} \text{ (fiber microbuckling)} = \frac{F_2 G_m}{1 - k_f \left(1 - \frac{G_m}{G_{f12}}\right)}$$

The transverse strengths are calculated from

$$S_{\ell 22T} = S_{mT}(FACT/DENOM)$$

$$S_{022C} = S_{mc}/DENOM$$

$$S_{\ell 12} = \frac{[(F_1 - 1 + G_m / G_{f12})F_2 G_{\ell 12} S_{ms}]}{G_m F_1} \text{ FACT}$$

where F_1 and F_2 are defined by the equations:

$$F_1 = \sqrt{\frac{\pi}{4k_f}}$$

$$F_2 = 1 - \sqrt{\frac{4k_\nu}{\pi k_m}}$$

The variable DENOM is a Fortran variable given by

DENOM =
$$\left[1 - \sqrt{k_f} \left(1 - \frac{E_m}{E_{f22}}\right)\right] \sqrt{1 + \varphi(\varphi - 1) + \frac{1}{3}(\varphi - 1)^2}$$

where φ is given by

$$\varphi = \frac{E_m}{E_{f22} \left[1 - \sqrt{k_f} \left(1 - \frac{E_m}{E_{f22}} \right) \right]}$$

$$\varphi = \frac{F_1 - 1}{F_1 - 1}$$

The Fortran variable FACT takes the value k_m if IFLAG is unity. Otherwise FACT takes the value unity. This variable is introduced to correlate the strengths of HMS and Kevlar fiber composites with the experimentally observed values. The main program INHYD checks for these fibers and assigns the appropriate values for IFLAG. IFLAG is set at zero for other fibers.

Moisture diffusivities:

$$D_{\ell 1 \, 1} = k_m D_m$$

$$D_{\ell 22} = (1 - \sqrt{k_f}) D_m$$

$$D_{\ell 33} = D_{\ell 22}$$

Moisture expansion coefficients:

$$\beta_{\ell 1 1} = \beta_m k_m E_m / E_{\ell 1 1}$$

$$\beta_{\ell 22} = \beta_m (1 - \sqrt{k_f})(1 + k_f \nu_m E_{f11} / E_{\ell 11})$$

$$\beta_{\ell33} = \beta_{\ell22}$$

Flexural moduli $(E_{\ell 11F}, E_{\ell 22F})$:

$$E_{\ell 11F} = E_{\ell 11}$$

$$E_{\Omega 2F} = E_{\Omega 2}$$

Flexural Strengths:

$$S_{\ell 23F} = \frac{\left(F_1 - 1 + \frac{G_m}{G_{f23}}\right) F_2 G_{\ell 23} S_{ms}}{G_m F_1}$$

$$S_{\ell 12F} = 1.5 S_{\ell 12}$$

Ply thickness: A default value of 0.005 is set for t_{ℓ} . This is overridden by the user specified value in the ICAN main program.

Interply thickness and interfiber spacing:

$$\delta_{\ell} = \left(\sqrt{\frac{\pi}{k_f}} - 2\right) \frac{d_f}{2}$$

$$\delta_f = \delta_\ell$$

Subroutine HTM (C, F, M, VF, VM, VV, IFLAG).—This subroutine generates the hygrothermomechanical properties based on the theory proposed in reference 15. The subroutine is called only if nontrivial entries for the use temperature and the moisture content ($T_u \neq 70$ °F or nonzero moisture content) are present. The equations programmed are mostly those discussed in the subroutine FIBMT description. Therefore, only the equations which are different are mentioned here.

Moisture expansion coefficients:

$$\beta_{122} = (1 - \sqrt{k_f})\beta_m \left[1 + \frac{\sqrt{k_f}(1 - \sqrt{k_f})E_m}{\sqrt{k_f}E_{122} + (1 - \sqrt{k_f})E_m} \right]$$

$$\beta_{P33} = \beta_{P22}$$

Strengths:

$$S_{\ell 22T} = \left(\frac{S_{mT}}{E_{m}}\right) \frac{E_{\ell 22} \left(1 - \sqrt{\frac{4k_{\nu}}{\pi k_{m}}}\right) (1 - \sqrt{k_{f}})}{1 - \left(\sqrt{k_{f}} E_{\ell 22} / E_{f 22}\right)} \text{ FACT}$$

$$S_{\ell 22C} = \left(\frac{S_{mC}}{E_m}\right) \frac{E_{\ell 22} \left(1 - \sqrt{\frac{4k_{\nu}}{\pi k_m}}\right) (1 - \sqrt{k_f})}{1 - \left(\sqrt{k_f} E_{\ell 22} / E_{f22}\right)} \text{FACT}$$

$$S_{\ell 12} = \left(\frac{S_{mS}}{G_{m}}\right) G_{\ell 12} \frac{\left(1 - \sqrt{\frac{4k_{\nu}}{\pi k_{m}}}\right) (1 - \sqrt{k_{f}})}{1 - \left(\sqrt{k_{f}} G_{\ell 12} / G_{f 12}\right)} \text{FACT}$$

$$S_{\ell 23F} = \left(\frac{S_{mS}}{G_m}\right) \frac{G_{\ell 23} \left(1 - \sqrt{\frac{4k_{\nu}}{\pi k_m}}\right) (1 - \sqrt{k_f})}{1 - \left(\sqrt{k_f} G_{\ell 23} / G_{f23}\right)}$$

$$S_{\ell 1} {}_2F = 1.5 S_{\ell 1} {}_2$$

In the preceding equations, FACT is a Fortran variable which is given by

$$FACT = \delta_s/\delta_f$$

for Kevlar and HMS fibers. For all other fibers FACT = 1.

Subroutine FLEXX (C).—The entries C(32) and C(33) of the ply property array C are generated in this subroutine. They are, respectively, the longitudinal flexural strength and the transverse flexural strength. The longitudinal flexural strength is given by

$$S_{\ell 11F} = \frac{2.5 S_{\ell 11T}}{\left(1 + \frac{S_{\ell 11T}}{S_{\ell 11C}}\right)}$$

The transverse flexural strength is given by

$$S_{\varnothing 2F} = \frac{2.5S_{\varnothing 2T}}{\left(1 + \frac{S_{\varnothing 2T}}{S_{\varnothing 2C}}\right)}$$

Subroutine COMPP (IPFLAG, ISFLAG).—This subroutine is called by INHYD to generate the properties of a hybrid ply. The equations are based on the theory proposed in reference 13. The properties are stored in the array H. The entries are, however, the same as those of array C given in the description for subroutine FIBMT. The inputs to this routine are the primary composite properties array P, the secondary composites property array S, and the percentage of the secondary composite k_{sc} . The equations are the following:

Elastic normal moduli:

$$E_{\ell 11}(H) = E_{\ell 11}(P) + [E_{\ell 11}(S) - E_{\ell 11}(P)]k_{sc}$$

$$E_{1/2}(H) = \frac{E_{1/2}(P)}{1 + k_{sc}[E_{1/2}(P)/E_{1/2}(S) - 1]}$$

$$E_{\ell 33}(H) = E_{\ell 33}(P) + [E_{\ell 33}(S) - E_{\ell 33}(P)]k_{sc}$$

Shear moduli:

$$G_{\ell 23}(H) = \frac{G_{\ell 23}(P)}{1 - k_{sc} \left(1 - \frac{G_{\ell 23}(P)}{G_{\ell 23}(S)}\right)}$$

$$G_{\ell 12}(H) = \frac{G_{\ell 12}(P)}{1 - k_{sc} \left(1 - \frac{G_{\ell 12}(P)}{G_{\ell 12}(P)}\right)}$$

$$G_{\ell 13}(\mathsf{H}) = G_{\ell 13}(\mathsf{P}) + k_{sc}[\mathsf{G}_{\ell 13}(\mathsf{S}) - G_{\ell 13}(\mathsf{P})]$$

Poisson's ratios:

$$\begin{split} \nu_{\ell 12}(\mathbf{H}) &= \nu_{\ell 12}(\mathbf{P}) + k_{sc}[\nu_{\ell 12}(\mathbf{S}) - \nu_{\ell 12}(\mathbf{P})] \\ \\ \nu_{\ell 13}(\mathbf{H}) &= \nu_{\ell 12}(\mathbf{P}) + \frac{k_{sc}[\nu_{\ell 12}(\mathbf{P}) - \nu_{\ell 12}(\mathbf{S})]}{(1 - k_{sc})[E_{\ell 33}(\mathbf{P}) / E_{\ell 33}(\mathbf{S})] - k_{sc}} \\ \\ \nu_{\ell 23}(\mathbf{H}) &= \nu_{\ell 23}(\mathbf{P}) + k_{sc}[\nu_{\ell 23}(\mathbf{S}) - \nu_{\ell 23}(\mathbf{S})] \end{split}$$

Coefficients of thermal expansion:

$$\alpha_{\ell|1}(H) = \frac{\alpha_{\ell|1}(P) + k_{sc} \{ [\alpha_{\ell|1}(S)E_{\ell|1}(S)/E_{\ell|1}(P)] - \alpha_{\ell|1}(P) \}}{1 + k_{sc} \left(\frac{E_{\ell|1}(S)}{E_{\ell|1}(P)} - 1 \right)}$$

$$\alpha_{\ell|3}(H) = \frac{1}{E_{\ell|3}(H)} \left\{ -\nu_{\ell|3}(H)E_{\ell|3}(H)\alpha_{\ell|1}(H) + (1 - k_{sc})E_{\ell|3}(P) \left[\alpha_{\ell|2}(P) + \nu_{\ell|3}(P)\alpha_{\ell|1}(P) \right] + k_{sc}E_{\ell|3}(S) \left[\alpha_{\ell|2}(S) + \nu_{\ell|3}(S)\alpha_{\ell|1}(S) \right] \right\}$$

$$\alpha_{\ell|2}(H) = (1 - k_{sc}) \left\{ \alpha_{\ell|2}(S) \left[1 + \nu_{\ell|2}(P) \right] + \nu_{\ell|2}(P)\alpha_{\ell|1} \right\} + k_{sc} \left\{ \alpha_{\ell|2}(S) \left[1 + \nu_{\ell|2}(S) \right] + \nu_{\ell|2}(S)\alpha_{\ell|1}(S) \right\}$$

$$-\nu_{\ell|2}(H)\alpha_{\ell|1}(H) - \nu_{\ell|2}(H)\alpha_{\ell|3}(H)$$

Density:

$$\rho_{\ell}(\mathbf{H}) = (1 - k_{sc})\rho_{\ell}(\mathbf{P}) + k_{sc}\rho_{\ell}(\mathbf{S})$$

Heat capacity:

$$C_{\ell}(\mathbf{H}) = \left\{ (1 - k_{sc}) | C_f(\mathbf{P}) k_f(\mathbf{P}) \rho_f(\mathbf{P}) + C_m(\mathbf{P}) k_m(\mathbf{P}) \rho_m(\mathbf{P}) | \right.$$

$$\left. + k_{sc} | C_f(\mathbf{S}) k_f(\mathbf{S}) \rho_f(\mathbf{S}) + C_m(\mathbf{S}) k_m(\mathbf{S}) \rho_m(\mathbf{S}) | \right.$$

$$\left. + |k_f(\mathbf{P}) k_{\nu}(\mathbf{P}) + k_{sc} k_{\nu}(\mathbf{S}) | M \rho_{mst} C_{mst} \right\} / \rho_{\ell}(\mathbf{H})$$

where ρ_{mst} and C_{mst} are the moisture density and heat capacity, respectively.

Heat conductivities:

$$K_{\ell | 1}(H) = (1 - k_{sc})[k_f(P)K_{\ell | 1}(P) + k_m(P)K_m(P)] + k_{sc}[k_f(S)K_{\ell | 1}(S) + k_m(S)K_m(S)]$$

$$K_{\ell 22}(P) = \frac{(1 - \sqrt{k_f(P)}K_m(P) + \sqrt{k_f(P)}K_m(P)}{1 - \sqrt{k_f(P)}[1 - K_m(P)/K_{\ell 22}(P)]}$$

$$K_{\ell 22}(S) = \frac{(1 - \sqrt{k_f(S)}K_m(S) + \sqrt{k_f(S)}K_m(S)}{1 - \sqrt{k_f(S)}[1 - K_m(S)/K_{\ell 22}(S)]}$$

$$K_{\ell 22}(H) = \frac{K_{\ell 22}(P)}{1 - k_{sc}[1 - K_{\ell 22}(S) / K_{\ell 22}(P)]}$$

$$K_{\ell 33}(H) = K_{\ell 22}(H)$$

The void conductivity K_{ν} with moisture content M is given by $K_{\nu} = MK_{mst}$. If there are voids in the primary composite, $K_{m}(P)$ in the preceding equations for heat conductivities is replaced by

$$K_m(P) = [1 - \sqrt{k_v(P)}]K_m(P) + \frac{\sqrt{k_v(P)}K_m(P)}{[1 - \sqrt{k_v(P)}][1 - K_m(P)/K_v]}$$

Similarly, for the secondary composite, $K_m(S)$ is replaced by

$$K_m(S) = [1 - \sqrt{k_{\nu}(S)}]K_m(S) + \frac{\sqrt{k_{\nu}(S)}K_m(S)}{[1 - \sqrt{k_{\nu}(S)}][1 - K_m(S)/K_{\nu}]}$$

Strengths.—The longitudinal strengths are based on the rule of mixtures:

$$S_{\ell 11T}(H) = S_{\ell 11T}(P)(1 - k_{sc}) + S_{\ell 11T}(S)k_{sc}$$

$$S_{\ell 11C}(H) = S_{\ell 11C}(P)(1 - k_{sc}) + S_{\ell 11C}(S)k_{sc}$$

The following are a few intermediate variables defined for convenience in the evaluation of transverse strengths:

$$Q_p = 1 - 2\sqrt{k_{\nu}(P)/\pi} \left[1 - 2\sqrt{k_f(P)/\pi} \right]$$

$$Q_s = 1 - 2\sqrt{k_{\nu}(S)/\pi} \left[1 - 2\sqrt{k_f(S)/\pi} \right]$$

 $S_{mC} = \min[S_{mC}(P) \text{ and } S_{mC}(S)]$

 $S_{mT} = \min[S_{mT}(P) \text{ and } S_{mT}(S)]$

 $S_{mS} = \min[S_{mS}(P) \text{ and } S_{mS}(S)]$

FACT $1 = k_m(P)$ (for HMS and Kevlar fibers)

FACT $2 = k_m(S)$ (for HMS and Kevlar fibers)

FACT 1 = FACT 2 = 1 (for all other fibers)

$$S_{\ell 22}(P) = \frac{(1 - k_{sc})Q_p / E_{P22}(P) \left[1 - \sqrt{\frac{k_f(P)}{\pi}} \left(1 - \frac{E_m(P)}{E_{f22}(P)} \right) \right]}{1 - \sqrt{k_f(P)} \left(1 - \frac{E_m(P)}{E_{f22}(P)} \right)} S_m(P)$$

$$S_{f22}(S) = \frac{\frac{k_{sc}Q_s}{E_{f22}(S)} \left[1 - \sqrt{\frac{k_f(S)}{\pi}} \left(1 - \frac{E_m(S)}{E_{f22}(S)} \right) \right]}{1 - \sqrt{k_f(S)} \left(1 - \frac{E_m(S)}{E_{f22}(S)} \right)} S_m(S)$$

$$\varphi_{p} = \frac{\sqrt{\frac{\pi}{4k_{f}(P)}} - \frac{E_{m}(P)}{E_{f22}(P) \left[1 - \sqrt{k_{f}(P)} \left(1 - \frac{E_{m}(P)}{E_{f22}(P)}\right)\right]}}{\sqrt{\frac{\pi}{4k_{f}(P)}} - 1}$$

$$\varphi_{s} = \frac{\sqrt{\frac{\pi}{4k_{f}(S)}} - \frac{E_{m}(S)}{E_{f22}(S) \left[1 - \sqrt{k_{f}(S)} \left(1 - \frac{E_{m}(S)}{E_{f22}(S)}\right)\right]}}{\sqrt{\frac{\pi}{4k_{f}(S)}} - 1}$$

DENOMP =
$$1 - \sqrt{k_f(P)} \left(1 - \frac{E_m(P)}{E_{f22}(P)} \right) \sqrt{1 + \varphi_p(\varphi_p - 1) + \frac{1}{3} (\varphi_p - 1)^2}$$

DENOMS =
$$1 - \sqrt{k_f(S)} \left(1 - \frac{E_m(S)}{E_{f22}(S)} \right) \sqrt{1 + \varphi_s(\varphi_s - 1) + \frac{1}{3}(\varphi_s - 1)^2}$$

The transverse and the shear strengths of hybrid composites are given by

$$S_{\ell 22T}(H) = E\ell 22(H) \left[\frac{(1 - k_{sc})FACT1}{E_{\ell 22}(P)DENOMP} + \frac{k_{sc}FACT2}{E_{\ell 22}(S)DENOMS} \right] S_{mT}$$

$$S_{\ell 22C}(H) = E\ell 22(H) \left[\frac{(1 - k_{sc})}{E_{\ell 22}(P)DENOMP} + \frac{k_{sc}}{E_{\ell 22}(S)DENOMS} \right] S_{mC}$$

$$S_{\ell 12}(H) = \frac{2G_{\ell 12}}{\pi} \left\{ \frac{\frac{(1 - k_{sc})Q_p}{G_{\ell 12}(P)} \text{ FACT1} \left[1 - \sqrt{\frac{k_f(P)}{\pi}} \left(1 - \frac{G_m(P)}{G_{\ell 12}(P)} \right) \right]}{1 - \sqrt{k_f(P)} \left(1 - \frac{G_m(P)}{G_{\ell 12}(P)} \right)} \right\}$$

$$+\frac{\frac{k_{sc}Q_{s}}{G_{\ell12}(S)}\operatorname{FACT2}\left[1-\sqrt{\frac{k_{f}(S)}{\pi}\left(1-\frac{G_{m}(S)}{G_{\ell12}(S)}\right)}\right]}{1-\sqrt{k_{f}(S)}\left(1-\frac{G_{m}(S)}{G_{l12}(S)}\right)}\right\}S_{mS}$$

Moisture diffusivity:

$$D'_{\ell}(P) = \frac{1 - \sqrt{k_{\nu}(P)} + k_{\nu}(P)}{[1 - \sqrt{k_{\ell}(P)}]D_{\ell}(P)}$$

$$D'_{\ell}(S) = \frac{1 - \sqrt{k_{\nu}(S)} + k_{\nu}(S)}{[1 - \sqrt{k_{\ell}(S)}]D_{\ell}(S)}$$

$$D_{\ell 11}(H) = (1 - k_{sc})k_m(P)D_{\ell}'(P) + k_{sc}k_m(S)D_{\ell}'(S)$$

$$D_{\ell 22}(H) = (1 - k_{sc}) \left[1 - 2\sqrt{k_f(P)} \right] D_{\ell}(P) + k_{sc} \left[1 - \sqrt{k_f(S)} \right] D_{\ell}(S)$$

$$D_{\ell 33}(H) = D_{\ell 22}(H)$$

Moisture expansion coefficients:

$$\beta_{\ell 11}(\mathbf{P}) = \frac{k_m(\mathbf{P})\beta_m(\mathbf{P})E_m(\mathbf{P})}{k_f(P)E_{f11}(\mathbf{P}) + k_m(\mathbf{P})E_m(\mathbf{P})}$$

$$\beta_{\ell \mid 1}(S) = \frac{k_m(S)\beta_m(S)E_m(S)}{k_f(S)E_{f\mid 1}(S) + k_m(S)E_m(S)}$$

$$\beta_{\ell 22}(P) = \beta_m(P) \left[1 - \sqrt{k_f(P)} \right] \left\{ 1 + \frac{k_f(P)k_m(P)E_{f11}(P)}{E_{f11}(P) + k_m(P)[E_m(P) - E_{f11}(P)]} \right\}$$

$$\beta_{\ell 22}(S) = \beta_m(S) \left[1 - \sqrt{k_f(S)} \right] \left\{ 1 + \frac{k_f(S) k_m(S) E_{f11}(S)}{E_{f11}(S) + k_m(S) \left[E_m(S) - E_{f11}(S) \right]} \right\}$$

$$\beta_{\ell | 1}(\mathbf{H}) = \frac{\left[(1 - k_{sc}) k_m(\mathbf{P}) \beta_m(\mathbf{P}) E_m(\mathbf{P}) + k_{sc} k_m(\mathbf{S}) \beta_m(\mathbf{S}) E_m(\mathbf{S}) \right]}{E_{\ell | 1}(\mathbf{H})}$$

$$\begin{split} \beta_{\ell 33}(\mathbf{H}) &= \left\{ -\nu_{\ell 13}(\mathbf{H}) E_{\ell 33}(\mathbf{H}) \beta_{\ell 11}(\mathbf{H}) + (1-k_{sc}) E_{\ell 33}(\mathbf{P}) [\beta_{\ell 22}(\mathbf{P}) + \nu_{\ell 13}(\mathbf{P}) \beta_{\ell 11}(\mathbf{P})] + k_{sc} E_{\ell 33}(\mathbf{S}) [\beta_{\ell 22}(\mathbf{S}) + \nu_{\ell 13}(\mathbf{S}) \beta_{\ell 11}(\mathbf{S})] \right\} \Big/ E_{\ell 33}(\mathbf{H}) \end{split}$$

$$v_{\ell 12}(P) = v_m(P) + k_f(P)[v_{f12}(P) - v_m(P)]$$

$$v_{f|2}(S) = v_m(S) + k_f(S)[v_{f|2}(S) - v_m(S)]$$

$$\nu_{\ell 32}(P) = \nu_m(P) + k_f(P) [\nu_{f23}(P) - \nu_m(P)]$$

$$\nu_{\ell32}(\mathbf{S}) = \nu_m(\mathbf{S}) + k_f(\mathbf{S}) \big[\nu_{f23}(\mathbf{S}) - \nu_m(\mathbf{S})\big]$$

$$\begin{split} \beta_{\ell 22}(\mathbf{H}) &= (1-k_{sc})[\beta_{\ell 22}(\mathbf{P})(1+\nu_{\ell 32}(\mathbf{P}))+\nu_{\ell 12}(\mathbf{P})\beta_{\ell 11}(\mathbf{P})] + k_{sc}[\beta_{\ell 22}(\mathbf{S})(1+\nu_{\ell 32}(\mathbf{S}))\\ &+\nu_{\ell 12}(\mathbf{S})\beta_{\ell 11}(\mathbf{S})] - \nu_{\ell 12}(\mathbf{H})\beta_{\ell 11}(\mathbf{H}) - \nu_{\ell 23}(\mathbf{H})\beta_{\ell 33}(\mathbf{H}) \end{split}$$

Flexural moduli:

$$E_{\ell 1.1E}(H) = E_{\ell 1.1}(H)$$

$$E_{\ell 22F}(H) = E_{\ell 22}(H)$$

Flexural strengths:

$$S_{\ell 23F}(H) = \frac{2G_{\ell 23}(H)}{\pi} \left\{ \frac{\left(1 - k_{sc}\right)Q_{p}}{G_{\ell 23}(P)} \left[1 - \sqrt{\frac{k_{f}(P)}{\pi}} \left(1 - \frac{G_{m}(P)}{G_{\ell 23}(P)}\right)\right] - \sqrt{k_{f}(P)} \left(1 - \frac{G_{m}(P)}{G_{\ell 23}(P)}\right) + \frac{k_{sc}Q_{s}}{G_{\ell 23}(S)} \frac{\left[1 - \sqrt{\frac{k_{f}(S)}{\pi}} \left(1 - \frac{G_{m}(S)}{G_{\ell 23}(S)}\right)\right]}{1 - \sqrt{k_{f}(S)} \left(1 - \frac{G_{m}(S)}{G_{\ell 23}(S)}\right)} \right\} S_{m}(S)$$

$$S_{\ell 12SB}(H) = 1.5S_{\ell 12}(H)$$

Fiber volume ratio:

$$k_f(H) = k_f(P) + k_{sc}[k_f(S) - k_f(P)]$$

Subroutines BANKRD and IDGER.—These two subroutines do preprocessing to generate compatible input data to the subroutine INHYD. The subroutine BANKRD is called first by the ICAN main program. The input to this routine is primarily the data supplied on the material card MATCRD by the user. These cards indicate the coded names for the fiber and matrix, the volume ratios of primary and secondary composites, and their respective fiber, and the matrix and void volume ratios. The subroutine BANKRD has its own data base containing the properties of fibers and matrices of commonly used materials. This data base is assigned to input unit 8. It is named FBMTDATA.BANK. The output of BANKRD are the arrays PFP, PFS, PMP, and PMS. The entries in PFP and PFS are the fiber properties of primary and secondary composites. The entries in PMP and PMS are the matrix properties of primary and secondary composites. These arrays are made common to the main program and the subroutine IDGER through the labeled common block MFBANK. The entries of PF and PM arrays are explained in the following list:

Fiber Property Arrays PFP and PFS

Entry	Description	Notation
1	not used	
2	fiber density	$ ho_f$
3	normal moduli	${E}_{f11}$
4	normal moduli	$egin{array}{c} ho_f \ E_{f11} \ E_{f22} \end{array}$
5	Poisson's ratio	ν_{f12}
6	Poisson's ratio	ν_{f23}
7	shear moduli	G_{f12}
8	shear moduli	G_{f23}^{f12}
9	thermal expansion coefficient	α_{f11}
10	thermal expansion coefficient	α_{f22}
11	heat conductivity	K_{fl1}
12	heat conductivity	K_{f22}
13	heat capacity	$K_{f22} \atop C_f \atop S_{fC}$
14	strengths	S_{fT}^{\prime}
15	strengths	S_{fC}
16	not used	
17	not used	
18	not used	
19	not used	
20	number of fibers per end	N_f
21	fiber diameters	d_f^J

Matrix Property Arrays PMP and PMS

Entry	Description	Notation
1	not used	
2	density	ρ_m
3	normal modulus	E_m
4	Poisson's ratio	ν_m
5	coefficient of thermal expansion	α_m
6	heat conductivity	K_m
7	heat capacity	C_m
8	tensile strength	S_{mT}
9	compressive strength	S_{mC}
10	shear strength	S_{mS}
11	allowable tensile strain	ϵ_{mT}
12	allowable compressive strain	ϵ_{mC}
13	allowable shear strain	ϵ_{mS}
14	allowable torsional strain	ϵ_{mTOR}
15	void conductivity	$K_{ u}$
16	glass transition temperature	T_{gdr}

The coded names for the fiber and matrix are stored in the matrix CODES by the main program. The entries in CODES are explained as follows:

CODES(1,1,I)	coded name of primary fiber
CODES(1,2,I)	coded name of primary matrix
CODES(2,1,I)	coded name of secondary fiber
CODES(2,2,I)	coded name of secondary matrix

The subroutine IDGER takes the information generated by BANKRD and arranges it in a proper format for the subroutine INHYD. These data are transferred to input unit 7 prior to calling INHYD. These data are purged at the end of the program execution.

Data Base FBMTDATA.BANK.

The constituent properties data base is a unique feature of the computer code ICAN. Its primary aim is to reduce the burden on the user by preparing properly formatted data for the program. The user only needs to specify the coded names for the fiber and matrix. The format of the data is explained in this section so as to enable the user to introduce new contents or to modify existing entries as appropriate to his/her needs. Data for four fibers and three matrices are provided in the present package.

The fiber properties are arranged in five physical cards of 80 column length. The first card contains a four-character code name of a fiber in format A4. The second to the fifth cards start with a two-letter mnemonic to indicate the type of properties that follow. The format on any of these cards is A4, 7E10.3, except for the second card. The second card is in the format A3, I6, 7E10.3. The mnemonics FP, FE, FT, and FS stand for fiber physical, elastic, thermal, and strength-related properties, respectively. The entries on these cards are explained as follows:

```
card 1 four character coded name for fiber card 2 FP; N_f, d_f, \rho_f card 3 FE; E_{f11}, E_{f22}, \gamma_{f12}, \gamma_{f23}, G_{f12}, G_{f23} card 4 FT; \alpha_{f11}, \alpha_{f22}, K_{f11}, K_{f22}, C_f card 5 FS; S_{fT}, S_{fC} (The remaining entries are open for future modifications.)
```

The matrix properties are arranged next after the line OVER END OF FIBER PROPERTIES. The properties have essentially the same format as those for fiber property cards. There are, however, six physical cards for each matrix material. The mnemonics used are MP, ME, MT, MS, and MV. They stand for matrix physical, elastic, thermal, strength-related, and miscellaneous properties, respectively. The format for the first card is A4, and the format for the rest of the cards is A3, 7E10.3. The entries in each card are as follows:

```
card 1 four character coded name for matrix card 2 MP; \rho_m card 3 ME; E_m, \nu_m, \alpha_m card 4 MT; K_m, C_m card 5 MS; S_{mT}, S_{mC}, S_{mS}, \epsilon_{mT}, \epsilon_{mC}, \epsilon_{mS}, \epsilon_{mTOR} card 6 MV; K_{\nu}, T_{gdr}
```

The data base presently contains properties for T-300 (T300), AS graphite (AS--), S-Glass (SGLA), and HMS (HMSF) fibers. The available matrix materials are high-modulus, high-strength (HMHS), intermediate-modulus, high-strength (IMLS) matrices, which are epoxy-type resins. The complete list of properties is shown in appendix C.

Lewis Research Center National Aeronautics and Space Administration Cleveland, Ohio, October 11, 1985

Appendix A List of Code Identifiers

Engineering symbol	Fortran symbol code	Comment
A_{cx}	ACX	composite axial stiffness; generated in subroutine GPCFD2
A_{cx}^R	RAC	reduced axial stiffness; computed in subroutine GPCFD2
BIDE	Boolean	true if interply effects are included; input
C_{cx}	CPC	composite coupling stiffness; generated in subroutine GPCFD2
C_{e1}	RESF	string with force variables in BLOCK DATA
C_{e2}	DISP	string with displacement variables in BLOCK DATA
COMSAT	Boolean	true if COMSA is executed; input
CSANB	Boolean	true if membrane and bending symmetry exists; input
D_{cx}	FTC	composite flexural rigidities; generated in subroutine GPCFD2
D_{cx}^R	RDC	reduced bending rigidities; computed in subroutine GPCFD2
D_f	DIAF	filament equivalent diameter; input
D_v	DISV, DISVI	displacement vectors; DISVI is either read in main program, or is generated in subroutine COMSA
E_f , E_{cf}	ECF	filament elastic constants; input
$E_{f11,\ell11,m11}$	EF11,EL11,EM11	filament, ply, and matrix normal moduli; filament and
		matrix moduli input
$G_{f12,\ell12,m11}$	EF12,EL12,EM12	filament, ply, and matrix shear moduli; filament and matrix shear moduli input
$E_{\mathfrak{G}}E_{\mathfrak{C}\ell}$	ECL	ply elastic constants; generated in subroutine INHYD
E_m, E_{cm}	ECM	matrix elastic constants; generated in subroutine INHYD
H_j	PL(9,I)	interply distortion energy coefficient; generated in main program
H_{kc}	СНК	array of constituent heat conductivities; input
$h_c^{\kappa c}$	ННС	composite heat capacity stored in PC(18) and PC(54)
i,j	I,J	index; generally ply or interply
$K_{cxx,cyy,cxy}$	HK11,22,33	composite two-dimensional heat conductivities in PC(51) to PC(53)
$K_{c11,c22,c33}$	HK11,22,33	composite three-dimensional heat conductivities along
		the material axes in, PC(15) to PC(17)
$K_{\rm f,v}$	KF,V	apparent fiber and void volume ratios; input
$K_{\mathrm{f}11,\ell11,m11}$	CHK	see H_{kc}
$K_{1xx,1yy,1xy}$	XK1,XK2,XK3	stress concentration factors generated in STRCNF
$k_{f,m}$	KFB,MB	actual fiber and matrix volume ratios
$k_{f\ell,v\ell}$	KFL,VL	ply apparent fiber and void volume ratios
L_{sc}	LSC	array of limiting conditions; input
M_{cx}	MBS	applied moment; input
$M_{cT_{\ell}X}$	MSDT MSDH	thermal moments; generated in GPCFD2
$\frac{M_{cM_ex}}{m}$	M	hygral moments; generated in GPCFD2
N_{cx}	NBS	load condition index applied membrane loads; input
$N_{cM_{iX}}$	NSDH	hygral force; generated in GPCFD2
$N_{cT_{e}x}$	NSDT	thermal force; generated in GPCFD2
N_f	NFPE	number of filaments per end; input
N_{ℓ}	NL	number of plies; input

$N_{\ell\!c}$	NLC	number of load conditions; input
N_{ms}	NMS	number of material systems; input
N_{pc}	NPC	string PROPC length; input
$N_{p\ell}$	NPL	string PROP length; input
NONUDF	Boolean	
		T (true) if Poisson's ratio difference chart is to be suppressed
$P_{_{C}}$	PC	composite properties array; generated in GACD3 and GPCFD2
P_{cp}	PROPC	string PROPC; composite property identifiers in GDCFD2
P_ℓ	PL	ply property array; portions generated in all parts of the program
$P_{\ell \! p}$	PROP	string PROP; ply properties identifiers in main program
	QF,I,P,R,S	indices to print out string PROP
$Q_{f,i,p,r,s} \ R$	R	transformation matrix; GACD3, GPCFD2, and COMSA
RINDV	Boolean	T (true) if displacements are read in; input
$S_{\ell 11T}$, etc.	PL(51) to PL(59,I)	ply limit stresses; generated in GLLSC
t_{ℓ}	TL	ply thickness; input
\dot{w}_{cb}	W _{XX}	composite local curvatures relative to the structural axes
α_c	CTE	composite coefficient of thermal expansion; three-
(dimensional in PC(12) to PC(14), two-dimensional in PC(48) to PC(50)
$\alpha_{f,\ell,m}$	VAF,AL,AM	filament, ply, and matrix thermal coefficients of expansion; input
$\beta_{e, \nu e}$	VCF	correlation factors for ply thermoelastic properties and strain magnification factors; set to unity in COMSA
β_h	BTA	correlation factors for ply heat conductivity; set to unity in COMSA
$oldsymbol{eta}_{\mathcal{S}}$	BET	correlation factors for ply strength; set to unity in COMSA
δ_ℓ	PL(8,1)	interply layer thickness; generated in INHYD
ϵ_{CSX}	UX	reference plane membrane strain; solved in terms of N_{cx} or input
ϵ_{ℓ}	EPS,PL(74) to PL(66,I)	ply strains; generated in COMSA
θ_{cs}	THCS	angle between composite material and structural axes;
Ç		input
$\theta_{\ell i}, \theta_{\ell C}$	THLC	angle between ply material and composite axes; input
ν_{f12} , ℓ_{12} , m_{12}	NUF12,L12,M12	filament, ply, and matrix Poisson's ratios; input
π	PIE	constant; input
$ ho_{f,m,\ell}$	RHOF,M,L	filament and matrix weight density; input and generated in FIBMT, HTM, and COMPP
σ_f , σ_m	SF, SM	microstresses in fibers and matrices generated in MCRSTR
ℓ_i	XPL,XSL,YPL,YSL	boundary zone decay length; generated in the main program and paired to EDGSTR
σ_ℓ	SIGL,PL(67) to PL(69,I)	ply stress; generated in COMSA

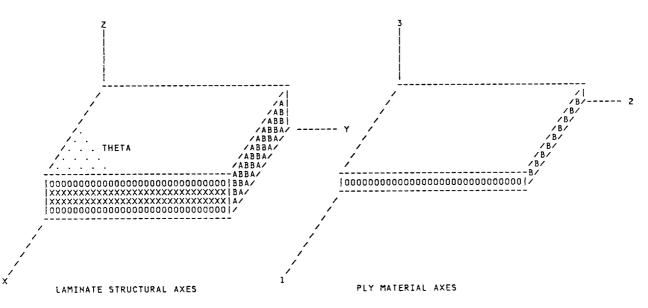
Appendix B Sample Input/Output

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Item 2
I C A N: COORDINATE SYSTEMS



I CAN INPUT DATA ECHO

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FOUR PLY SYMMETRIC LAMINATE. ICAN SAMPLE INPUT DATA.

STDATA 4 1 2

T COMSAT
F CSANB
F RINDV
T NONUDF
PLY 1 1 1 70.00 70.0 .0 0.0 .010
PLY 2 2 70.00 70.0 .0 90.0 .005
PLY 3 2 70.00 70.0 .0 90.0 .005
PLY 4 1 70.00 70.0 .0 90.0 .005
PLY 4 1 70.00 70.0 .0 90.0 .005
PLY 4 1 70.00 70.0 .0 90.0 .010
MATCRDAS--IMLS .55 .02 AS--IMLS 0.0 .57 .03
MATCRDSGLAHMHS .55 .01 AS--IMHS 0.4 .57 .01
PLOAD 1000. 0.0 0.0 0.0 0.0 MX,NY,NXY,THCS
PLOAD 0.0 0.0 0.0 0.0 MX,NY,NXY
PMX/PRSS
```

Item 4

SUMMARY OF INPUT DATA

FOUR PLY SYMMETRIC LAMINATE. ICAN SAMPLE INPUT DATA.

--- CASE CONTROL DECK ---NUMBER OF LAYERS NL = 4
NUMBER OF LOADING CONDITIONS NLC = 1
NUMBER OF MATERIAL SYSTEMS NMS = 2

COMSAT CSANB BIDE RINDV NONUDE

	LAMINATE	100	FIGURATIO	H	_	
PLY	но	MID	DELTAT	DELTAM	THETA	T-NESS
PLY PLY PLY PLY	1 2 3 4	1 2 2 1	0.000 0.000 0.000 0.000	0.0% 0.0% 0.0% 0.0%	0.0 90.0 90.0 0.0	0.010 0.005 0.005 0.010

	COMPOS	ITE MATERI	AL SYST	 			
MATCRD	MID	PRIMARY	VFP	SECONDARY		VFS	vvs
MATCRD MATCRD	1 2	ASIMLS SGLAHMHS		ASIMLS ASIMHS	0.00	0.57 0.57	0.03 0.01

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> CONS	TITUENT PROPERTIES: EC	HO FROM DATA B	ANK. <	OF	POOR	PAGE IS QUALITY
PRIMARY	FIBER PROPERTIES; A	S FIBER			11	ANYFILLA
1	ELASTIC MODULI	EFP1 EFP2	0.3100E 08 0.2000E 07			
2 3 4 5 6 7	SHEAR MODULI	GFP12 GFP23	0.2000E 07 0.1000E 07			
5	POISSON'S RATIO	NUFP12 NUFP23	0.2000E 00 0.2500E 00			
7 8	THERM. EXP. COEF.	CTEFP1 CTEFP2	-0.5500E-06 0.5600E-05			
9 10	DENSITY NO. OF FIBERS/END	RHOFP NFP	0.6300E-01 0.1000E 05			
11 12	FIBER DIAMETER HEAT CAPACITY	DIFP CFPC	0.3000E-03 0.1700E 00			
13 14	HEAT CONDUCTIVITY	KFP1 KFP2	0.5800E 03 0.5800E 02			
15 16 17	STRENGTHS	KFP3 SFPT SFPC	0.5800E 02 0.4000E 05 0.4000E 06			
PRIMARY	MATRIX PROPERTIES;		DRY RT. PROPERTIES.			
1 2 3	ELASTIC MODULUS SHEAR HODULUS	EMP GIIP	0.5000E 06 0.1773E 06			
3 4	POISSON'S RATIO THERM. EXP. COEF.	HUMP CTEMP	0.4100E 00 0.5700E-04 0.4600E-01			
4 5 6 7	DENSITY HEAT CAPACITY HEAT CONDUCTIVITY	RHOMP CMPC KMP	0.46002-01 0.2500E 00 0.1250E 01			
8 9	STRENGTHS	SMPT SMPC	0.7000E 04 0.2100E 05			
10 11	MOISTURE COEF	SMPS BTAMP	0.7000E 04 0.4000E-02			
12	DIFFUSIVITY	DIFMP	0.2000E-03			

Item 5(b)

PRIMARY COMPOSITE PROPERTIES; 55/ 43 AS--/IMLS

BASED ON MICROMECHANICS OF INTRAPLY HYBRID COMPOSITES: ELASTIC AND THERMAL PROPERTIES.

FIBER VOLUME RATIO - 0.550 MATRIX VOLUME RATIO - 0.430 VOID VOLUME RATIO - 0.020 VOID CONDUCTIVITY - 0.22499990E 00

1 2	ELASTIC MODULI	EPC1 EPC2 EPC3	0.1726E 08 0.1127E 07 0.1127E 07
1 2 3 4 5 6 7 8 9	SHEAR MODULI	GPC12 GPC23 GPC13	0.5470E 06 0.3238E 06 0.5470E 06
6 7 8	POISSON'S RATIO	NUPC12 NUPC23	0.2945E 00 0.4821E 00 0.2945E 00
10 11	THERM. EXP. COEF.	NUPC13 CTEPC1 CTEPC2	0.1418E-06 0.2464E-04 0.2464E-04
12 13 14		CTEPC3 RHOPC CPC	0.5443E-01 0.1991E 00
15	HEAT CONDUCTIVITY	KPC1	0.3195E 03
16		KPC2	0.3702E 01
17		KPC3	0.3702E 01
18	STRENGTHS	SPC1T	0.2228E 06
19		SPC1C	0.8764E 05
20		SPC2T	0.5006E 04
21	MOIST. DIFFUSIVITY	SPC2C	0.1502E 05
22		SPC12	0.5126E 04
23		DPC1	0.8600E-04
24	MOIST. EXP. COEF.	DPC2	0.5168E-04
25		DPC3	0.5168E-04
26		BTAPC1	0.4981E-04
27 28 29	FLEXURAL MODULI	BTAPC2 BTAFC3 EPC1F	0.1726E 08
30	51115.1011.10	EPC2F	0.1127E 07
31		SFC23	0.3983E 04
32		SPC1F	0.1572E 06
33	PLY THICKNESS	SPC2F	0.9387E 04
34		SPCSB	0.7689E 04
35		TPC	0.5000E-02
- 36 37	INTERPLY THICKNESS	PLPC	0.5850E-04
	INTERFIBER SPACING	PLPCS	0.5850E-04

Item 5(c)

--> CONSTITUENT PROPERTIES: ECHO FROM DATA BANK. <--PRIMARY FIBER PROPERTIES; SGLA FIBER ELASTIC MODULI 0.1240E 08 0.1240E 08 0.1240E 08 0.5170E 07 0.5170E 07 0.2000E 00 EFP2 GFP12 SHEAR MODULI GFP23 NUFP12 POISSON'S RATIO 6 7 NUFP23 THERM. EXP. COEF. CTEFP1 0.2800E-05 8 0.28C0E-05 DENSITY RHOFP 0.9000E-01 NO. OF FIBERS/END FIBER DIAMETER 10 11 NFP DIFP 0.2040E 03 0.3600E-03 0.1700E 00 0.7500E 01 0.7500E 01 12 13 14 15 CFPC KFP1 KFP2 HEAT CAPACITY HEAT CONDUCTIVITY STRENGTHS SEPT 0.3000E 06 PRIMARY MATRIX PROPERTIES; HMHS MATRIX. DRY RT. PROPERTIES. ELASTIC MODULUS EMP 0.7500E 06 SHEAR MODULUS POISSON'S RATIO 0.2778E 06 0.3500E 00 0.4000E-04 GMP THERM. EXP. COEF. DENSITY NUMP CTEMP 0.4500E-01 0.2500E 01 0.2500E 05 0.2000E 05 0.5000E 05 RHOMP HEAT CONDUCTIVITY 6 KMP 8 STRENGTHS SMPT SMPC SMPS 10 11 MOISTURE COEF BTAMP 0.4000E-02 DIFFUSIVITY DIFMP 0.2000E-03

Item 5(d)

PRIMARY COMPOSITE PROPERTIES; 55/ 44 SGLA/HMHS

BASED ON MICROMECHANICS OF INTRAPLY HYBRID COMPOSITES: ELASTIC AND THERMAL PROPERTIES.

FIBER VOLUME RATIO - 0.550 MATRIX VOLUME RATIO - 0.440 VOID VOLUME RATIO - 0.010 VOLUME RATIO - 0.22499990E 00

```
EPC1
EPC2
EPC3
GPC12
GPC23
GPC13
NUPC12
                                                                                              0.7150E 07
0.2473E 07
0.2473E 07
0.9314E 06
0.5792E 06
                ELASTIC MODULI
  2
                SHEAR MODULI
                                                                                              0.9314E 06
0.2675E 00
0.3778E 00
                POISSON'S RATIO
                                                                      NUPC13
NUPC13
CTEPC1
CTEPC2
CTEPC3
RHOPC
  89
                                                                                              0.2675E 00
                THERM. EXP. COEF.
10
11
12
13
14
15
16
17
                                                                                              0.1580E-04
0.1580E-04
0.6930E-01
0.1929E 00
                DENSITY
                                                                      CPC
KPC1
KPC2
KPC3
SPC1T
                HEAT CAPACITY
HEAT CONDUCTIVITY
                                                                                              0.4675E 01
0.2750E 01
0.2750E 01
0.2076E 06
18
                STRENGTHS
                                                                       SPC1C
SPC2T
                                                                                              0.1730E 06
0.1256E 05
0.3140E 05
20
21
22
23
                                                                      SPC2C
SPC12
DPC1
DPC2
DPC3
                                                                                              0.1047E 05
0.8800E-04
                MOIST. DIFFUSIVITY
24
25
26
27
                                                                                             0.5168E-04
0.5168E-04
0.1846E-03
0.1379E-02
                MOIST. EXP. COEF.
                                                                      BTAPC1
BTAPC2
                                                                      BTAPC3
EPC1F
EPC2F
SPC23
SPC1F
SPC2F
                                                                                             0.1379E-02
0.1379E-02
0.7150E 07
0.2473E 07
0.6510E 04
0.2359E 06
28
29
30
31
32
33
                FLEXURAL MODULI
                STRENGTHS
                                                                                             0.2243E 05
0.1570E 05
                                                                      SPCSB
TPC
PLPC
                PLY THICKNESS
                                                                                             0.5000E-02
0.7020E-04
                INTERPLY THICKNESS
INTERFIBER SPACING
                                                                      PLPCS
                                                                                             0.7020E-04
```

Item 5(e)

--> CONSTITUENT PROPERTIES: ECHO FROM DATA BANK. <--SECONDARY FIBER PROPERTIES; AS-- FIBER 0.310CE 03 0.2000E 07 0.2000E 07 0.1000E 07 0.2500E 00 0.2500E 00 0.5500E-06 0.5600E-05 0.6300E-01 0.1000E 05 0.3000E-03 0.1700E 03 0.5800E 03 0.5800E 02 0.5800E 02 EFS1 EFS2 GFS12 ELASTIC MODULI SHEAR MODULI GFS23 NUFS12 NUFS23 CTEFS1 POISSON'S RATIO THERM. EXP. COEF. CTEFS2 RHOFS DEMSITY
NO. OF FIBERS/END
FIBER DIAMETER
HEAT CAPACITY
HEAT CONDUCTIVITY NFS DIFS CFSC KFS1 KFS2 KFS3 SFST SFSC 1 Ó 11 12 13 14 15 16 17 STRENGTHS IMHS MATRIX. DRY RT. PROPERTIES. SECONDARY MATRIX PROPERTIES; ELASTIC MODULUS
SHEAR MODULUS
FOISSON'S RATIO
THERM. EXP. COEF.
DENSITY 0.5000E 06 0.5000E 06 0.1852E 06 0.3500E 00 0.3600E-04 0.4400E-01 0.2500E 01 0.1250E 01 0.1500E 05 0.3500E 05 0.3500E 05 0.4000E-02 0.2000E-03 EMS GUS RHOMS HEAT CAPACITY
HEAT CONDUCTIVITY
STRENGTHS KMS SNST SMSC SMSS 10 MOISTURE COEF DIFFUSIVITY BTAMS DIFIIS

Item 5(f)

SECONDARY COMPOSITE PROPERTIES; 57/ 42 AS--/IMHS

BASED ON MICROMECHANICS OF INTRAPLY HYBRID COMPOSITES: ELASTIC AND THERMAL PROPERTIES.

FIBER VOLUME RATIO - 0.570 MATRIX VOLUME RATIO - 0.420 VOID VOLUME RATIO - 0.010 VOID CONDUCTIVITY - 0.22499990E 00

1 2 3	ELASTIC MODULI	ESC1	0.1788E 08
2		ESC2 ESC3	0.1153E 07 0.1153E 07
3	SHEAR MODULI	GSC12	0.1153E 07 0.5880E 06
5	SHEAR HODOLI	GSC23	0.3458E 06
6		GSC13	0.5880E 06
7	POISSON'S RATIO	NUSC12	0.2645E 00
5 6 7 8		NUSC23	0.4294E 00
9		NUSC13	0.2645E 00
10	THERM. EXP. COEF.	CTESC1	-0.1280E-06
11		CTESC2	0.1605E-04
12		CTESC3	0.1605E-04
13	DENSITY	RHOSC	0.5439E-01
14	HEAT CAPACITY	csc	0.1972E 00 0.3311E 03
15 16	HEAT CONDUCTIVITY	KSC1 KSC2	0.3311E 03 0.3918E 01
17		KSC3	0.3918E 01
18	STRENGTHS	SSCIT	0.2307E 06
19	21121101112	SSCIC	0.1568E 06
2ó		SSC2T	0.1026E 05
21		SSC2C	0.2394E 05
22		SSC12	0.9369E 04
23	MOIST. DIFFUSIVITY	DSC1	0.8400E-04
24		DSC2	0.4900E-04
25		DSC3	0.4910E-04
26	MOIST. EXP. COEF.	BTASC1	0.4658E-04
27		BTASC2	0.1319E-02 0.1319E-02
28	FLEXURAL MODULI	BTASC3 ESC1F	0.1319E-02 0.1788E 08
29 30	F LEXUKAL HODGET	ESC2F	0.1153E 07
31	STRENGTHS	SSC23	0.7424E 04
32	JIMB/101115	SSCIF	0.2334E 06
33		SSC2F	0.1796E 05
34		SSCSB	0.1405E 05
35	PLY THICKNESS	TSC	0.5000E-02
36	INTERPLY THICKNESS		0.5215E-04
37	INTERFIBER SPACING	PLSCS	0.5215E-04

Item 5(g)

HYBRID COMPOSITE PROPERTIES; 60/40 SGLA/HMHS/AS--/IMHS BASED ON MICROMECHANICS OF INTRAPLY HYBRID COMPOSITES: ELASTIC AND THERMAL PROPERTIES.

PRIMARY COMPOSITE VOLUME RATIO - 0.600 SECONDARY COMPOSITE VOLUME RATIO - 0.400

1	ELASTIC MODULI	EHC1	0.1144E 08
2 3 4 5 6 7		EHC2	0.1696E 07
3	611777	EHC3	0.1945E 07
4	SHEAR MODULI	GHC12	0.7551E 06
5		GHC23	0.4561E 06
6		GHC13	0.7941E 06
	POISSON'S RATIO	NUHC12	0.2663E 00
8		NUHC23	0.3985E 00
9		NUHC13	0.2689E 00
10	THERM. EXP. COEF.	CTEHC1	0.1603E-05
11		CTEHC2	0.1601E-04
12	B. 201	CTEHC3	0.1634E-04
13	DENSITY	RHOHC	0.6334E-01
14	HEAT CAPACITY	CHC	0.1943E 00
15	HEAT CONDUCTIVITY	KHCl	0.1352E 03
16		KHC2	0.2305E 01
17	A	KHC3	0.2305E 01
18	STRENGTHS	SHCIT	0.2168E 06
19		SHC1C	0.1665E 06
20		SHC2T	0.9915E 04
21 22 23		SHC2C	0.2314E 05
22	MATAR	SHC12	0.1195E 05
23	MOIST. DIFFUSIVITY	DHC1	0.8736E-04
24		DHC2	0.5117E-04
25	MOTOR DUD	DPC3	0.5117E-04
26	MOIST. EXP. COEF.	BTAHC1	0.9858E-04
27 28		BTAHC2	0.8565E-03
20 29	ETTUIDET MARIE	BTAHC3	0.1455E-02
30	FLEXURAL MODULI	EHClF	0.1144E 08
31	STRENGTHS	EHC2F	0.1696E 07
32	SIRENGIAS	SHC23	0.1019E 05
33		SHC1F	0.2355E 06
34		SHC2F	0.1735E 05
35	PLY THICKNESS	SHCSB	0.1793E 05
36	INTERPLY THICKNESS	THC	0.5000E-02
37		PLHC	0.5215E-04
38	INTERFIBER SPACING FIBER VOL. RATIO	PLHCS	0.5215E-04
39	MOISTURE CONTENT	VFH	0.5580E 00
40	MATRIX VOL. RATIO	M	0.0000
	MATATA VOL. RATEO	VMH	0.4320E 00

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Item 6

3-D COMPOSITE STRAIN STRESS TEMPERATURE MOISTURE RELATIONS - STRUCTURAL AXES

	-1-	-2-	-3-	-4-	- 5-	-6-	-70-	- DM-
_	. (07/5:07	-0.5952E-08	-0.2727E-07	0.0000	0.0000	0.3255E-13	0.1102E-05	0.1009E-03
1	0.6976E-07	0.1962E-06	-0.8485E-07	0.0000	0.0000	-0.1464E-11	0.5805E-05	0.3370E-03
2	-0.5952E-08	-0.8485E-07	0.5614E-06	0.0000	0.0000	0.6682E-12	0.2839E-04	0.1859E-02
3	-0.2727E-07	0.0000	0.0000	0.2139E-05	0.5229E-12	0.0000	0.0000	0.0000
4	0.0000	0.0000	0.0000	0.5229E-12	0.1935E-05	0.0000	0.0000	0.0000
5	0.0000 0.3255E-13	-0.1464E-11	0.6682E-12	0.0000	0.0000	0.1622E-05	-0.4330E-10	-0.2425E-08

3-D COMPOSITE STRESS STRAIN RELATIONS - STRUCTURAL AXES

	-1-	-2-	-3-	-4-	-5-	-6-
ı	0.1473E 08	0.8093E 06	0.8377E 06	0.0000	0.0000	0.8960E-01
2	0.8093E 06	0.5499E 07	0.8703E 06	0.0000	0.0000	0.4587E 01
7	0.8377E 06	0.8703E 06	0.1953E 07	0.0000	0.0000	-0.3603E-01
4	0.0000	0.0000	0.0000	0.4676E 06	-0.1263E 00	0.0000
5	0.0000	0.0000	0.0000	-0.1263E 00	0.5167E 06	0.0000
כ		******	0.7/075.03	0.0000	0.0000	0.6164E 06
6	0.8960E-01	0.4587E 01	-0.3603E-01	0.0000	0.000	

MAT9 CARD FOR MSC/NASTRAN SOLID ELEMENTS

G11,G12,G13,G14,G15,G16,G22,G23,G24,G25,G26,G33,G34,G35,G36,G44,G45,G46,G55,G56,G66
0.14731064E 08 0.80927925E 06 0.8377038E 06 0.89597344E-01 0.00000000 0.00000000 0.54987690E 07 0.87032406E 06
0.45865879E 01 0.00000000 0.00000000 0.19533170E 07-0.36027569E-01 0.00000000 0.61636813E 06
0.000000000 0.46757519E 06-0.12633294E 00 0.51670638E 06

Item 7
COMPOSITE PROPERTIES

COMPOSITE PROPERTIES - VALID ONLY FOR CONSTANLINES 1 TO 31 3-D COMPOSITE PROPERTIES ABOUT LINES 33 TO 62 2-D COMPOSITE PROPERTIES ABOUT	T STRU	ERATURE TALAXES ICTURAL	THROUGH THICKNESS
1 RHOC 0.5740E-01 2 TC 0.3000E-01 3 GC11 0.1473E 08 4 CC12 0.8093E 06 5 CC13 0.8377E 06 6 CC22 0.5499E 07 7 CC23 0.87703E 07 9 CC44 0.4676E 06 10 CC55 0.5167E 06 11 CC66 0.6164E 06 12 CTE11 0.1102E-05 13 CTE22 0.5805E-05 14 CTE33 0.2839E-04 15 HK11 0.2138E 03 16 HK22 0.4755E 02 17 HK33 0.3080E 01 18 HHC 0.1975E 00 19 EC11 0.1433E 08 19 EC11 0.1433E 08 20 EC22 0.5505E-05 21 EC33 0.1781E 07 21 EC33 0.1781E 07 22 EC25 0.4676E 06 23 EC31 0.5167E 06 24 EC12 0.6164E 06 25 NUC21 0.8531E-01 26 NUC21 0.8531E-01 27 HUC13 0.3908E 00 28 NUC21 0.3908E 00 28 NUC21 0.3908E 00 28 NUC21 0.3908E 00 28 NUC21 0.3908E 00	2345678901234567890123456789	B2DEC CC112 CCC123 CCC233 ECC122 ECC122 ECC122 ECC122 ECC122 ECC122 ECC122 ECC1212 ECC1213 CCSN1331 CCSN1331 CCSN1332 CCTE212 HK122 HK222 DPC233 DPC1213 DPC233 DPC1213 BTAC2	0.0000 0.1215E 08 0.3746E 06 0.1067E 00 0.4610E 07 0.4055E 01 0.6164E 06 0.1212E 08 0.498E 07 0.6164E 06 0.8126E-01 0.3024E-01 -0.3615E-06 -0.1839E-07 0.6574E-05 0.8818E-06 0.1102E-05 0.5805E-10 0.2138E 03 0.4755E 02 0.5785E-04 0.19778E-02 0.3578E-02 0.3578E-02 0.3578E-02

FORCES	FORCES FORCE DISPLACEMENT RELATIONS						DISPL	T-FORCES	H-FORCES
HX HY HXY	0.3644E 06 0.1124E 05 0.3201E-02	0.1124E 05 0.1383E 06 0.1217E 00	0.3201E-02 0.1217E 00 0.1849E 05	0.0000 0.0000 -0.7276E-11	0.0000 -0.1373E-03 -0.2619E-09	-0.7276E-11 -0.2619E-09 0.0000	UX VY VXPUY	0.0000 0.0000 0.0000	0.0000 0.0000 0.0000
MX MY MXY	0.0000 0.0000 -0.7276E-11	0.0000 -0.1373E-03 -0.2619E-09	-0.7276E-11 -0.2619E-09 0.0000	0.3776E 02 0.7610E 00 0.2667E-07	0.7610E 00 0.3419E 01 0.1014E-05	0.2667E-07 0.1014E-05 0.1248E 01	MXX MYY WXY	0.0000 0.0000 0.0000	0.0000 0.0000 0.0000
				Item 9					
REDUCED	STIFFNESS MATR	IX		REDUCED	BENDING REGIDI	TIES			
0.36441E 0 0.11238E 0 0.32006E-0	5 0.13330E 06	0.32006E-02 0.12165E 00 0.18491E 05		0.37763E 0 0.76104E 0 0.26672E-0	0 0.34186E 01	0.10138E-05			

Item 10

S C M E U S E F U L D A T A F O R F.E. A N A L Y S I S

COMPOSITE THICKNESS FOR F.E. ANALYSIS = 0.30000E-01

PROPERTIES FOR F.E. ANALYSIS E11,E12,E13,E22,E23,E33 PROPERTIES SCALED BY 10**-6
0.32533E-01 -0.67069E-02 -0.29839E-07 0.21747E 00 0.14296E-05 0.16224E 01

BENDING EQUIVALENT PROPERTIES NUCXY, NCYX, ECXX, ECYY, GCXY
0.22261E 00 0.20153E-01 0.16708E 08 0.15126E 07 0.55473E 06

MASTRAN MEMBRANE EQUIVALENT ELASTIC COEFFICIENTS G11,G12,G13,G22,G23,G33
0.12147E 08 0.37462E 06 0.10669E 00 0.46099E 07 0.40551E 01 0.61637E 06

MASTRAN BENDING EQUIVALENT ELASTIC COEFFICIENTS G11,G12,G13,G22,G23,G33
0.16734E 08 0.33824E 06 0.11854E-01 0.15194E 07 0.45056E 00 0.55473E 06

Item 11

	DISP.		COMBINED FORCES					
1	0.2751E-02	-1- 0.2751E-05	-2- -0.2236E-06	-3- 0.9946E-12	0.1818E-12	-5- -0.9021E-11	-6- -0.2356E-16	0.1000E 04
2	-0.2236E-03	-0.2236E-06	0.7249E-05	-0.4765E-10	-0.5895E-11	0.2925E-09	0.1283E-14	0.0000
3	0.9946E-09	0.9946E-12	-0.4765E-10	0.5408E-04	-0.3466E-16	0.2237E-14	-0.1181E-19	0.0000
4	0.1818E-09	0.1818E-12	-0.5895E-11	-0.3466E-16	0.2660E-01	-0.5922E-02	0.4241E-08	0.0000
5	-0.9021E-08	-0.9021E-11	0.2925E-09	0.2237E-14	-0.5922E-02	0.2938E 00	-0.2385E-06	0.0000
6	-0.2356E-13	-0.2356E-16	0.1283E-14	-0.1181E-19	0.4241E-08	-0.2385E-06	0.8012E 00	0.0000

HOTE: THE DISPLACEMENTS ARE REFERENCE PLANE MEMBRANE STRAINS (UX , VY , VXPUY) AND CURVATURES (WXX , WYY , WXY)

PLY HYGROTHERMOMECHANICAL PROPERTIES/RESPONSE

FOR LOAD CONDITIONS
MEMBRANE LOADS NBS(X,Y,XY-M) ARE 1000. 0. 0.
BENDING LOADS NBS(X,Y,XY-M) ARE 0. 0. 0.
QXZ,QYZ AND APPLIED PRESSURES ARE 0. 0. 0. 0.
NOTE: NO MOISTURE OR TEMPERATURE

LAYER PROPERTIES, ROWS-PROPERTY, COLUMNS-LAYER

PLY NUMBER MATERIAL SYSTEM	AS/IMLS AS/IMLS	2 SGLA/HMHS AS/IMHS	3 SGLA/HMHS AS/IMHS	AS/IMLS AS/IMLS	
ORIENTATION	U.U 				
1 KV 2 KFB 3 KFB 4 EM 5 KMB 6 RHOL 7 TL 8 DELTA 9 ILDC 10 ZB 11 ZGC 11 THCS 13 THLC 14 THLS 15 SC112 17 SC12 17 SC12 17 SC12 17 SC12 17 SC23 20 SC33 21 SC44 22 SC55 23 SC64 22 CTE12 25 CTE22 26 CTE31 27 HK11 28 HK22 29 HK33 31 EL11 32 EL23 33 EL33 34 GL23 33 GL12 37 NUL12 38 NUL13	0.2000E-01 0.5500E 00 0.5500E 00 0.4500E 00 0.4500E 00 0.4500E-01 0.5850E-04 0.0000 0.5000E-02 -0.1000E-01 0.0000 0.0000 0.101E 08 0.7797E 06 0.7797E 06 0.7797E 06 0.7797E 06 0.1631E 07 0.8713E 06 0.15470E 06 0.16418E-06 0.16418E-06 0.14418E-06 0.14418E-06 0.14418E-06 0.1418E-06	0.1000E-01 0.5580E 00 0.5524E 00 0.4420E 00 0.4420E 00 0.4376E 00 0.500E-02 0.5215E-04 0.1250E-01 -0.2500E-02 0.1250E-01 -0.2500E-02 0.1571E 01 0.1571E 01 0.1571E 01 0.1571E 01 0.1571E 01 0.1571E 01 0.1571E 01 0.1571E 00 0.1571E 01 0.1571E 01 0.2166E 07 0.7551E 06 0.7551E 06 0.7551E 01 0.12305E 01 0.12305E 01 0.1246E 07 0.1696E 07 0.1696E 07 0.7551E 06 0.7551E 06 0.7551E 06 0.7551E 06 0.7551E 06 0.7551E 06 0.7551E 06	0.1000E-01 0.5580E-00 0.5580E-00 0.4420E-00 0.4376E-01 0.5000E-02 0.5215E-04 0.0000 0.1750E-01 0.2500E-02 0.1750E-01 0.1571E-01 0.1571E-01 0.1571E-01 0.1571E-01 0.1571E-01 0.1571E-01 0.1571E-06 0.2166E-07 0.9537E-06 0.2166E-07 0.9537E-06 0.2166E-07 0.9537E-06 0.2305E-01 0.1601E-04 0.11552E-03 0.2305E-01 0.1943E-03 0.2305E-01 0.1943E-00 0.11696E-07 0.4561E-06 0.7551E-06 0.7551E-06 0.7551E-06 0.7551E-06 0.7551E-06 0.7551E-06 0.7551E-06 0.7551E-06 0.7551E-06 0.7551E-06 0.7551E-06 0.7551E-06 0.7551E-06 0.7551E-06 0.7551E-06	0.2000E-01 0.5500E 00 0.5590E 00 0.4500E 00 0.4410E 00 0.4410E 00 0.2500E-01 0.1000E-01 0.0000 0.2500E-01 0.1000E-01 0.0000 0.0000 0.2101E 08 0.7797E 06 0.71631E 07 0.8713E 07 0.8713E 06 0.5470E 06 0.1418E-06 0.2464E-04 0.3195E 03 0.3702E 01 0.1991E 00 0.1127E 07 0.31238E 06 0.1127E 07 0.31238E 06 0.1127E 07 0.3127E 07 0.3238E 06 0.5470E 06 0.2464E-04 0.3195E 03 0.3702E 01 0.1991E 00 0.1726E 08 0.1127E 07 0.3238E 06 0.5470E 06 0.5470E 06 0.5470E 06 0.5470E 06 0.5470E 06	
41 NUL23 42 NUL32 43 DPL1 44 DPL2 45 DPL3 46 BTAL1 47 BTAL2 48 PTAL3 49 ILMFC 50 TEMPD 51 LSC11T 52 LSC11T 52 LSC12 57 LSC23 58 LSCC23 59 LSCC13 60 LSC12 57 LSC23 61 KSL12AB 62 MDEIE 63 RELROT 64 EPS11 65 EPS22 66 EPS12 67 SIG11 68 SIG22 70 DELFI 71 MFC TGE 73 SIG13 74 SIG23 75 SIG33	0.4821E 00 0.4821E 00 0.4821E 00 0.8600E-04 0.5168E-04 0.5168E-04 0.4981E-0-2 0.1452E-02 0.0000 0.2228E 06 0.8764E 05 0.5106E 04 0.1502E 05 0.5106E 04 0.1502E 04 0.1502E 04 0.1502E 04 0.2751E-02 0.2036E-03 0.9646E 00 0.2751E-02 -0.2236E-03 0.9646E 00 0.2751E-02 -0.2236E-03 0.9646E 00 0.1212E 01 0.5441E-03 0.5441E-03 0.5441E-03 0.121E 01 0.0000 0.1121E 01 0.0000	0.3947E-01 0.3985E 00 0.3985E 00 0.8736E-04 0.5117E-04 0.5117E-04 0.5117E-04 0.9858E-03 0.1455E-02 0.8405E 06 0.1665E 06 0.1665E 06 0.1665E 06 0.1665E 06 0.1915E 05 0.1019E 05 0.1019E 05 0.6196E 05 0.7303E 05	0.3985E 00 0.3985E 00 0.8736E-04 0.5117E-04 0.5117E-04 0.9853E-04 0.8565E-03 0.1455E-02 0.8916E 02 0.2168E 06 0.1665E 06 0.1665E 06 0.1665E 05 0.1195E 06 0.81472 05 0.3925E-03 0.2751E 00 0.1000E 01 -0.2236E-03 0.2751E-08 -0.1329E 04 0.4614E 02 0.6393E 00 0.00000 0.00000 0.00000	0.4821E 00 0.4821E 00 0.4821E 00 0.5168E-04 0.5168E-04 0.5168E-02 0.1452E-02 0.1452E-02 0.8405E 02 0.0000 0.2228E 05 0.5764E 05 0.5006E 05 0.5126E 00 0.5126E 00 0.0000 0.00000 0.00000	

DETAILS OF POISSON RATIO MISMATCH

POISSON"S RATIOS OF THE COMPOSITE
ANUCXY = 0.0813
ANUCYX = 0.0308
ANUCSX = -0.0000
ANUCSY = 0.0000

NO.	THETA	ANULXY	AHULSX	ANULSY	POIDFN	POIDFS
1	0.0	0.2945	0.0000	0.0000	0.2132	-0.0000
2	90.0	0.0395	-0.0000	-0.0000	-0.0418	-0.0000
3	90.0	0.0395	-0.0000	-0.0000	-0.0418	-0.0000
4	0.0	0.2945	0.0000	0.0000	0.2132	-0.0000

Item 14 FREE EDGE STRESSES

1 0.0 0.143E 01 0.199E-01 0.163E-07 0.000 0.116E-01 0.337E-02 0.412E-2 90.0 0.138E 00 -0.339E-01 -0.326E-07 0.298E 00 -0.979E-08 0.803E-03 0.248E-3 90.0 0.138E 00 -0.399E-01 -0.326E-07 0.345E 00 -0.845E-08 0.200E-03 0.248E-3 90.0 0.138E 00 -0.399E-01 -0.326E-07 0.298E 00 -0.574E-08 0.803E-03 0.248E-3 90.0 0.138E 00 -0.399E-01 -0.326E-07 0.345E 00 -0.495E-08 0.200E-03 0.248E-3 90.0 0.138E 00 -0.399E-01 -0.326E-07 0.345E 00 -0.495E-08 0.200E-03 0.248E-3 90.0 0.138E 00 -0.399E-01 -0.326E-07 0.345E 00 -0.495E-08 0.200E-03 0.248E-3 90.0 0.138E 00 -0.399E-01 -0.326E-07 0.345E 00 -0.495E-08 0.200E-03 0.248E-3 90.0 0.138E 00 -0.399E-01 -0.326E-07 0.345E 00 -0.495E-08 0.200E-03 0.248E-3 90.0 0.200E-03	PLY	THETA	SIGXX	SIGYY	SIGXY	YDCAY LENGTH	SIGZY	SIGZZ	SIGZX
, it is a second to the second		90.0 90.0 90.0 90.0 90.0	0.143E 01 0.138E 00 0.138E 00 0.138E 00 0.138E 00 0.138E 01	0.199E-01 -0.399E-01 -0.399E-01 -0.399E-01 -0.399E-01 0.199E-01	0.163E-07 -0.326E-07 -0.326E-07 -0.326E-07 -0.326E-07 0.163E-07	0.000 0.298E 00 0.345E 00 0.298E 00 0.345E 00 0.119E 00	0.116E-01 -0.979E-08 -0.845E-08 -0.574E-08 -0.495E-08 0.116E-01	0.337E-02 0.803E-03 0.200E-03 0.803E-03 0.200E-03 0.337E-02	0.412E-08 0.412E-08 0.248E-08 0.248E-08 0.248E-08 0.248E-08 0.412E-08

NOTE: THE INTERLAMINAR STRESSES ARE BETWEEN PLIES (I-1) AND (I).

NOTE: IF THE PLY NO IS REPEATED THEN THE SECOND ONE INDICATES STRESSES IN THE SECONDARY COMPOSITE.

NOTE: FOR ANGLE PLY LAMINATES SIGYY IS 0. CONSEQUENTLY SIGZY AN D SIGZZ ARE COMPUTED AS ZERO.

TO OBTAIN NONTRIVIAL SIGZY AND SIGZZ, ONE MUST SPECIFY A THIN INTERPLY LAYER.

THE INTERPLY LAYER THICKNESS MAY BE OBTAINED FROM THE PLY PROPERTY TABLE.

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Item 15(a)

MICROSTRESSES

(NOTE: ROWS-PROPERTY, COLUMNS-LAYER)

		2	3	4	
PLY NUMBER		CCLACUMUE	SCI AZHMHS	AS/IMLS	
MATERIAL SYSTEM	AS/IMLS	SGLAZININS	AC / TMUS	AS/IMIS	
	AS/IMLS	ASVIMHS	A3>11///3	0.0	
ORTENTATION	0.0	90.0	90.0	0.0	
1 CM11	n 1381F 04	-0.8714E 02	-0.8714E 02	0.1381E 04	
1 31111	0 0000	-0 5809F 02	-0.5809E 02	0.0000	
1 51111	0.000	0 15365 06	n 1534E 04	0.2669E 03	
2 SM1T	U.2669E U3	0.15546 04	0 1561F 04	0.0000	
2 SM1T	0.0000	0.15615 04	-0 1661E 06	0 8564F 05	
3 SF1L	0.8564E 05	-0.1441E 04	-0.14415 04	0.000	
3 SF1L	0.0000	-0.3602E 04	-0.36026 04	-0.2185E 03	
4 SFIT	-0.2185E 03	-0.4087E 03	-0.4087E 03	-0.21656 03	
4 SFIT	0.0000	-0.2406E 04	-0.2406E 04	0.000	
C CM341	0 1595F 03	-0.7294E 01	-0.7294E 01	0.1595E US	
5 SM2AL 5 SM2AL 6 SM2AT	0.13/32.03	-0.4862E 01	-0.2406E 04 -0.7294E 01 -0.4862E 01 0.1706E 04 0.2324E 04	0.0000	
5 SMZAL	0.0000	0 17065 06	0.1706E 04	0.3445E 03	
6 SMZAT	0.3445E US	0.1706E 04 0.2324E 04	0 2324F 04	0.0000	
6 SM2AT	0.0000	U.2324E U4	0.2324E 04 0.4632E 03	-0.1662E 05	
7 SM2BL	-0.1662E 05	0.4632E 03	0.46322 03	0.0000	
7 SM2BL	0.0000	0.4314E 03		0.0000	
8 SM2BT	0.7763E 03	0.3858E 04	0.3858E 04	0.7763E 03 0.0000	
8 SM2BT	0.000	0.7882E 04	0.7882E 04	0.0000	
8 511201	-0 1662F 05	0.4632E 03	0.4632E 03	-0.1662E 05	
9 SF2BL	-0.10022 03	0.4314E 03	0.4314E 03	0.0000	
9 SF2BL	0.0000	0.3858E 04	0.3858E 04	0.7763E 03	
10 SF2BT	U.//63E U3	0.7882E 04	0.7882E 04	0.0000	
10 SF2BT	0.0000	0.78825 04	-0.7294E 01	0.0000 0.7763E 03 0.0000 0.1595E 03	
11 SM3AL	0.1595E 03	-0.7294E 01	0.72746 01	0.0000	
II SM3AL	0.0000	-0.4862E 01	V. 10055	-0.2126E 02	
12 SM3AT	-0.2126E 02	-0.9887E 02	-0.9887E 02		
12 SM3AT	0.0000	-0.6591E 02	-0.6591E 02	0.0000	
12 JIIJAI	-0 1662F 05	0.4632E 03 0.4314E 03	0.4632E 03	-0.1662E 05	
13 SM3BL	0.10022.05	0 4314F 03	0.4314E 03	0.0000 0.2316E 03 0.0000	
13 SM3BL	0.0000	0 1407E 04	0 1607E 04	0.2316E 03	
14 SM3BT	0.23162 03	0.1607E 04 0.1497E 04	A 1/07F 06	0.0000	
14 SM3BT	0.0000	0.14775 07	0.4632E 03	-0.1662E 05	
15 SF3BL	-0.1662E 05	0.4632E 03	0.40322 03	0.000	
15 SF3BL	0.0000	0.43146 03	0.43145 03	0 2316F 03	
16 SF3BT	0.2316E 03	0.1607E 04	0.160/5 04	0.23102.03	
16 SF3BT	0.0000	0.1497E 04	0.149/E 04	0.0000	
17 SM12A	n 2137E-03	-0.2348E-02	-0.2348E-02	0.213/E-03	
17 SHIZE	0.000	-0.2439E-02	-0.2439E-02	0.0000	
17 SM12A	0 (5025-03	-0 6382F-02	-0.6382E-02	0.6592E-03	
18 SM12B	0.65926-05	_n 0965E-02	-0.9945E-02	0.0800	
18 SM12B	0.000	0.77736 02	-0 6382F-02	0.6592E-03	
19 SF12B	0.6592E-03	-0.63626-02	-0.000EE-02	0.0000	
19 SF12B	0.0000	-0.9945E-UZ	-0.77436-02	0 2137F-03	
20 SM13A	0.2137E-03	-0.2348E-02	-U.2346E-U2	0.213,2000	
20 SM13A	0.0000	-0.2439E-02	-0.2439E-02	0.0000	
21 SM13B	0 6592E-03	-0.6382E-02	-0.6382E-02	0.65925-03	
21 311130	0.0000	-0.9945E-02	-0.9945E-02	0.0000	
21 SM13B	n 4592F-03	-0.6382E-02	-0.6382E-02	0.6592E-03	
22 SF13B	0.05/2000	-n 9945E-02	-0.9945E-02	0.000	
22 SF133	0.0000	0.000	0.0000	0.0000	
23 SM23A	0.0000	0.0000	0.0000	0.0000	
23 SM23A	0.0000	0.0000	0.0000	0.000	
24 SM23B	0.0000	0.000	0.0000	0.000	
24 SM23B	0.0000	0.0000	0.0000	0.0000	
25 SF23B	0.0000	0.0000	0.0000	0.0000	
25 SF23B	AS/IMLS 0.0 0.1381E 04 0.2669E 03 0.00000 0.8564E 05 0.00000 0.1595E 03 0.00000 0.3445E 03 0.00000 0.7763E 03 0.00000 0.1595E 03 0.00000 0.2316E 03 0.00000 0.2316E 03 0.00000 0.2316E 03 0.00000 0.2316E 03 0.00000 0.2317E-03 0.00000 0.2137E-03 0.00000 0.6592E-03 0.00000 0.6592E-03 0.00000 0.6592E-03 0.00000 0.6592E-03 0.00000 0.6592E-03 0.00000 0.00000 0.00000 0.00000 0.00000 0.00000	0.0000	0.0000	-0.1662E 05 0.0000 0.2316E 03 0.0000 0.2137E-03 0.0000 0.6592E-03 0.0000 0.6592E-03 0.0000 0.6592E-03 0.0000 0.6592E-03 0.0000 0.6592E-03 0.0000 0.6592E-03	

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NOTATION: S --- STRESS (SIGMA)

M --- MATRIX AND F --- FIBER

1,2,3 --- DIRECTIONS FOR STRESSES - PLY MATERIAL AXES

L,T --- DIRECTIONS OF PLY STRESSES

A --- REGION CONTAINING NO FIBERS

B --- REGION CONTAINING FIBERS AND MATRIX

EXAMPLE: SM2AL STANDS FOR TRANSVERSE NORMAL STRESS

IN REGION A DUE TO A LOAD IN THE LOGITUDINAL

DIRECTION
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Item 15(b) MICROSTRESS INFLUENCE COEFFICIENTS

THE FOLLOWING	ARE THE MICRO	STRESS INFLUENCE	COEFFICIENTS	FOR THE PRIMARY	COMPOSITE AS-	-/IMLS SYST	EM
INF. COEF.	SIGMAII LBS/SQ.IN	SIGMAZZ LUS/SQ.IN	SIGMA12 LBS/SQ.IN	SIGMA13 LBS/SQ.IN	SIGMA23 LBS/SQ.IN	DELTA T 1 DEG F	DELTA M
1 SM11 2 SM22A 3 SM22B 4 SM12B 6 SM12B 6 SM13A 7 SM13B 8 SM23A 9 SM23A 10 SM33A 11 SM33B 11 SM33B 11 SM33B 11 SM33B 11 SF22B 14 SF23B 15 SF12 17 SF23B	0.0290 0.0033 -0.3484 0.0000 0.0000 0.0000 0.0000 0.0000 0.0003 -0.3484 1.7955 -0.3484 -0.3484 -0.3484	0.4615 0.5183 1.1678 0.0000 0.0000 0.0000 0.0000 0.0000 0.0000 0.0200 0.3484 1.1678 0.3484 0.3484 0.0000	0.000 0.0000 0.0000 0.3927 1.16 0.0000 0.0000 0.0000 0.0000 0.0000 0.0000 0.0000 0.0000	0.0000 0.0000 0.0000 0.0000 0.0000 0.3927 1.2116 0.0000 0.0000 0.0000 0.0000 0.0000 0.0000 0.0000 0.0000	0.0000 0.0000 0.0000 0.0000 0.0000 0.0000 0.5475 1.4043 0.0000 0.0000 0.0000 0.0000 0.0000	-28.4291 -16.1814 -5.6376 0.0000 0.0000 0.0000 0.0000 0.0000 0.0000 -16.1814 -5.6376 -5.6376 5.6376 0.0000 0.0000	-1975.0911 -1274.0061 443.8653 0.0000 0.0000 0.0000 0.0000 0.0000 -1274.0061 443.8653 1544.1631 443.8633 443.8633 0.0000 0.0000

MOTE: TO OBTAIN THE ABSOLUTE VALUE OF THE MICROSTRESSES THE INF. COEF. SHOULD BE MULTIPLIED BY THE APPROPRIATE STRESSES OR THE TEMPERATURE GRADIENT OR THE MOISTURE CONTENT.

EXPLANATION: SM22B , FOR EXAMPLE, STANDS FOR TRANSVERSE HORMAL STRESS INFLUENCE COEFFICIENT IN REGION B

MICROSTRESS INFLUENCE COEFFICIENTS

THE FOLLOWING	ARE THE MICRO	STRESS INFLUENC	E COEFFICIENTS	FOR THE PRIMARY	COMPOSITE SGL	AZHMHS SYST	EM
INF. COEF.	SIGMA11 LBS/SQ.IN	SIGMA22 LBS/SQ.IN	SIGMA12 LBS/SQ.IN	SIGMA13 LBS/SQ.IN	SIGMA23 LBS/SQ.IN	DELTA T 1 DEG F	DELTA M
1 SM11 2 SM22A 3 SM22B 4 SM12B 6 SM13A 7 SM13B 8 SM23A 9 SM23A 10 SM13A 11 SM13A 11 SM13A 11 SM33A 11 SM33A 11 SM33A 11 SM33A 11 SM33A 11 SM22B 14 SF211 13 SF22B 14 SF33B 15 SF13B	0.0655 0.0655 0.03484 0.0000 0.0000 0.0000 0.0000 0.0000 0.0055 -0.3424 1.0837 -0.3484 -0.3484 0.0000	0.3325 0.3698 0.8363 0.0000 0.0000 0.0000 0.0000 0.0000 0.0000 0.0000 0.3484 0.3484 0.8363 0.8363 0.0000 0.0000	0.0000 0.0000 0.0000 0.3643 0.9902 0.0000 0.0000 0.0000 0.0000 0.0000 0.0000 0.0000 0.0000	0.0000 0.0000 0.0000 0.0000 0.3443 0.9902 0.0000 0.0000 0.0000 0.0000 0.0000 0.0000 0.0000	0.000 0.000 0.000 0.000 0.000 0.000 0.000 0.6091 2.0423 0.000 0.000 0.000 0.000 0.000 0.000 0.000	-28.7981 -17.9927 6.2687 0.0000 0.0000 0.0000 0.0000 0.0000 0.0000 -17.9927 6.2687 -14.8484 6.2687 6.2687 0.0000 0.0000	-2926.0596 -2357.6494 821.4043 0.0000 0.0000 0.0000 0.0000 -2357.6494 821.4043 1222.4413 821.4043 821.4043 0.0000 0.0000

NOTE: TO OBTAIN THE ABSOLUTE VALUE OF THE MICROSTRESSES THE INF. COEF. SHOULD BE MULTIPLIED BY THE APPROPRIATE STRESSES OR THE TEMPERATURE GRADIENT OR THE MOISTURE CONTENT.

EXPLANATION: SM22B , FOR EXAMPLE, STANDS FOR TRANSVERSE NORMAL STRESS INFLUENCE COEFFICIENT IN REGION B

MICROSTRESS INFLUENCE COEFFICIENTS

THE FOLLOWING	ARE THE MICRO	STRESS INFLUENCE	COEFFICIENTS	FOR THE SECONDARY	COMPOSITE	AS/IMHS	SYSTEM
INF. COEF.	SIGMA11 LBS/SQ.IN	SIGMA22 LBS/SQ.IN	SIGMA12 LBS/SQ.IN	SIGMA13 LBS/SQ.IN	SIGMA23 LBS/SQ.IN	DELTA T 1 DEG F	DELTA M 1%
1 SM11 2 SM22A 3 SM22B 4 SM12B 5 SM13B 5 SM13B 7 SM13B 8 SM23A 7 SM23B 10 SM33B 11 SM33B 12 SF11 13 SF22B 14 SF33B 15 SF22B 14 SF33B 17 SF23B	0.0437 -0.3245 -0.0000 -0.0000 -0.0000 -0.0000 -0.0000 -0.0037 -0.3245 -2.7093 -0.3245 -0.3245 -0.3265	0.3384 0.5036 1.7084 0.0000 0.0000 0.0000 0.0000 0.0000 0.0143 0.3245 -0.5215 1.7084 0.3245 0.0000 0.0000	0.0000 0.0000 0.0000 0.3784 1.5430 0.0000 0.0000 0.0000 0.0000 0.0000 0.0000 0.0000 0.0000 0.0000	0.0000 0.0000 0.0000 0.0000 0.0000 0.0000 0.0000 0.0000 0.0000 0.0000 0.0000 0.0000 0.0000	0.0000 0.0000 0.0000 0.0000 0.0000 0.0000 0.4060 1.0551 0.0000 0.0000 0.0000 0.0000 0.0000 0.0000 0.0000	-17.1987 -9.9952 3.2438 0.0000 0.0000 0.0000 0.0000 -9.9952 3.2438 66.7289 3.2438 0.0000 0.0000	-1950.7063 -1571.7661 510.0889 0.0000 0.0000 0.0000 0.0000 0.0000 -1571.7661 510.0889 3056.1045 510.0889 0.0000 0.0000

NOTE: TO OBTAIN THE ABSOLUTE VALUE OF THE MICROSTRESSES THE INF. COEF. SHOULD BE MULTIPLIED BY THE APPROPRIATE STRESSES OR THE TEMPERATURE GRADIENT OR THE MOISTURE CONTENT.

EXPLANATION: SM22B , FOR EXAMPLE, STANDS FOR TRANSVERSE NORMAL STRESS INFLUENCE COEFFICIENT IN REGION B

Item 16

STRESS CONCENTRATION FACTORS (AROUND A CIRCULAR HOLE)

NOTE: K1XX --> STRESS CONCENTRATION FACTOR DUE TO SIGMA XX
K1YY --> STRESS CONCENTRATION FACTOR DUE TO SIGMA YY
K1XY --> STRESS CONCENTRATION FACTOR DUE TO SIGMA XY
LAYUP --> 0 90 90 0

THETA	K1XX	KlYY	KlXY	THETA	K1XX	Klyy	KlXY
0.0	-0.6160	3.8562	0.0000	180.0	-0.6160	3.8562	0.0002
5.0	-0.5709	3.6729	-1.1975 -2.1209	185.0 190.0	-0.5709 -0.4572	3.6729 3.2155	-2.1208
10.0 15.0	-0.4572 -0.3168	3.2156 2.6650	-2.1209	195.0	-0.3168	2.6649	-2.6885
20.0	-0.3168	2.1516	-2.9777	200.0	-0.1799	2.1515	-2.9777
25.0	-0.0569	1.7253	-3.1020	205.0	-0.0570	1.7252	-3.1020
30.0	0.0532	1.3875	-3.1493	210.0	0.0532	1.3875	-3.1493
35.0	0.1566	1.1225	-3.1741	215.0	0.1566	1.1225	-3.1741
40.0	0.2613	0.9117	-3.2080	220.0	0.2613	0.9116	-3.2080
45.0	0.3764	0.7383	-3.2701	225.0	0.3764	0.7382	-3.2701
50.0	0.5138	0.5879	-3.3730	230.0	0.5137	0.5879 0.4472	-3.3730 -3.5262
55.0	0.6898	0.4473	-3.5263	235.0	0.6898 0.9301	0.3018	-3.7367
60.0	0.9302	0.3019 0.1331	-3.7367 -4.0029	240.0 245.0	1.2763	0.1331	-4.0028
65.0	1.2764 1.7980	-0.0864	-4.2958	250.0	1.7979	-0.0865	-4.2957
70.0 75.0	2.6025	-0.3968	-4.5006	255.0	2.6023	-0.3969	-4.5006
80.0	3.7983	-0.8378	-4.2743	260.0	3.7980	-0.8379	-4.2744
85.0	5.2286	-1.3548	-2.9009	265.0	5.2283	-1.3549	-2.9013
90.0	5.9765	-1.6233	-0.0001	270.0	5.9765	-1.6233	-0.0008
95.0	5.2287	-1.3549	2.9007	275.0	5.2290	-1.3550	2.9003
100.0	3.7984	-0.8379	4.2743	280.0	3.7987	-0.8380	4.2741
105.0	2.6026	-0.3969	4.5007	285.0	2.6028	-0.3970	4.5007 4.2958
110.0	1.7980	-0.0865	4.2958	290.0	1.7982 1.2765	-0.0865 0.1330	4.0030
115.0	1.2764	0.1330	4.0029	295.0 300.0	0.9303	0.3018	3.7368
120.0	0.9302 0.6899	0.3018 0.4472	3.7367 3.5263	305.0	0.6899	0.4472	3.5263
125.0 130.0	0.5138	0.5879	3.3730	310.0	0.5138	0.5878	3.3731
135.0	0.3764	0.7382	3.2702	315.0	0.3764	0.7382	3.2702
140.0	0.2613	0.9116	3.2081	320.0	0.2613	0.9116	3.2081
145.0	0.1567	1.1225	3.1741	325.0	0.1567	1.1224	3.1741
150.0	0.0532	1.3875	3.1493	330.0	0.0532	1.3874	3.1493
155.0	-0.0569	1.7252	3.1021	335.0	-0.0569	1.7251	3.1021 2.9778
160.0	-0.1799	2.1515	2.9777	340.0	-0.1798 -0.3168	2.1514 2.6647	2.9778
165.0	-0.3168	2.6648	2.6886 2.1210	345.0 350.0	-0.3168	3.2153	2.1211
170.0 175.0	-0.4571 -0.5709	3.2155 3.6728	1.1976	355.0	-0.5709	3.6728	1.1979
1/3.0	-0.3707	3.0720					

Item 17
LOCATIONS OF PROBABLE DELAMINATION

DECULTS FOR BLY NO.			
RESULTS FOR PLY NO. 1 CRITERION			
	RANGE		LOCATION *
MAX OF KIXX*(NUCRT-NULR MAX OF KIYY*(NUCRT-NULR MAX OF KIYY*(NUCRT-NULR MAX OF KIXX*(NUCRT-NULR MAX OF KIYY*(NUCRT-NULR MAX OF KIYY*(NUCRT-NULR MAX OF KIXX*(NUCRT-NULR MAX OF KIYX*(NUCRT-NULR MAX OF KIYX*(NUCRT-NULR MAX OF KIXX*(NUCRT-NULR MAX OF KIXX**)	7) 0.0 90.0 7) 0.0 90.0 7) 0.0 90.0 7) 90.0 180.0 7) 90.0 180.0 7) 90.0 270.0 7) 180.0 270.0 7) 180.0 270.0 7) 180.0 270.0 180.0 270.0 1270.0 0.0 1270.0 0.0	0.588 0.822 1.411 0.588 0.822 1.411 0.588 0.822 1.411 0.588	75.0 0.0 60.0 105.0 180.0 120.0 255.0 180.0 240.0 285.0 0.0 300.0
RESULTS FOR PLY NO. 2	ORIENTATION 90.0 M	ATERIAL SGLA	HMHS ASIMHS
CRITERION	RANGE		LOCATION *
MAX OF KIXX*(NUCRT-NULRT MAX OF KIXY*(NUCRT-NULRT MAX OF KIXY*(NUCRT-NULRT MAX OF KIXX*(NUCRT-NULRT MAX OF KIYX*(NUCRT-NULRT MAX OF KIYX*(NUCRT-NULRT MAX OF KIXX*(NUCRT-NULRT MAX OF KIYX*(NUCRT-NULRT MAX OF KIYX*(NUCRT-NULRT MAX OF KIXX*(NUCRT-NULRT MAX OF KIXX*(NUCRT NULRT MAX OF KIXX*(NUCRT NULRT NULR	0.0 90.0 0.0 90.0 0.0 90.0) 90.0 180.0) 90.0 180.0) 90.0 180.0) 180.0 270.0) 180.0 270.0) 180.0 270.0) 270.0 0.0) 270.0 0.0	1.407 1.087 1.476 1.407 1.087 1.476 1.407 1.087 1.476 1.407	90.0 15.0 25.0 90.0 165.0 155.0 270.0 195.0 205.0 270.0 335.0
RESULTS FOR PLY NO. 3	ORIENTATION 90.0 M	ATERIAL SGLAP	MHS ASIMHS
CRITERION	RANGE		LOCATION *
MAX OF KIXX*(NUCRT-NULRT MAX OF KIYY*(NUCRT-NULRT MAX OF KIXY*(NUCRT-NULRT MAX OF KIXY*(NUCRT MAX OF KIXY*(NUCRT-NULRT MAX OF KIXY*(NUCRT-NULRT MAX OF KIXY*(NUCRT-NULRT MAX OF KIXY*(NUCRT MAX OF KIXY*(NUCRT MAX OF KIXY*)	0.0 90.0 0.0 90.0 0.0 90.0 0.0 180.0 0.0 180.0 0.0 180.0 0.0 180.0 0.180.0 270.0 0.180.0 270.0 0.180.0 270.0 0.180.0 270.0 0.270.0 0.0 0.270.0 0.0	1.407 1.087 1.476 1.407 1.087 1.487 1.407 1.087 1.407 1.087 1.407 1.407	90.0 15.0 25.0 90.0 165.0 155.0 270.0 195.0 205.0 275.0 345.0
RESULTS FOR PLY NO. 4			
CRITERION	RANGE		LOCATION *
MAX OF KIXXXKNUCRT-NULRT MAX OF KIYYXKNUCRT-NULRT MAX OF KIXYXKNUCRT-NULRT MAX OF KIXXXKNUCRT-NULRT MAX OF KIXYXKNUCRT-NULRT MAX OF KIXYXKNUCRT-NULRT MAX OF KIXXXKNUCRT-NULRT MAX OF KIXYXKNUCRT-NULRT MAX OF KIXXXKNUCRT-NULRT MAX OF KIXYXKNUCRT-NULRT MAX OF KIXXXKNUCRT-NULRT MAX OF KIXXXXXXXXXXXXXXXXXXXXXXXXXXXXXXXXXXXX	0 90.0 180.0 180.0 270.0 180.0 270.0 180.0 270.0 270.0 0.0 270.0 0.0 270.0 0.0	0.588 0.822 1.411 0.588 0.822 1.411 0.588 0.822 1.411 0.588 0.822 1.411	120.0 255.0 180.0 240.0 285.0 0.0 300.0
K1XY -+> 5TRE5S (ONCENTRATION FACTOR ONCENTRATION FACTOR SON RATIO IN R AND E POISSON RATIO IN RADIAL AND THE TANK	R DUE TO SIGM T AXES R AND T AXES SENTIAL DIREC	A XY Tions)

Item 18
PLY STRESS AND STRAIN INFLUENCE COEFFICIENTS ARRAYS

PLY NO	. MATERIAL SYSTEM	THETA	RESPONSE	XX (UNIT I	NY DAD L	HXY B./INCH)	MX (UNIT M	MY IOMENTLB.	MXY IN/INCH)	DELTAT (1 DEG F	DELTAM) (1 %)
1	AS/IMLS	0.0	EPS11 EPS22 EPS12 SIG12 SIG22 SIG12	2.7511 -0.2236 0.0000 47.6932 0.6647 0.0000	-0.2236 7.2490 -0.0000 -1.4628 8.1391 -0.0000	0.0000 -0.0000 54.0302 0.0000 -0.0001 29.5831	266.0017 -59.2160 0.0000 4598.8906 21.6664 0.0000	-59.2159 2938.3235 -0.0024 -47.6819 3309.6074 -0.0013	0.0000 -0.0024 8011.9414 -0.0001 -0.0027 4382.7227	1.1801 5.8164 -0.0000 11.7478 -20.9790 -0.0000	105.0192 342.4932 -0.0023 588.3518 -1238.7244 -0.0012
2	SGLA/HMHS AS/IMHS										
			EPS11 EPS22 EPS12 SIG11 SIG22 SIG12	-0.2236 2.7511 -0.0000 -1.3294 4.6136 -0.0000	7.2490 -0.2236 0.0001 83.7219 2.9257 0.0001	0.0000 -0.0001 -54.0802 0.0002 -0.0001 -40.8337	-14.8040 66.5005 -0.0002 -140.8320 107.2302 -0.0002	8487.6133	0.0019 -0.0025 -2002.9873 0.0213 -0.0034 -1512.3735	5.8164 1.1801 0.0001 41.9581 -23.4957 0.0000	342.4929 105.0192 0.0029 2477.4478 -1176.7065 0.0022
3	SGLA/HMHS AS/IMHS										
			EPS11 EPS22 EPS12 SIG11 SIG22 SIG12	-0.2236 2.7511 -0.0000 -1.3294 4.6136 -0.0000	7.2490 -0.2236 0.0001 83.7219 2.9257 0.0001	0.0000 -0.0001 -54.0802 0.0002 -0.0001 -40.8337	14.8040 -66.5004 0.0002 140.8316 -107.2300 0.0002	-309.9319	-0.0019 0.0025 2002.9846 -0.0213 0.0034 1512.3713	5.8164 1.1801 0.0001 41.9580 -23.4957 0.0000	342.4927 105.0192 0.0029 2477.4451 -1176.7065 0.0022
4	AS/IMLS	0.0	EPS11 EPS22 EPS12 SIG11 SIG22 SIG12	2.7511 -0.2236 9.0000 47.6932 0.6647 0.0000	-0.2236 7.2490 -0.0000 -1.4628 8.1391 -0.0000	0.0000 -0.0000 54.0802 0.0000 -0.0001 29.5831	-0.0000 -4598.8906	59.2159 -2938.3228 0.0024 47.6819 -3309.6067 0.0013	0.0024 -8011.9414 0.0001	1.1801 5.8164 -0.0000 11.7478 -20.9790 -0.0000	105.0192 342.4924 -0.0023 588.3518 -1238.7251 -0.0012

NOTE: STRAINS ARE IN MICRO INCH/INCH. STRESSES ARE IN POUNDS/INCH SQ.

EXPLANATION OF THE INFLUENCE COEFFICIENTS

NX,NY AND NXY ARE UNIT LOADS IN LB/INCH. MX,MY AND MXY ARE UNIT MOMENTS IN LB.IN/INCH. DELTAT IS A UNIT TEMP. DIFF. AND DELTAM IS A UNIT PERCENTAGE OF MOISTURE CONTENT. TO OBTAIN RESPONSE R FOR A GENERAL APPLIED LOAD VECTOR F USE THE FOLLOWING EQUATION:

 $(R) = (AINF) \times (F)$

NOTE: R IS A 6X1 COLUMN VECTOR DEFINED BY

(R) = (EPS11 EPS22 EPS12 SIG11 SIG12 SIG12)
F IS A 8X1 COLUMN VECTOR DEFINED BY

(F) = (NX NY NXY MX MY MXY DELTAT DELTAM. AINF IS A (6X8) MATRIX CONTAINING THE INFLUENCE COEFFICIENTS ARRAYS.

PLY STRESS INFLUENCE COEFFICIENTS ARRAYS

			_							 	
PLY NO). MATERIAL SYSTEM	THETA	RESPONSE	NX (UNIT L SCALE F		NXY 3./INCH) 33.333	MX (UNIT MO SCALE F	MY MENTLB.I ACTOR = 66 (6/TC*	66.668	DELTAT (1 DEG F) 13.354	DELTAM (1 %) 1223.138
1	AS/IMLS	0.0	SIG11 SIG22 SIG12	1.4308 0.0199 0.0000	-0.0439 0.2442 -0.0000	0.0000 -0.0000 0.8875	0.6898 0.0032 0.0000	-0.0072 0.4964 -0.0000	-0.0000 -0.0000 0.6574	0.8797 -1.5709 -0.0000	0.4810 -1.0127 -0.0000
2	SGLA/HMHS AS/IMHS	90.0	SIG11 SIG22	-0.0399 0.1384	2.5117 0.0878	a.0000 -0.0000	-0.0211 0.0161 -0.0000	1.2731 0.0465 0.0000	3.0000 -0.0000 -0.2269	3.1419 -1.7594 0.0000	2.0255 -0.9620 0.0000
3	SGLA/HMHS AS/IMHS	90.0	SIG12	-0.0000	0.0000	-1.2250	-0.0000	0.0000			
			SIG11 SIG22 SIG12	-0.0399 0.1384 -0.0000	2.5117 0.0878 0.0000	0.0000 -0.0000 -1.2250	0.0211 -0.0161 0.0000	-1.2731 -0.0465 -0.0000	-0.0000 0.0000 0.2269	3.1419 -1.7594 0.0000	2.0255 -0.9620 0.0000
4	AS/IMLS	0.0		1.4308 0.0199 0.0000	-0.0439 0.2442 -0.0000	0.0000 -0.0000 0.8875	-0.6898 -0.0032 -0.0000	0.0072 -0.4964 0.0000	0.0000 0.0000 -0.6574	0.8797 -1.5709 -0.0000	0.4810 -1.0127 -0.0000

NOTE: THE MEMBRANE STRESSES ARE NORMALIZED W.R.T THE AVERAGE STRESS DUE TO UNIT LOAD IN AN EQUIVALENT HOMOGENEOUS SECTION. THE BENDING STRESSES ARE NORMALIZED W.R.T THE MAXIMUM STRESS DUE TO UNIT MOMENT. THE TEMPERATURE AND MOISTURE STRESSES ARE NORMALIZED W.R.T THE AVERAGE STRESSES DUE TO UNIT TEMPERATURE DIFFERENCE AND UNIT PERCENTAGE OF MOISTURE. TO OBTAIN THE ABSOLUTE VALUES OF THE STRESSES THE INFLUENCE COEFFICIENTS SHOULD BE MULTIPLIED BY THE CORRESPONDING LOADS TO OBTAIN STRESSES IN THE PLIES.

Item 19 LAMINATE FAILURE STRESS ANALYSIS

	LAMINA	TE FAILURE	STRESSES BASE	JP>	0 90 9 FIRST PLY F	0 0 AILURE CRITERIA	(NO TEMPERATURE	OR MOISTURE STRESSES	e)
PLY NO	D.	= 1		0.00			-IMLS ASIMLS		
LOADS	•	SL11T 222.7741 KSI	SL11C 87.6392 KSI	2	SL22T 5.0065 KSI	SL22C 15.0194 KSI	SL12S 5.1261 KSI	FAIL. LOAD KSI	MODE
SCXXT SCXXC SCYYT SCYYC SCXYS	MIN (MIN (- MIN (155.699 -155.699 -5076.305 5076.305 0.000	-61.252 61.252 1997.011 -1997.015 0.000		251.063 -251.063 20.504 -20.504 ******	-753.188 753.188 -61.511 61.511 *******	0.000 0.000 0.000 0.000 0.000	155.699 61.252 20.504 61.511	SL11T SL11C SL22T SL22C

	DANIMATE FAILURE	SIKESSES BASED UPON	FIRST PLY FA	LURE CRITERIA (NO	TEMPERATURE OR	MOISTURE STRESSES)	
PLY NO		THETA = 90.00	MATERIAL				
LOADS	SL11T 216.8321 KSI	SL11C 166.5112 KSI	SL22T 9.9151 KSI	SL22C 23.1353 KSI	SL12S 11.9513 KSI	FAIL. LOAD	MODE
SCXXI SCXYI SCXYI SCXYI SCXYI	MIN (5436.801 MIN (86.330 MIN (-86.330	4175.063 -4175.063 -66.295 66.295 *******	71.638 -71.638 112.967 -112.967 *******	-167.155 167.155 -263.589 263.589 ********	0.000) 0.000) ******** ******** 9.756)	71.638 167.155 86.330 66.295 9.756	SL22T SL22C SL11T SL11C SL12S

LAT	INATE FAILURE	STRESSES BASED UPON	FIRST PLY FA	ILURE CRITERIA (NO	TEMPERATURE O	R MOISTURE STRESSES)	
PLY NO.	= 3	THETA = 90.00					
LOADS	SL11T 216.8321 KSI	SL11C 166.5112 KSI	SL22T 9.9151 KSI	SL22C 23.1353 KSI	SL12S 11.9513 KSI	FAIL. LOAD KSI	MODE
SCXXT MIN SCXXC MIN SCYYT MIN SCYYC MIN SCXYS MIN	(5436.801 (86.330	4175.063 -4175.063 -66.295 66.295 ******	71.638 -71.638 112.967 -112.967 *******	-167.155 167.155 -263.589 263.589 ********	0.000) 0.000) ******** ********* 9.756)	71.638 167.155 86.330 66.295 9.756	SL22T SL22C SL11T SL11C SL12S

MOTE: "****** IMPLIES -"NOT APPLICABLE"-

LAMI	NATE FAILURE	STRESSES BASED U	> 0 90 90 JPON FIRST PLY FA	0 ILURE CRITERIA (NO T	EMPERATURE OF	MOISTURE STRESSES)	
PLY NO.	= 4			SYSTEM = ASIMLS			
LOADS	SL11T 222.7741 KSI	SL11C 87.6392 KSI	SL22T 5.0065 KSI	SL22C 15.0194 KSI	SL12S 5.1261 KSI	FAIL. LOAD	MODE
SCXXT MIN SCXXC MIN SCXYC MIN SCYYC MIN SCXYS MIN SCXXS MIN SCXXS MIN SCXXS MIN SCXXS	-155.699 -5076.309 5076.309	-61.252 61.252 1997.017 -1997.017 0.000	251.062 -251.062 20.504 -20.504 *******	-753.187 753.187 -61.511 61.511 ********	0.000) 0.000) 0.000) 0.000) 5.776)	155.699 61.252 20.504 61.511 5.776	SL11T SL11C SL22T SL22C SL22C SL12S

SUMMARY

LAMINATE FAILURE STRESS ANALYSIS - (NO TEMPERATURE OR MOISTURE STRESSES)
(BASED UPON FIRST PLY FAILURE)

LOAD TYPE	STRESS KSI	FAILURE MODE	PLY NO.	THETA	MATERIAL	SYSTEM
SCXXT SCXXC SCYYT SCYYC SCXYS	71.638 61.252 20.504 61.511 5.776	SL22T SL11C SL22T SL22C SL12S	3 4 1 1 4	90.0 0.0 0.0 0.0 0.0	ASIMLS ASIMLS ASIMLS	ASIMHS ASIMLS ASIMLS ASIMLS ASIMLS

LAMINATE FAILURE STRESS ANALYSIS - (NO TEMPERATURE OR MOISTURE STRESSES)
(BASED UPON FIBER FAILURE)

LOAD TYPE	STRESS KSI	FAILURE MODE	PLY NO.	THETA	MATERIAL	SYSTEM
SCXXT SCXXC SCYYT SCYYC SCXYS	155.699 61.252 86.330 66.295 *******	SLIIT SLIIC SLIIT SLIIC N/A	4 4 2 2	0.0 0.0 90.0 90.0	ASIMLS SGLAHMHS	ASIMLS ASIMIS ASIMIS

MOTE: IF THERE IS NO ANGLE PLY "SCXYS" BASED UPON FIBRE FAILURE IS NOT PREDICTED.

Appendix C Resident Data Bank (FBMTDATA.BANK)

```
T300
      3000 0.300E-03 0.640E-01
  FP
  FE 0.320E 08 0.200E 07 0.200E 00 0.250E 00 0.130E 07 0.700E 06
  FT -0.550E-06 0.560E-05 0.580E 03 0.580E 02 0.170E 00
  FS 0.350E 06 0.300E 06
                           0.000
                                     0.000 0.000
  AS--
  FP 10000 0.300E-03 0.630E-01
  FE 0.310E 08 0.200E 07 0.200E 00 0.250E 00 0.200E 07 0.100E 07
  FT -0.550E-06 0.560E-05 0.580E 03 0.580E 02 0.170E 00
  FS 0.400E 06 0.400E 06 0.000 0.000 0.000
 SGLA
       204 0.360E-03 0.900E-01
 FE 0.124E 08 0.124E 08 0.200E 00 0.200E 00 0.517E 07 0.517E 07
 FT 0.280E-05 0.280E-05 0.750E 01 0.750E 01 0.170E 00
 FS 0.360E 06 0.300E 06 0.360E 06 0.300E 06 0.180E 06 0.180E 06
 HMSF HIGH MODULUS SURFACE TREATED FIBER.
 FP 10000 0.300E-03 0.703E-01
 FE 0.550E 08 0.900E 06 0.200E 00 0.250E 00 0.110E 07 0.700E 06
 FT -0.550E-06 0.560E-05 0.580E 03 0.580E 02 0.170E 00
 FS 0.280E 06 0.200E 06
                            0.000 0.000 0.000
 OVER END OF FIBER PROPERTIES.
IMLS INTERMEDIATE MODULUS LOW STRENGTH MATRIX.
MP 0.460E-01
ME 0.500E 06 0.410E 00 0.570E-04
MT 0.125E 01 0.250E 00
MS 0.700E 04 0.210E 05 0.700E 04 0.140E-01 0.420E-01 0.320E-01 0.320E-01
MV 0.225E 00 0.420E 03
IMHS INTERMEDIATE MODULUS HIGH STRENGTH MATRIX.
MP 0.440E-01
ME 0.500E 06 0.350E 00 0.360E-04
MT 0.125E 01 0.250E 00
MS 0.150E 05 0.350E 05 0.130E 05 0.200E-01 0.500E-01 0.350E-01 0.350E-01
MV 0.225E 00 0.420E 03
HMHS HIGH MODULUS HIGH STRENGTH MATRIX.
MP 0.450E-01
ME 0.750E 06 0.350E 00 0.400E-04
MT 0.125E 01 0.250E 00
MS 0.200E 05 0.500E 05 0.150E 05 0.200E-01 0.500E-01 0.400E-01 0.400E-01
MV 0.225E 00 0.420E 03
OVER END OF MATRIX PROPERTIES.
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